

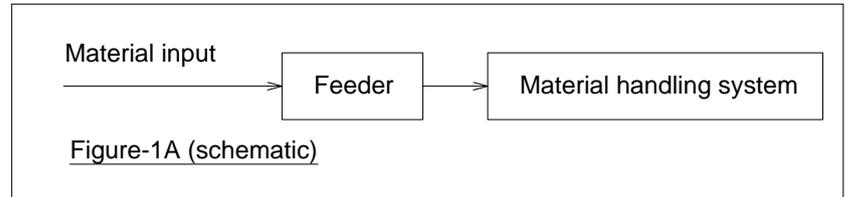
# SOME EXTRACTS FROM THE BOOK – BELT FEEDER DESIGN AND HOPPER BIN SILO

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## Chapter 1: FEEDER TYPES AND APPLICATION

### 1.1.0 NEED OF FEEDERS IN A SYSTEM

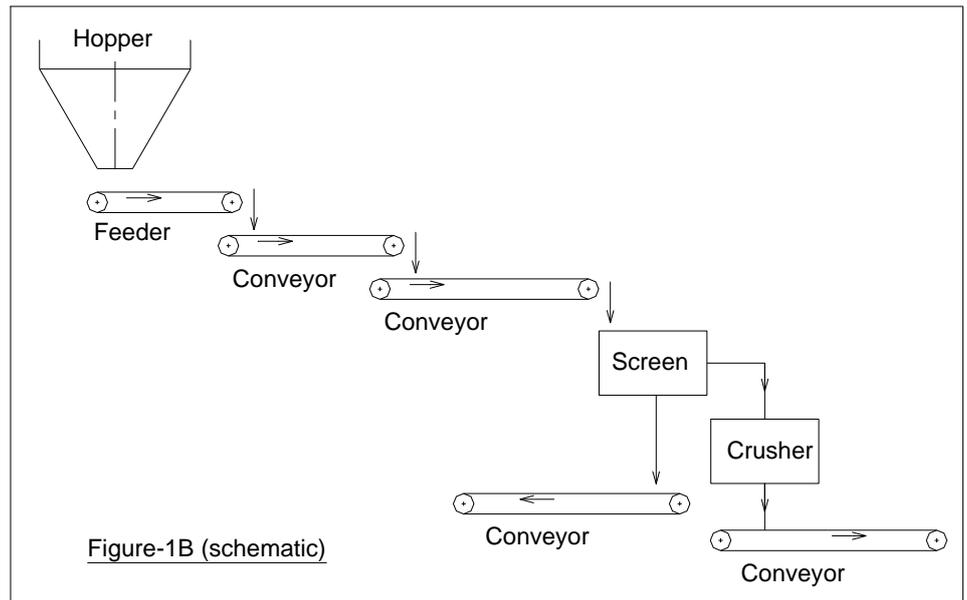
The properly designed bulk material handling system always commences from the feeder, i.e. first equipment in the system (or section of the system), should always be feeder. This is depicted



schematically in figure-1A. The feeder decides the magnitude of load on the system. Therefore, the system load condition and thereby its performance is governed / controlled by the feeder.

For example, a belt conveyor conveys the material; whatever quantity is loaded onto it. If the quantity is loaded on the belt is less than its capability, then it will run at partial capacity. However, if the quantity loaded is excessive then the

conveyor will be overloaded, spillage and even failure. The belt conveyor which has correct magnitude of load will have optimum performance, long life, maximum monetary return from investment. Similarly, if the receiving equipment happens to be crusher instead of conveyor, then, it will also have under-loading or correct-loading or overloading with



consequential outcome (there can be few types of crushers which are suitable for choke-feed, but then that crusher will be also working as feeder-cum-crusher).

As said before; any section of bulk material handling system always commences with feed control, i.e. mostly, by the equipment named as feeder. However, sometimes starting equipment may not be named as feeder, but it might actually be functioning indirectly as feeder also. For example, in a reclaiming system, the first equipment could be bucket wheel reclaimer. It is named as reclaimer, but in reality it is functioning as reclaimer and also as

feeder, because it is accepting only specific maximum quantity of material from stock pile and then passing it to down-line system.

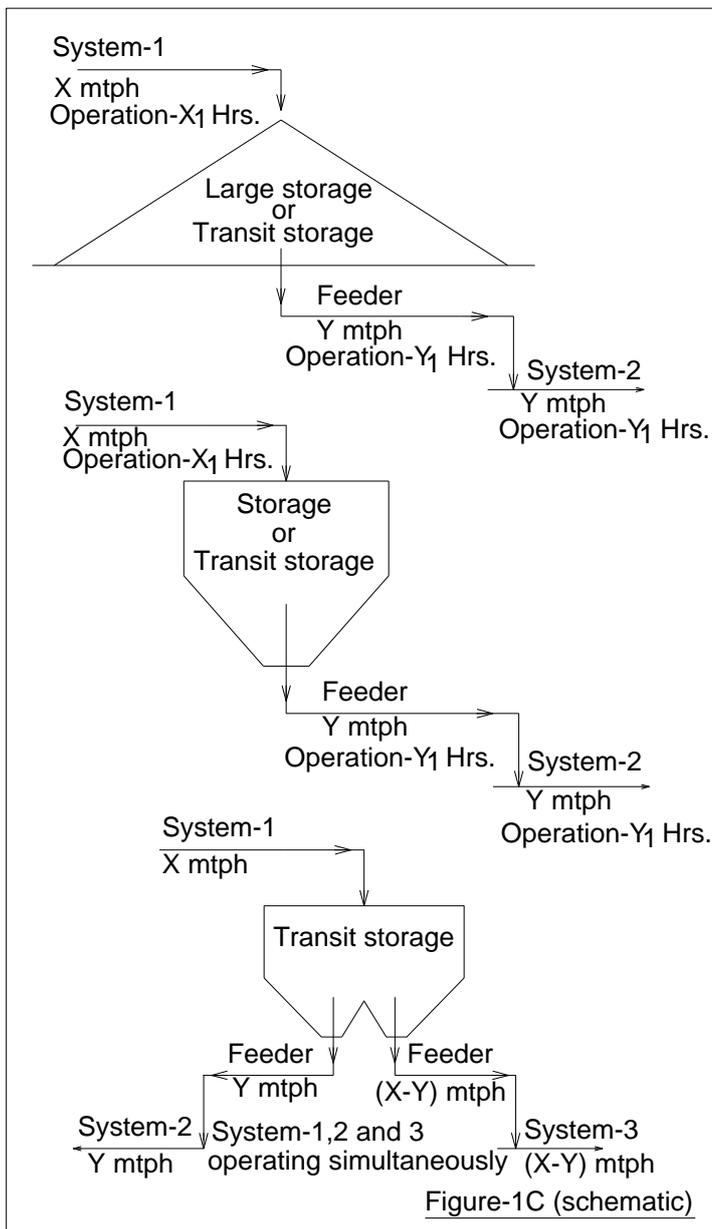
The bulk material handling system (or section of the system) is made-up of handling equipment in series. In this arrangement; the material from one equipment flows into second equipment, and from there to third equipment and so on; as shown in figure-1B (refer page 1). So far these equipment in series are operating simultaneously and at the same capacity, then there would not be feeder (for feed regulation) at intermediate point, as it would introduce disturbance into stabilised flow pattern. Thus, feeder is not required among series of equipment, when their operation is identical with respect to time and flow rate. In short, the first equipment in any section of bulk material handling system needs to be feeder or equipment with feed control. The subsequent equipment in that section does not need (have) feed regulation, unless its flow pattern is disturbed by items like storage facility.

However, if the interconnected systems have difference in operational time or difference in operational capacity, or difference in both together, then feeder would be needed at junction of such two systems, as shown in figure-1C. The figure shows some of the typical cases where feeders are needed. The reader to note that the difference in actual operational capacity for the two interconnected systems would result into material accumulation at junction, creating two sections of the material handling systems.

Case-1: The common example is stockyard system wherein in-coming and out-coming systems have differing values of flow rate and operating hours.

Case-2: This is similar to case-1, but interim storage is by underground hopper or over ground hopper / bin / bunker. The common example is wagon tippler system, wherein hopper is transitional in nature. The hopper receives the material in rapid cyclic pattern from wagon unloading system, but outflow is continuous. The other example is coal bunkers at boilers in power plant. The coal bunkers serve as interim storage as against transitional hopper of wagon tippler system. Similar example can be also seen at the end of in-coming mine conveyor at cement plant.

Case-3: The common example is coal received at power station, which is partly sent towards boiler bunker and partly towards stockyard.



## 1.2.0 TYPE OF FEEDERS

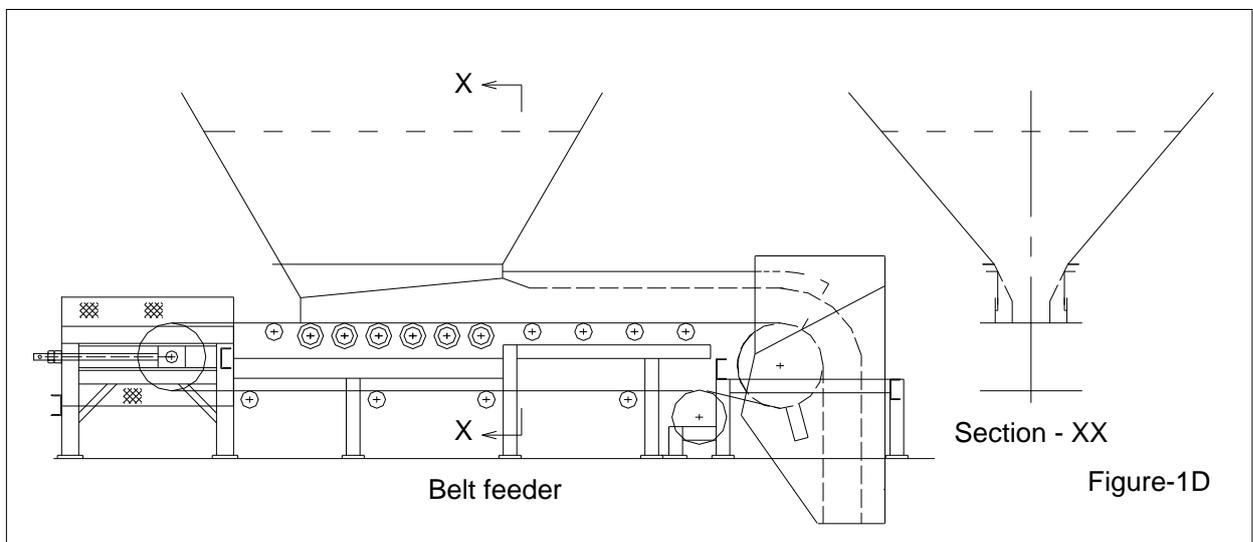
Various types of feeders have evolved during course of time, to suit differing needs of bulk material handling plants. The different types of feeders are needed because bulk materials can range from food grains, coal, minerals, granite, and so on which have altogether different physical characteristics. The different types of feeders are also required to suit the need for large difference in capacity ranging from few mtpm to mtpm in thousands. Mainly, following types of feeders are available for choice and needs:

- 1) Belt feeders
- 2) Apron feeders
- 3) Vibrating feeders (Electromagnetic)
- 4) Vibrating feeders (Mechanical)
- 5) Reciprocating feeders
- 6) Screw feeders
- 7) Drag chain / drag flight feeders
- 8) Rotary table feeders
- 9) Rotary van feeders
- 10) Rotary drum feeders
- 11) Rotary plough feeders

## 1.3.0 FEEDERS MAIN CHARACTERISTICS AND APPLICATION

### 1.3.1 Belt feeders

Figure-1D shows the belt feeder. The belt feeders are one of the widely used feeders. They are suited for handling of granular material or materials of comparatively lesser lump size (in comparison to apron feeder). The limitation of lump size depends upon toughness, hardness, abrasiveness and roughness of lumps. It also



depends upon flow cross section area (mtpm) in relation to lump size, and consequent room for lumps to adjust the position without creating undue pressure / abrasion / tear on belt.

The belt feeder is not recommended for very hard and tough material which have sharp cutting edges and comparatively of large lumps (i.e. belt feeder is not substitute to apron feeder). It is difficult to quantify this issue in simple or mathematical terms. In case of uncommon application, the designer has to check about the previous use of belt feeder in somewhat comparable situation in existing plants or his previous experience. Regarding basic rule for preliminary decision, the designer has to imagine that :

- 1) In case of large lumpy material, imagine that the lump/s are blocked momentarily (i.e. not moving with belt).
- 2) Lumps are pressing on belt due to pressure above and also additionally due to reshuffling reaction forces when the belt is trying to dislodge the jammed lumps (by eliminating arch formation in plane of belt). Such things continue to happen momentarily even without being observed.
- 3) In the situation stated above, imagine whether the sharp edges front part would get sheared off to make the lump edges blunt. If these edges front line are getting blunted, or the pressure is not high enough to create cut / puncture on belt, then belt feeder can suit.
- 4) In the situation stated above, imagine whether the sharp edges of lumps will get worn out by belt (also by material particles on belt), to make them blunt. If the edges extreme front line get blunted immediately, or the pressure is not high enough to create cut / puncture on belt, then belt feeder can suit the application.
- 5) If the points mentioned against serial number 3 and 4 are unfavourable; then the same can be overcome to certain extent by providing thick top cover to belt, making the use of belt feeder possible.

The aforesaid guidelines help in engineering judgement. The belt feeder use for granular or material of limited lump size, do not pose such dilemma.

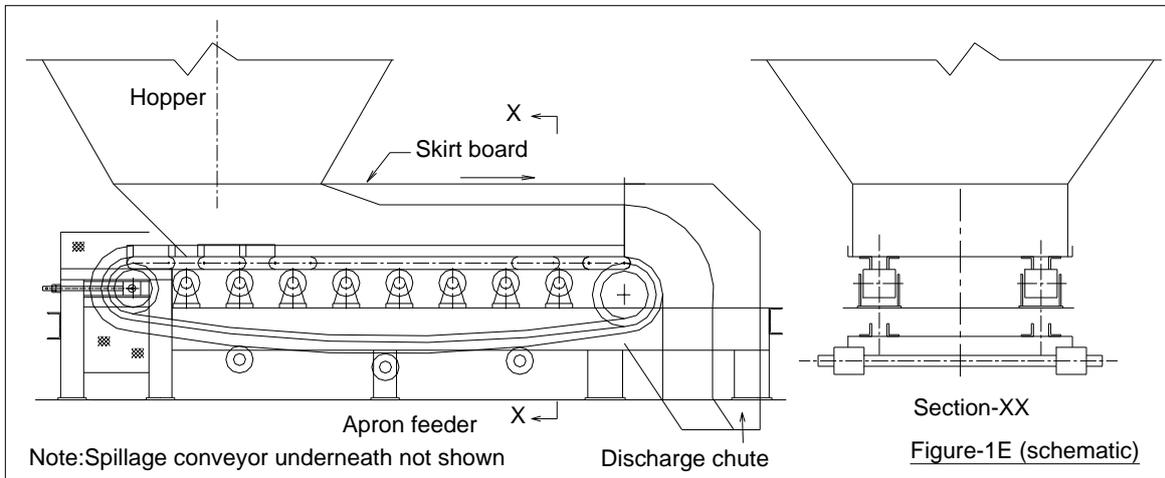
The belt feeder can extract the material from hopper outlet. The hopper outlet length along feeder, can be up to 7 to 8 meters in favourable situation (lesser the feed zone length, more favorable is the situation for belt life). The belt feeder center to center distance is different from this feed zone length. The virtual freedom in choosing center to center distance of belt feeder, provides excellent flexibility for optimum layout of associated portion of the plant.

The belt feeder discharge is positive volumetric in nature. The typical capacity range is up to 1500 m<sup>3</sup>/hour, for regularly used belt widths. However, belt feeders of higher capacities are also possible. As an example, a mine in Germany has 6400 mm wide belt feeder for handling lignite at much higher capacity.

### **1.3.2 Apron feeders**

Figure-1E shows the apron feeder. The apron feeder is used for dealing with materials which are very hard, abrasive, tough and for lumps of larger dimensions; which are beyond the scope of belt feeders. The boulders of even 1.5 m edge length dimension can be handled, because such lumps will be falling and carried by steel pans, which can have thickness of 6 mm to 40 mm. Again, at loading zone, the multiple support pads under the pans can be provided to withstand the impact of such large lumps.

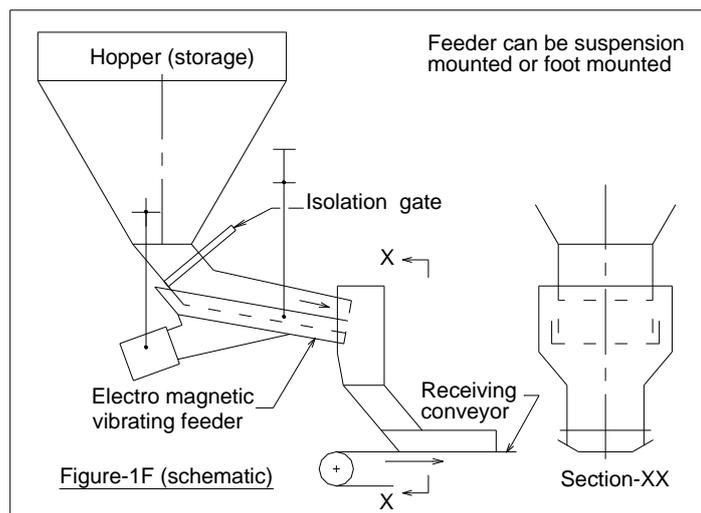
The apron feeder can extract material from hopper outlet. The hopper outlet length can be up to 7 to 8 m (lesser the length the more favourable is the situation). The discharge is positive volumetric in nature, if lump size is small compared to the flow cross section width and depth. The typical capacity range is up to 2100 m<sup>3</sup>/hour, for regularly used apron widths. The apron feeder is costly equipment but its sturdiness is not surpassed by other



feeders.

### 1.3.3 Vibrating feeders (electromagnetic)

Figure-1F shows the electromagnetic type vibrating feeder. These feeders are economical compared to other feeders; as number of items in equipment are very less. These are suited for granular materials or materials of limited lump size. The equipment does not fully extract the material from hopper, in true sense. Rather material is taken by the feeder tray in a controlled manner. The feeder discharge is susceptible to variation in flowability unless getting adjusted by close-loop control signal from belt weigher on subsequent conveyor. The susceptibility is relevant only if there is a wide



variation in flowability. The equipment is partially supporting material column in hopper, so it can deal with lumpy material comparable to belt feeder and material which can harm belt. However, tray is of comparatively less thickness and not so robust. Also, the limitation of power / force allows its application for granular to comparatively smaller size lump material. The material flows in a loose (fluidic) condition and so lumps jamming and forceful abrasion on tray is absent, (this is also due to reason that the equipment is not capable in dealing with full extraction of material like apron feeder or belt feeder).

The hopper outlet length along tray will be of specific (small) dimension, not like long opening (free dimension) in case of belt feeders / apron feeders. The equipment should be used with caution for wet or iron ore application (if electrical protections are not up to the mark). The typical capacity range is up to 600 m<sup>3</sup>/hour.

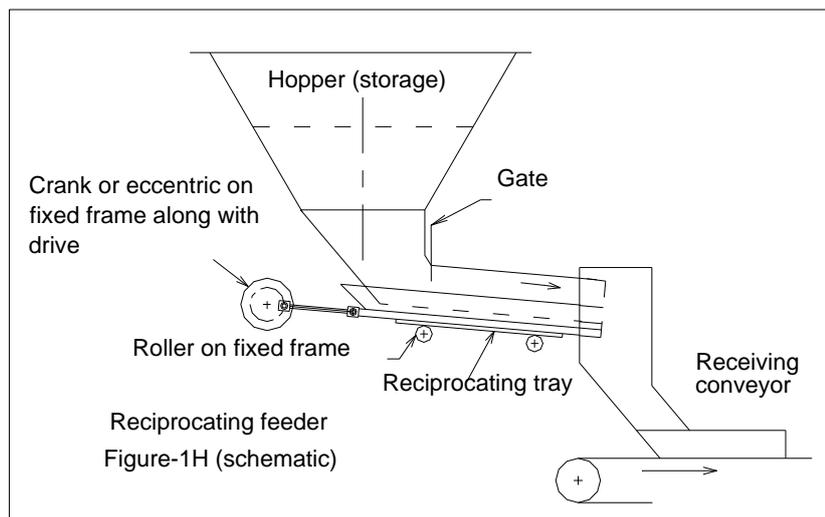
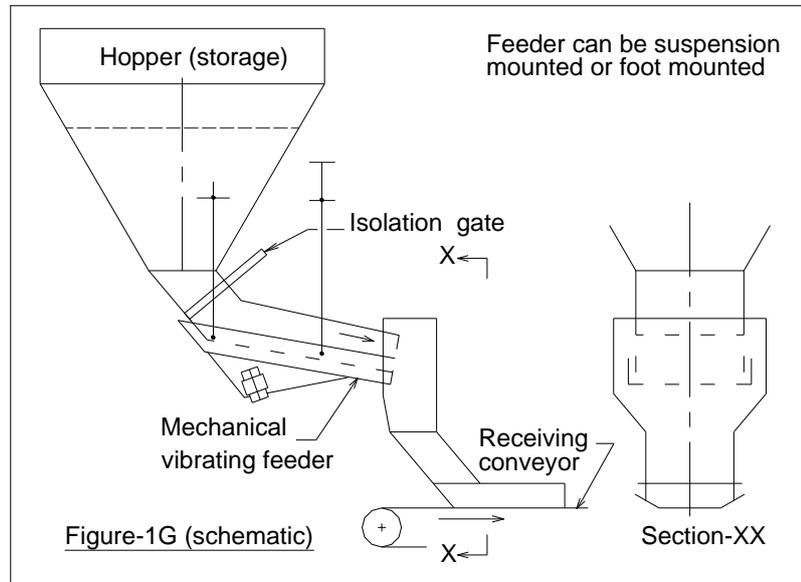
### 1.3.4 Vibrating feeders (Mechanical)

Figure-1G shows the mechanical type vibrating feeder. These feeders function like vibrating feeders (electromagnetic). However, vibrations are created by unbalanced rotating mass, hence tray size, power, force options and ranges are very large. The tray can be made

much stronger and robust, and so it can be used for comparatively difficult material and also for larger capacity. One can come across mechanical vibrating feeder for capacity up to 1100 mtp/h of coal or 3000 mtp/h for iron ore. The material flows in a loose (fluidic) condition and so lumps jamming and forceful abrasion on tray is absent (this is also due to reason that the equipment is not capable in dealing with full extraction of material like apron feeder or belt feeder).

The hopper outlet length along tray will be of specific (small) dimension, not like long opening in case of belt

feeders / apron feeders. Typical capacity range is up to 1250 m<sup>3</sup>/hour.



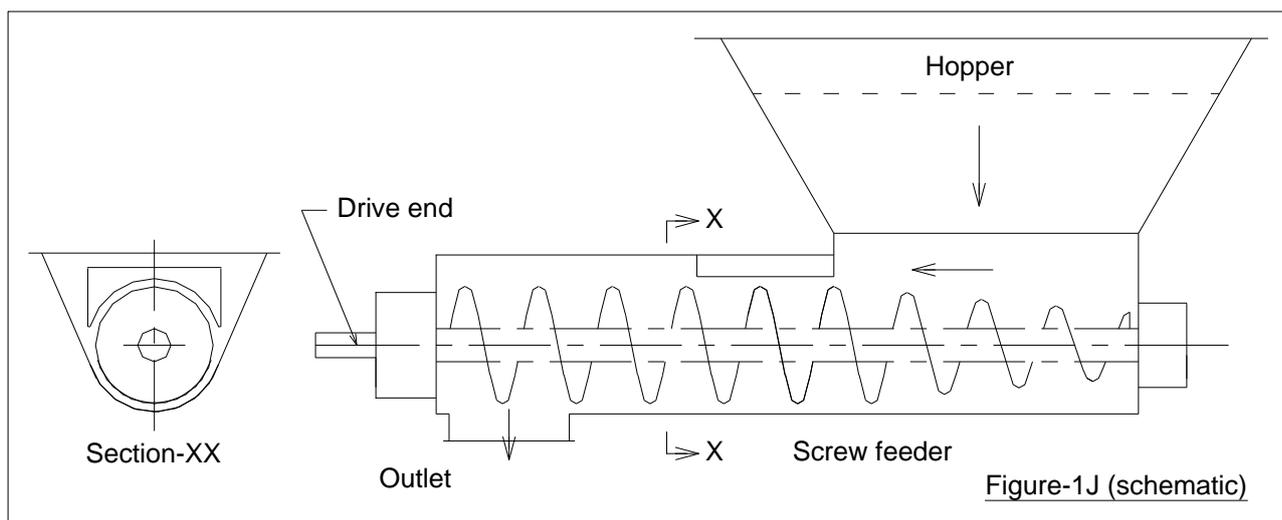
### 1.3.5 Reciprocating feeders

The reciprocating feeder arrangement is shown in figure-1H. This feeder is in use since very long time. The feeder has reciprocating tray. The reciprocating motion is imparted by crank or eccentric and connecting rod. The feeder discharge is volumetric in nature, and is less susceptible to flowability of material, as compared to vibrating feeder. However, material movement on tray is of simple dragging nature, instead of jumping type (in case of vibrating feeder). This results into more wear of tray. But still certain industries use the reciprocating

feeder. The magnitude of vibrating forces are comparatively high but at a very low frequency, say at about 60 cycle per minute. The commonly used reciprocating feeders have capacity range up to  $250\text{m}^3/\text{hr}$ , for material of average abrasiveness. The higher capacities are possible. The feeder can handle larger lumps, compared to vibrating feeder.

### 1.3.6 Screw feeders

Figure-1J shows the screw feeder. These feeders are suitable for material which are granular / powdery or which have small size lumps (in tens of mm). The feeder extracts the material from hopper. It provides totally enclosed construction from hopper to receiving equipment. The capacity range is less compared to earlier described feeders.

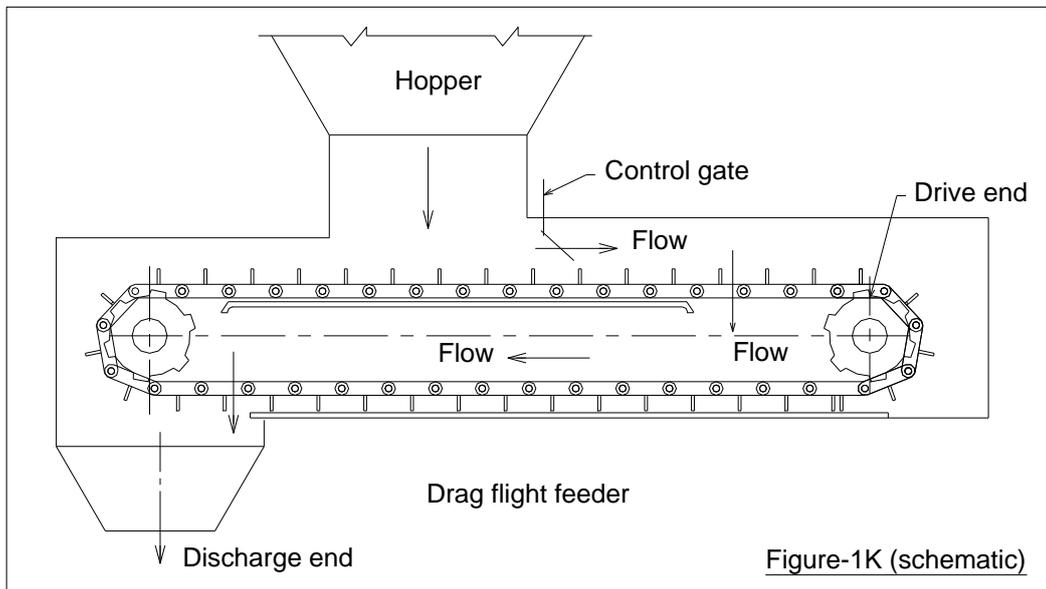


The material continuously rubs with flights and trough. So, abrasive material will cause faster wear. The feeder is extensively used in grain industries and for granular materials in process plants.

It is not used for materials which have tendency to pack or interlock and thereby difficult to shear or create flow. It should also be used with caution where material is likely to solidify during idle time. Feeder is simple and economical. The typical capacity range is up to  $200\text{ m}^3/\text{hour}$

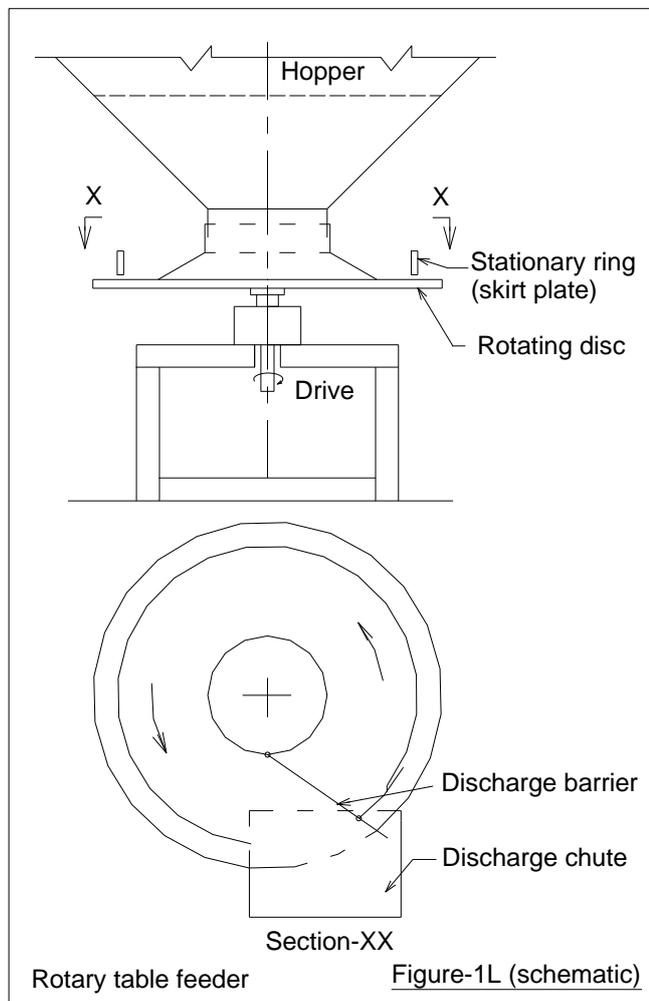
### 1.3.7 Drag chain / Drag flight feeders

Figure-1K shows the drag chain / drag flight feeder. The feeder extracts the material from hopper. It is suitable for materials of moderate size lumps and of average abrasiveness. The hopper outlet can have some length along feeder. It can provide enclosed construction. The feeder needs minimum installation heights, it also imparts agitation to material at outlet, i.e. improves flow at hopper outlet. Typical capacity range is up to  $100\text{ m}^3/\text{hour}$ .



### 1.3.8 Rotary table feeders

Figure-1L shows the rotary table feeder. These feeders are suitable to install under hopper outlet of larger diameter to prevent clogging by sluggish material. The feeders are suitable for non abrasive and marginally abrasive materials. The material continuously rubs / slides on table, however, table can be fitted with thick liner if needed. Discharge is volumetric in nature. The capacity range is limited, say up to 20 m<sup>3</sup>/hour.

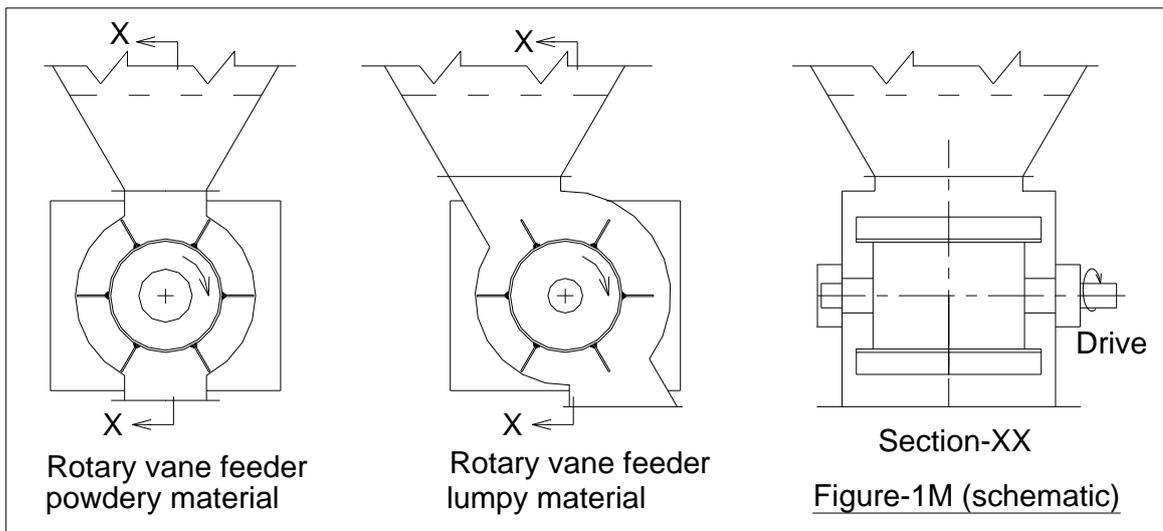


### 1.3.9 Rotary vane feeders

Figure-1M shows the rotary vane feeder. These feeders are particularly used to discharge fine freely flowing material from hopper, while maintaining sealing so that air / gases do not flow into hopper, when hopper is under negative air pressure. These feeders are regular features for discharge of dust from dust collection hopper / enclosure in a dust extraction plant. These feeders can be also used when

such sealing is not required. The discharge is positive volumetric in nature. The other area of application can be process plant, where material is to flow in a totally enclosed construction. The feeder is suitable for materials,

which are free flowing and non-sticky. This feeder application competes with screw feeder, but this is not so popular as screw feeder. However, if feeding is to be accomplished with minimum horizontal displacement, then this feeder will be the choice.



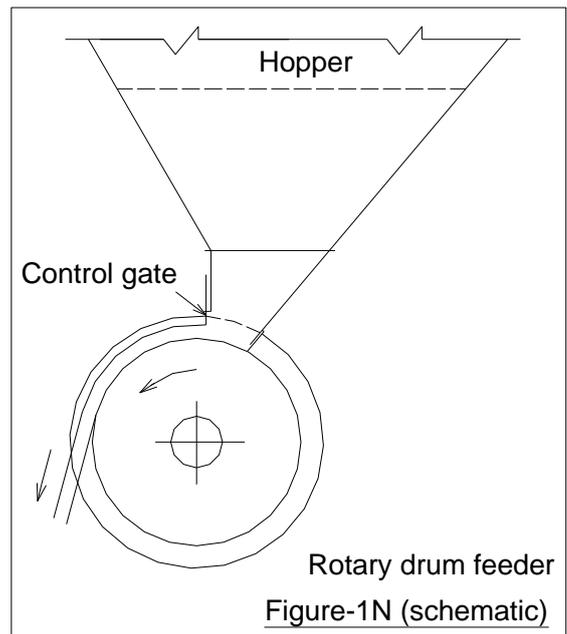
### 1.3.10 Rotary drum feeders

Figure-1N shows the rotary drum feeder. This simple and sturdy feeder is suitable for free flowing and small lump material. It extracts the material from hopper. The discharge is positive volumetric and accurate. This feeder is not suitable for very abrasive materials in continuous duty application. It is also not suitable for sticky material. The material rubs continuously with rotating periphery. The typical capacity range is up to 150 m<sup>3</sup>/hour.

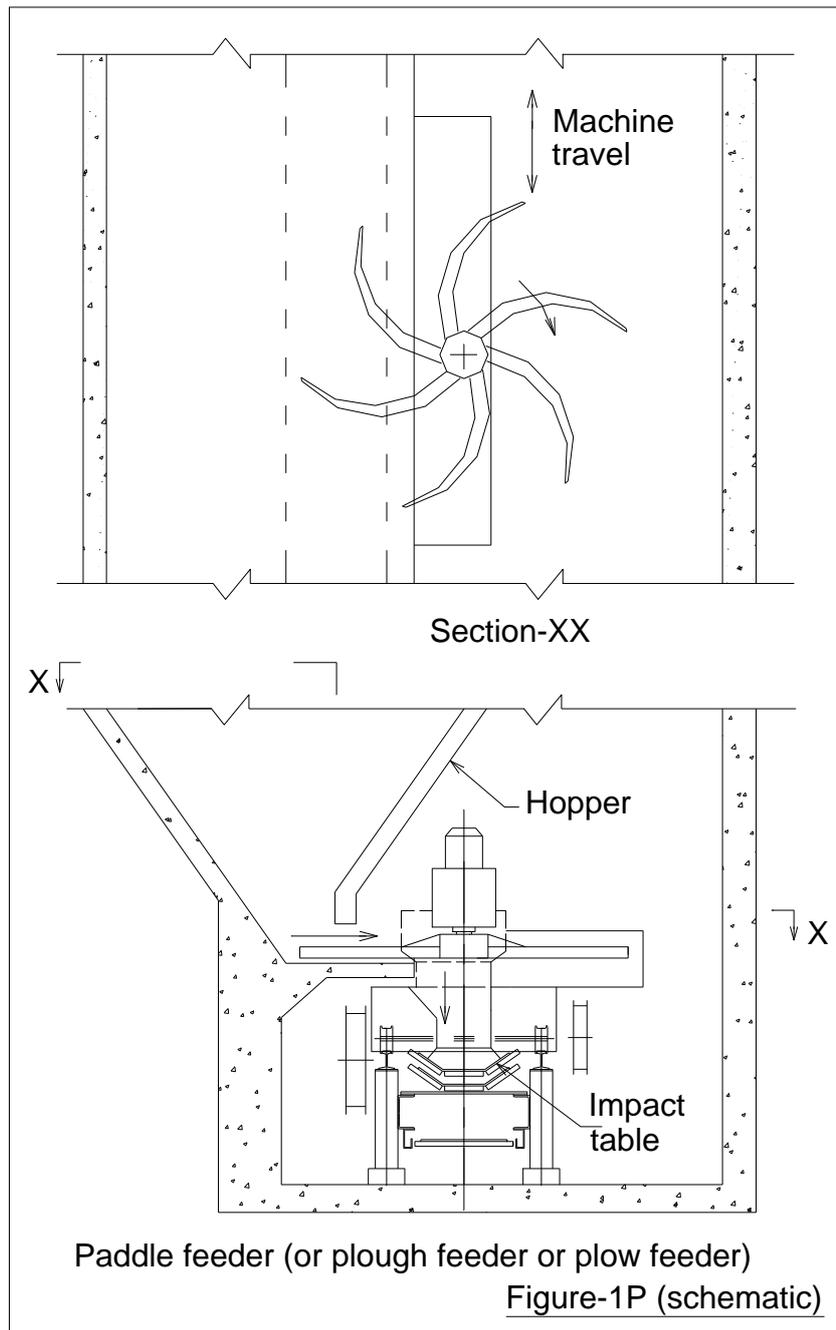
### 1.3.11 Paddle feeders (or plough feeders or plow feeders)

Figure-1P shows the paddle feeder. Generally, this is travelling type and extracts material from hopper-shelf.

The feeder travel and thereby hopper outlet length can be up to 200m or so. This feeder is suitable to operate in tunnel under stockpile. The feeder along with civil work is an expensive proposition, and is used to reclaim material from track hopper or long stockpile on storage-yard. The feeder can deal with practically any material, and in large capacity range. The feeder requirement in a particular layout arrangement is without alternative option of matching performance. Thus, this feeder does not compete with other feeders, but competes with other reclaiming machines. It is more as reclaiming machine-cum-feeder. The feeder extracts the material forcefully and so, it can also deal with materials, which have tendency to pack or interlock. The typical capacity range is up



to 1250 m<sup>3</sup>/hour. More capacity is also possible. In general, this is used for lump size up to 450 mm. This depends upon the characteristics of material.



## Chapter 2: INTRODUCTION TO BELT FEEDER

This chapter has **7 pages**. Following 2 pages write-up is typical.

### BELT FEEDER FUNCTION

The purpose and function of belt feeder is to draw out specific quantity (m<sup>3</sup>/sec) of material from hopper, for discharging in to onward system. The specific quantity could be as per pre-setting or as dictated by manual /

automatic command. The equipment like conveyor, crusher, screen, etc., if placed directly below hopper, same will get flooded with material from hopper. This will result into overloading of this equipment, because this equipment can not be provided with constructional feature for taking only set quantity of material (exception is some crusher suitable for choke feed). In fact there would be chaos in entire system, in absence of feeder below hopper.

The belt feeder is placed below the hopper. The belt feeder also gets flooded with material (choke feed). However, it is designed to work in this condition and take only set quantity ( $m^3/sec$ ) of material, even though more quantity of material is present in the hopper.

Referring to figure- 2A & 2B, the belt feeder skirt board is flange connected with the hopper outlet (or adapter outlet). Thus, hopper skirt board and belt forms totally enclosed space. The material in the hopper has continuity through skirt board, and rests (presses) directly on the belt, due to gravitational force.

Thus material is directly pressing on belt, all the time, and hence there exists frictional grip between belt and material. In view of this frictional grip, the belt forward motion drags the material along with it. However, entire body of material in hopper, can not move forward due to following reasons:

- The belt motion tends to drag the body of material forward, but hopper (adapter) front wall acts as barrier except for opening at exit end of hopper.
- There is frictional grip between material and hopper / skirt walls, which opposes the material movement forward.
- The material body is subjected to forward forces by tractive pull and backward forces by frictional resistances. This opposing force results in to shearing of material at weakest plane. Accordingly, part of material in contact with belt moves forward, whereas balance material tends to be stationary.
- Not withstanding the numerous intricacies of internal forces and internal movements within material, finally the material quantity which is emerging out at hopper outlet front end is specific in accordance with front end opening area and belt velocity. This is so, because material is being pulled out by belt, under choke feed situation.
- The material quantity  $Q_v$   $m^3/sec$  drawn out from hopper, and which would be discharged by belt feeder at head pulley is given by following formula:

$$Q_v = (\text{front end opening area } m^2) \times (\text{material cross section average velocity at this opening, } m/sec).$$

The material cross section average velocity at hopper exit is subjective to specific application, on case to case basis. This could be in the range of 0.70 to 0.85 of belt velocity. As a general statement, considering this to be 0.75 of belt velocity, the formula can be written as below:

$$Q_v = (\text{front end opening area } m^2) \times [(\text{belt velocity } m/sec) \times 0.75]$$

$$= (\text{skirt inside width at exit}) \times [(\text{opening height at exit}) \times 0.75] \times (\text{belt velocity}) \quad m^3/sec$$

The above formula clarifies the basic functional nature of belt feeder discharge. For more clarity, refer chapter-6 and chapter-7.

It is evident from this formula that  $Q_v$  is volumetric in nature and can be adjusted by front end opening area or by adjustment in belt velocity. Accordingly, the belt discharge rate is controlled as below:

- 1) The control gate (i.e. front end opening height adjustment gate / slide plate) is always provided in belt feeder. This enables to manually change the opening height and thereby flow area at exit section. This is widely used to control flow rate for many of the feeders dealing with granular material or when lump size is not large, and when push button adjustment is not needed.

- 2) The variable speed drive enables to vary the feeder discharge because discharge is directly proportional to belt velocity. So slower speed is used for lesser discharge, and faster speed for more discharge. The operator makes the speed setting to suit required discharge. Thus this arrangement enables push button control of discharge rate. The variable speed drive can be also used for automatic control of belt speed so as to have set value of discharge rate (mtph), by electrical inter-lock with belt weigher on subsequent conveyor.

Most of the time belt feeders are set to discharge specific  $m^3/sec$ . In case one is trying to change the discharge rate frequently, the following aspects and limitation of the whole system should be taken in to consideration:

- Hopper filling rate multiplied by filling duration, in certain time cycle.
- The hopper should have enough storage capacity to balance out its inflow and outflow, in the aforesaid time cycle. In short, feeder discharge rate should not be changed arbitrarily; ignoring the hopper inflow cycle, hopper storage capacity and hopper outflow (feeder discharge). Otherwise, this can result into flow imbalance and system tripping and non-workable system.
- As said before, belt feeder discharge rate is volumetric in nature and this can be converted in to mtpm as below.

$$\text{The feeder discharge rate in mtpm} = (\text{volumetric discharge } m^3/sec) \times 3600 \times (\text{bulk density } kg/m^3) \div 1000 = 3.6 \times (\text{volumetric discharge } m^3/sec) \times (\text{bulk density } kg/m^3) \quad \text{mtpm}$$

### Chapter 3: BULK MATERIALS

This chapter has **10 pages**. Following 1 page write-up is typical.

**Table-2 : Common materials repose angle and wall friction coefficient**

Material	Repose Angle degrees	Material and surface friction coefficient $\mu_s$	
		Case-1	Case-2
Ash fly	41	0.50	0.60
Barley	24	0.25	0.35
Cement clinker	44	0.45	0.55
Cement portland (non-aerated)	37	0.40	0.45
Coal bituminous	36	0.44	0.49
Coal bituminous, fines	41	0.40	0.50
Coke	35	0.50	0.55
Granite, blackish (-) 75 mm	38	0.47	0.57
Gravel (river)	37	0.40	0.48
Iron Ore Pellets	36	0.50	0.55

Material	Repose Angle degrees	Material and surface friction coefficient $\mu_s$	
		Case-1	Case-2
Lignite (dry)	37	0.475	0.55
Limestone	37	0.42	0.50
Limestone, fines	38	0.40	0.50
Maize	34	0.23	0.36
Sand dry	37	0.38	0.48
Slag clinker	38	0.50	0.60
Soya beans	27	0.25	0.38
Sugar	37	0.45	0.50
Wheat	30	0.24	0.38

**Note :** 1) The table-2 indicates average values. These can vary as per source. Use specific values for contractual needs.

- 2) Case-1  $\mu_s$  : This is applicable to plain and fairly even surface of steel, aluminum, average plastic; without protruding edges. Flush and welded steel surface would be of this type.
- 3) Case-2  $\mu_s$  : This is applicable to surface of medium smoothness / evenness, such as welded steel flush surface (below average), smooth concrete, wood planks, protruding edges, bolt head rivets etc.
- 4) The designer can also use  $\mu_s$  value in between case-1 and case-2. This data is not applicable to corrugated surface.

## Chapter 4: HOPPER, BIN, SILO AND BUNKER

This chapter has **14 pages**. Following 4 pages write-up is typical.

### HOPPER, BIN, SILO AND BUNKER

The hopper, bin, silo and bunker name / word is not used very systematically and carefully, and hence, its scientific definition / clarity is blurred. In earlier time, the use of these names was very limited to specific item, as per traditional vocabulary in particular profession. For example farmer will say grain-bin to the container he is using for storing grains, silo for storing silage (green grass) at farm and coal bunker to underground coal storage near his house.

These items (hopper, bin, silo and bunker) are very important and inevitable features in bulk material handling industry. People in industry are often using any of these names just to mean it as 'A container in plant to accommodate bulk material'. However as per Oxford dictionary, these names convey following meaning, as a part of general vocabulary.

Hopper: A container shaped like 'V' to hold grain, coal, etc. and lets it out through bottom.

Bin: A container with lid on top to store material. The bin could mean very large container and also very small container (like dustbin). This definition does not mention inverted 'V' shape at bottom.

Silo: Relatively tall container at farm to store grain, or underground civil structure to keep silage (green grass, etc.), or underground structure to keep missiles and / or dangerous goods. This definition does not specify provision for bottom outlet.

Bunker: An underground type structure for shelter or for placing guns or for storing coal, etc. in a ship or outside house. This definition also does not mention inverted 'V' shape at bottom.

So common feature of all these four names is that each imply it 'A container to accommodate material'.

Possibly, following technical definitions will help the owner while selecting / using the name in context of bulk material handling industry (of course there are no hard and fast rules as per practice in industry).

Hopper: The frustum of pyramid or cone, in inverted position, without vertical faces or having vertical faces of limited height. Hopper is required for functional purpose and for some storage (where storage is not so dominant).

Bin: Container mainly used for storage capacity, with tall vertical faces. The bin as understood in bulk material handling vocabulary could have flat bottom or inverted frustum of pyramid at bottom or inverted frustum of cone at bottom. The storage aspect is dominant for bin.

Silo: This can be understood same as for bin, i.e. Container mainly used for storage capacity, with tall vertical faces. The silo as understood in bulk material handling vocabulary could have flat bottom or inverted frustum of pyramid at bottom or inverted frustum of cone at bottom. The storage aspect is dominant for silo.

Bunker: Container mainly used for storage capacity. Original reference implied strongly constructed item for storage below ground or below working surface (i.e. storage in ship, etc). However, present day bulk material handling vocabulary also uses this word for overground storage, say coal bunker for boilers. Then it is synonymous to bin. The bunker will have bottom portion same as mentioned for bin.

As explained in foregoing write-up, the word hopper, bin, silo and bunker implies some specific aspects / features, but present day these are used in free style manner in industry; and so the reader has freedom to follow his choice, however, foregoing information will help to make better choice for name! In general, the name

mentioned by buyer becomes the name of the item in particular plant. The foregoing lengthy elaboration about name is not for hypothetical reasons, but directly concerns what name to be used here.

As for the issue of using name in this book; the situation is as below:

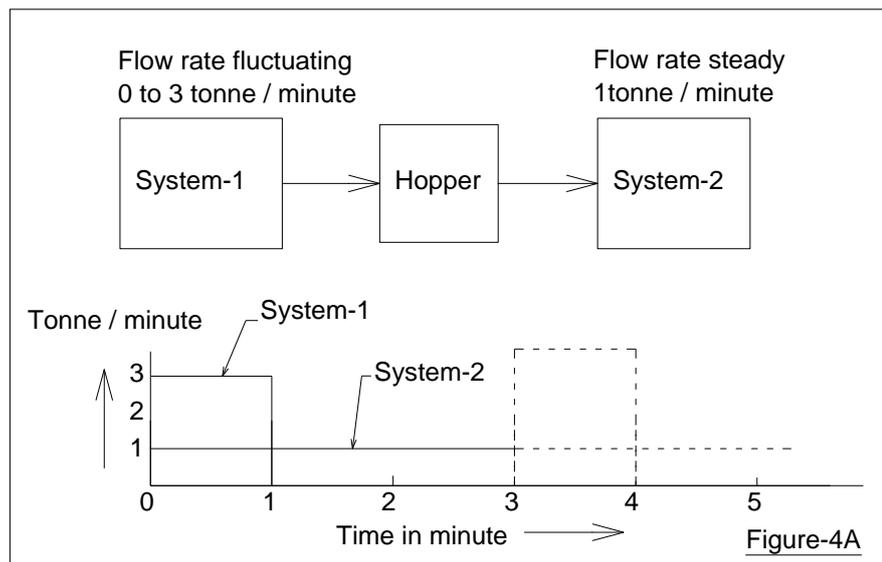
The bulk material storage container in bulk material handling plant will always have bottom discharge outlet and equipment at bottom. So, the hopper aspect is present most of the time and it should prevail. Thus, the right word for such storage container would be hopper, or (hopper + bin) or (hopper + silo) or (hopper + bunker). However using such theoretically correct name would make the presentation difficult and also uncomfortable for the reader. So, only one word hopper has been used in this book in following manner.

- **Word hopper is used in this book to mean the complete container for storing material.** The hopper of this book can have only converging portion or converging portion + vertical portion.
- To describe the engineering phenomenon or formula applicable to particular region of hopper, the issue has been addressed in this book by using words such as **'hopper vertical portion'** or **'hopper converging portion'**.

It would be better if reputed standards promote the use of only single name (for complete container) in bulk material handling industry, because dictionary meanings of various original names have artistic angle for sophisticated expressions, but the same are not relevant for bulk material handling industry today. Because these items are being used for storing all sorts of materials, ranging from iron ore pellets, minerals, fertilisers, salts and so on, which are at variance to original reference to hopper, bin, silo and bunker.

## HOPPER FUNCTIONS

The hopper/s are inevitable items in most of the plants for handling of bulk materials. The hopper is needed at the junction of two systems which have different values of instantaneous flow rates ( $m^3/sec$ ), and system themselves are not capable to absorb / cushion-out this difference in flow rate.



### Example-1

Calculate the gross and maximum effective capacity of hopper as shown in figure-4K. The material inside hopper is coal of (-) 50mm size, bulk density  $0.8 t/m^3$ , repose angle  $35^\circ$ . The material filling at top in area  $2m \times 2m$  at center.

Solution

The material maximum filling in hopper will be as shown in figure-4K. The filled volume to be divided into known shapes to enable calculation of capacity. The material from top face of 2m x 2m will spread laterally as per 35° repose angle. As the hopper cross section is rectangle, the sloping faces will intersect to two vertical faces as shown.

The material spread from each corner of top square will form conical surface. There will be 4 nos. of quarter cones i.e. all together will form one cone. However, these quarter cones base will not be flat but will be curved up-down-up in accordance with cone curved surface intersection with vertical planes at differing horizontal distance.

The hopper converging portion (imagine views without dotted extension lines below bottom outlet) would look like frustum of pyramid, but closer study shows it is not frustum of

pyramid. All the four edges are appearing in plan view but are not meeting at common point. If these four edges are meeting at common point, then these would also appear meeting at common point in plan view; because view of the point is same from any angle. This would be more clear by extending elevation and end view, below bottom outlet, as shown in dotted lines. These dotted lines are meeting at different place, in elevation and end view. So, converging portion is not frustum of pyramid. Instead it is frustum of wedge. The bottom converging portion volume can be computed as wedge of 3.4641 + 0.8659 = 4.33 m height minus wedge of 0.8659 m height. The material fill-up volume is as below, as per foregoing explanation.

Portion (1), cuboid =  $2 \times 2 \times (1.05 + 0.70) = 7.0 \text{ m}^3$

Portion (2), prism =  $0.5 \times 2.5 \times 1.75 \times 2 = 4.375 \text{ m}^3$

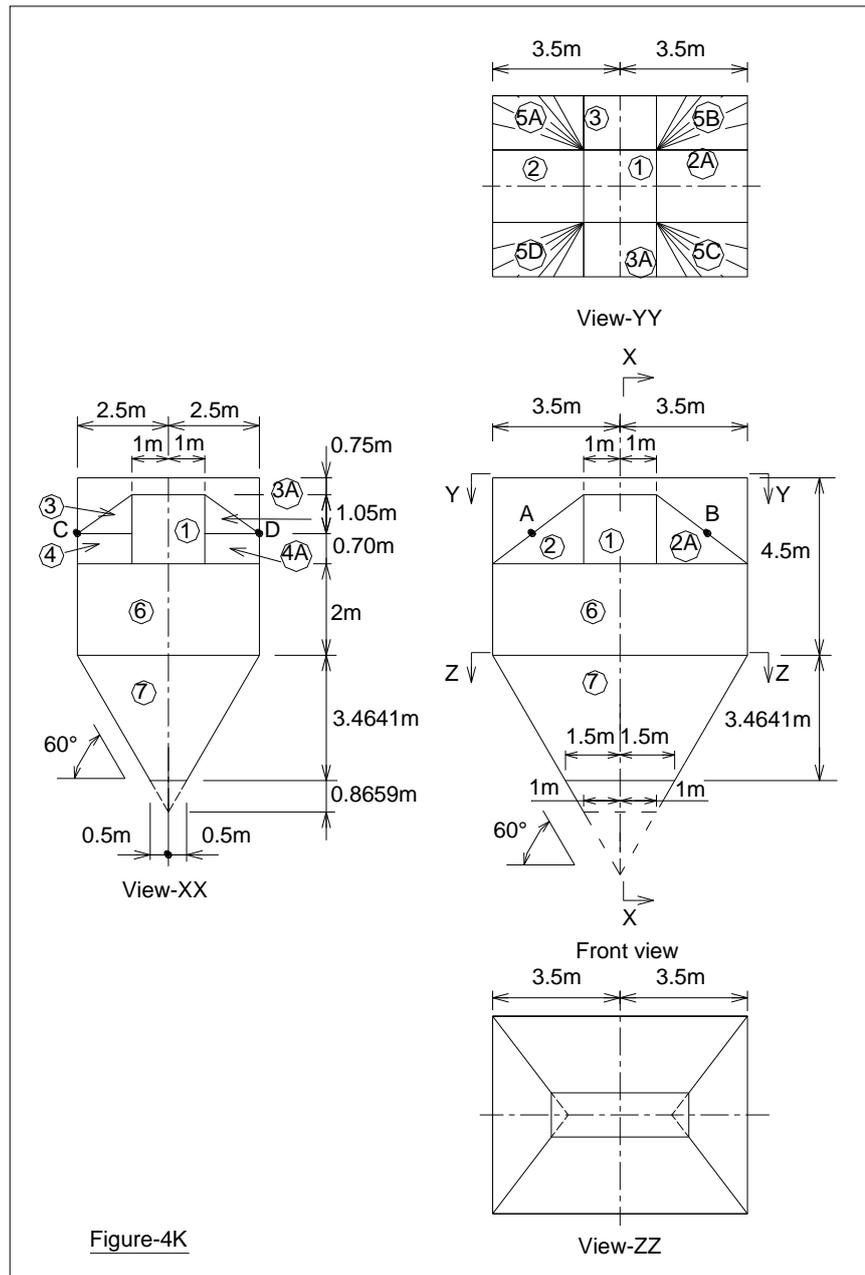


Figure-4K

$$\text{Portion (2A), prism} = 0.5 \times 2.5 \times 1.75 \times 2 = 4.375 \text{ m}^3$$

$$\text{Portion (3), prism} = 0.5 \times 1.5 \times 1.05 \times 2 = 1.575 \text{ m}^3$$

$$\text{Portion (3A), prism} = 0.5 \times 1.5 \times 1.05 \times 2 = 1.575 \text{ m}^3$$

$$\text{Portion (4), cuboid} = 1.5 \times 0.7 \times 2 = 2.10 \text{ m}^3$$

$$\text{Portion (4A), cuboid} = 1.5 \times 0.7 \times 2 = 2.10 \text{ m}^3$$

The four nos. of cone quadrant will make one cone. So, volume of one cone is computed. Looking to plan view, the base radius can be considered approximately as an average of  $(2.5 - 1.0) + (3.5 - 1.0) + \text{diagonal} = 1.5 + 2.5 + \text{diagonal}$ .

$$\text{Average radius} = \frac{\left(1.5 + 2.5 + \sqrt{1.5^2 + 2.5^2}\right)}{3} = 2.305 \text{ m}$$

$$\text{Its average height as } 0.5 \times [1.05 + (1.05 + 0.7)] = 1.4 \text{ m}$$

$$\text{Portion (5A) + (5B) + (5C) + (5D), cone} = \frac{1}{3} \times 1.4 \times \pi \times 2.305^2 = 7.785 \text{ m}^3$$

$$\text{Portion (6), cuboid} = 5 \times 7 \times 2 = 70 \text{ m}^3$$

$$\text{Portion (7)} = \frac{4.33 \times 5 \times (7 + 7 + 2)}{6} - \frac{0.8659 \times 1 \times (3 + 3 + 2)}{6} = 57.733 - 1.154 = 56.579 \text{ m}^3$$

Hence maximum effective volume :

$$= 7.0 + 4.375 + 4.375 + 1.575 + 1.575 + 2.10 + 2.10 + 7.785 + 70 + 56.579 = 157.464 \text{ m}^3$$

$$\text{Gross volume} = 5 \times 7 \times 4.5 + 56.579 = 214.079 \text{ m}^3$$

## Chapter 5: BELT SPEED AND CAPACITY FOR BELT FEEDER

This chapter has **24 pages**. Following 5 pages write-up is typical.

### BELT SPEED

Selecting the optimum belt speed is very important step in design of belt feeder. The belt feeder performance, life and price depend upon belt speed. The belt speed selection requires thoughtful understanding of bulk material characteristics and its action on belt described in foregoing cl.-5.4.1 to cl.-5.4.5. The belt speed is influenced by following points:

- The belt speed is less for material of higher abrasion capability. The belt speed is more for material of less abrasion capability.

The material abrasion capability is in proportion to total abrasion factor Aft. The total abrasion factor

$$Aft = \text{General abrasion } Af + \text{Lump factor } Lf$$

- The belt speed being used is somewhat less for heavy bulk material. This is due to reason that for same column height, the material force (pressure) and belt abrasion is more in case of heavy material. The material column height is same for equal values of friction angles, equal values of external features of lumps / granules and hopper arrangement; but independent of bulk density. So density aspect is to be incorporated in belt speed calculation. This influence is accounted by factor Df.

- The belt speed is comparatively less for difficult feed zone and is more for easy feed zone. This is due to consideration that the difficult feed zone results into more abrasion / wear of belt. This influence is accounted by feed zone factor Ff.

The belt speed basic formula is as below, in considerations to above influences (also refer page-56).

$$\begin{aligned} \text{Belt speed } v &= \left[ 0.1 + \frac{(0.5 - 0.1) \times (100 - Aft)}{100} \right] \cdot Df \cdot Ff \quad \text{mps} \\ &= \left[ 0.1 + 0.4 \times \frac{(100 - Aft)}{100} \right] \cdot Df \cdot Ff \quad \text{mps} \end{aligned}$$

The reader would be interested to know about the mentioned belt speed formula. This is based on following benchmarks:

- Belt speed of about 0.075 mps (15 fpm) is used in applications dealing with most difficult material and most difficult feed zone i.e. worst situation as permitted for belt feeder.
- Belt speed of about 0.5 mps (100 fpm) is used in applications dealing with very easy materials and easy feed zone.
- The observed speed values in practice for some of the intermediate materials.

The formula provides speed within this range in accordance with the application conditions.

The belt speed calculation always involves certain element of subjectivity, because most suitable speed will depend upon the exact nature of material and belt feeder hopper arrangement, which are specific to application. This should be given open thought and in case of doubt, opt for somewhat lower speed. The past experience / data, if available, should also be utilised in problems pertaining to application engineering.

The belt feeder located in constrained space (like mobile equipment) can have speed more than calculated, but same amounts to reduced life, as no option.

For grain like wheat, rice, etc., Aft is zero for use in this formula, which provides belt speed of 0.5 mps as an average value for grain. However, somewhat higher speed can be used for grain if material pressure is not very high (i.e. if hopper is not very deep).

The required input to this formula are described as below:

#### Abrasion total factor Aft

This factor is sum of following factors:

Aft = abrasion factor Af + lump factor Lf.

The value of Af is to be decided using table-3. This table mentions value of Af for model materials. Now, actual material to be handled by belt feeder may not be mentioned in this table. In such situation, compare the conventional abrasiveness of actual material with the listed material. The Af value of best matching material will also be Af value of actual material. The designer can also select intermediate value, in accordance with relative comparison.

The abrasive gradation such as A1, A2, A3, A4 or 6, 7, 8, 9, etc. are easily available for most of the materials, from published literature. This abrasive gradation provides easy guide to decide value of Af. However, visual inspection of material for refinement of decision is recommended for application and contractual design.

Similarly value of Lf is to be decided using graphs of figure-5D. The graph mentions value of Lf for model materials. So, actual material to be handled by belt feeder may not be mentioned in this graph. In such case

compare the abrasion / attrition capability of lumps of actual material, to the attrition capability of lumps of model material. The Lf value of best matching material will also be Lf value of actual material. The designer can also select the intermediate value, in accordance with relative comparison. The above mentioned lump attrition capability implies the lump capability to inflict abrasion / wear / deterioration of belt as a combined effect of lump hardness, lump toughness and sharp edges / corners on lump, as described under cl.-5.4.4.

Coming to the practical aspect of comparison of lump factor; it is necessary that the designer should see the actual material and also the model materials, to enable him to make correct judgement. The listed model materials like wheat, lignite, coal, limestone, cement clinker, granite, etc. are so common that the engineer with very little exposure to bulk material handling will come across and see these materials. It is possible that such materials might have been already seen in day to day life without specific exposure. As for the actual material, one can ask for sample or alternatively refer to published information on such material. Or reference should be made to buyer / producer to provide physical characteristics and description as to how it compare to model materials on concerned aspects. The experienced engineer can make comparative decision on visual inspect, because such decision relates to only one issue i.e. **how good / bad is material lump for damage / abrasion to belt.**

The other alternative option is to ask for numerical values of hardness, toughness, etc. of lumps which demands testing of reasonable number of sample. This is expensive and time consuming. Thus , values of Af and Lf are decided as explained in foregoing write-up. The value of Aft is:

$$Aft = Af + Lf.$$

#### Bulk density factor Df

$$Df = 1.0 \quad \text{if material bulk density} \leq 1000\text{kg/m}^3$$

$$Df = 0.95 \quad \text{if } 1000 \text{ kg/m}^3 < \text{Bulk density of material} \leq 1650 \text{ kg/m}^3 \text{ (i.e. when bulk density is more than } 1000 \text{ kg/m}^3, \text{ and up to } 1650 \text{ kg/m}^3.$$

#### Feed zone factor Ff

This factor depends upon skirt board arrangement, feed zone length, feed zone width and lump factor. Thus it is inter dependent on lump factor also. This is due to reason that the difficult lumpy material and difficult feed zone combine effect is “geometric (more than proportionate)” in nature.

The values of feed zone factor Ff are as below:

$$\text{Most easy or easy feed zone } Lf \leq 25 : Ff = 1.0$$

$$\text{Most easy or easy feed zone } Lf > 25 : Ff = 0.90$$

$$\text{Difficult feed zone } Lf \leq 25 : Ff = 0.90$$

$$\text{Difficult feed zone } Lf > 25 : Ff = 0.80$$

$$\text{Most difficult feed zone } Lf \leq 25 : Ff = 0.85$$

$$\text{Most difficult feed zone } Lf > 25 : Ff = 0.75$$

The aforesaid values are primarily for industrial materials. In case of grains like wheat, rice, etc., Ff can be considered generally as 1.0 or in very adverse conditions as 0.9.

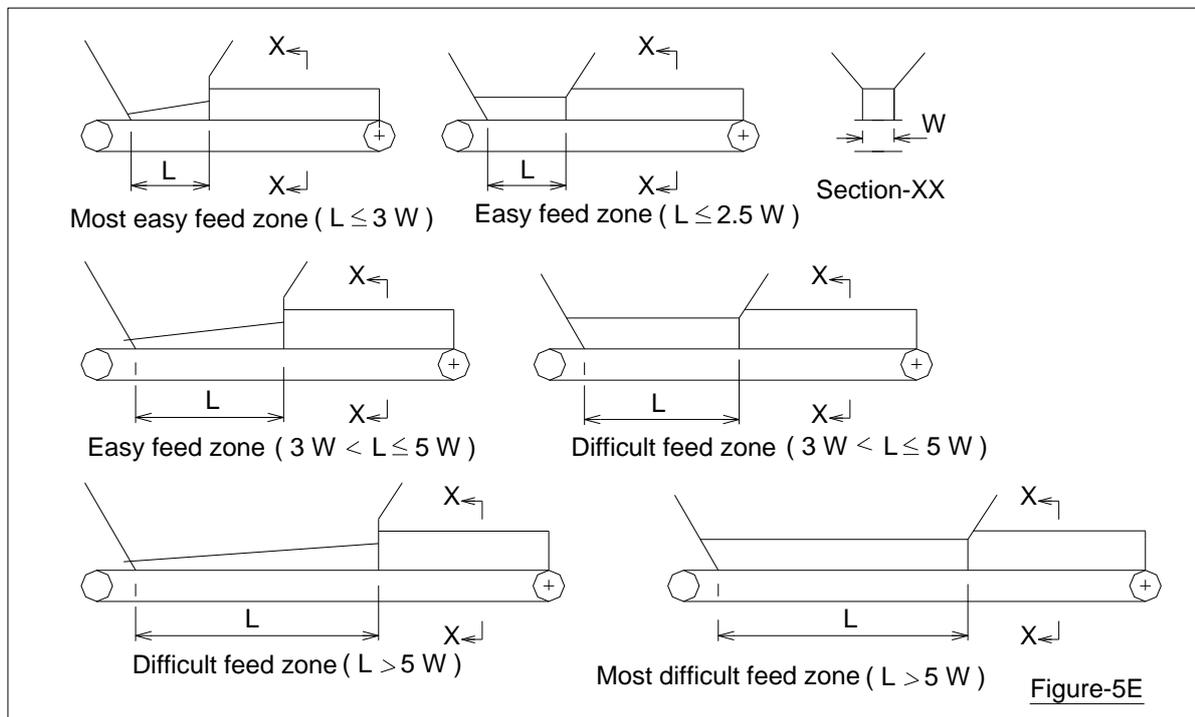
Thus to decide Ff, one has to decide lump factor Lf and feed zone type i.e. whether easy type, difficult type, more difficult type, etc.

The lump factor Lf is known as per clause 5.4.5.

Referring to figure-5E, the decision for feed zone type whether most easy, easy, difficult or most difficult; requires relative value of L and W, which are yet not known (in fact the exercise is to find the values of L and W). To circumvent this obstacle, consider feed zone arrangement at midway, say ‘difficult’, while making first time

calculation, and decide  $F_f$  accordingly. Use this  $F_f$  value to calculate preliminary belt speed. Thus, having decided the preliminary belt speed, the preliminary value of  $W$  becomes known as per clause-5.7.0. This becomes an input to next stage design process, to derive real value of  $W$ . This is the standard process of first stage design becoming input to second stage design to reach the final value. The design procedure will be clear from the example.

Firstly, decide the preliminary elevation view of the proposed arrangement for belt feeder, as shown in following figure-5E, (depiction is as per scale).



The belt feeder feed zone arrangement can be as per any one of the arrangement in figure-5E. These arrangements elevation views (feed zone length) depends upon technical requirements such as starting point of belt feeder, ending point of belt feeder, feed zone length to suit dimensional constrain, hopper outlet size, etc. These are already known to suit the overall plant arrangement. The preliminary value of  $W$  is already decided as mentioned in foregoing write-up Hence preliminary plotting or assessing of the applicable arrangement is possible (This refers to only preliminary arrangement). This would enable to decide second stage value of  $F_f$ . Having decided the value of  $A_f$ ,  $L_f$ ,  $A_{ft}$ ,  $D_f$  and  $F_f$  as explained in foregoing write-up, calculate the belt speed  $v$  as below:

$$\text{Belt speed } v = \left[ 0.1 + 0.4 \times \frac{(100 - A_{ft})}{100} \right] \cdot D_f \cdot F_f \quad \text{mps}$$

Above calculated speed when equal or larger than approximately 0.125 mps (25 fpm), the same to be amended by following factors, if applicable.

Material pressure factor 1.0; for  $C_2 \leq 2.25$ .

OR material pressure factor 0.925; for  $2.25 < C_2 \leq 3.5$

OR material pressure factor 0.85; for  $3.5 < C_2 \leq 4.5$ .

Lump numerical dimension factor 0.95; for lump dimension  $\geq 170$  mm.

OR Lump numerical dimension factor 0.9; for lump dimension  $> 250$  mm, subjects to experience.

The pressure factor  $C_2$  is for dynamic (continuous operation) condition. Refer chapter-8, cl.-8.14.4, page- 206, for definition of  $C_2$ .

The above factors are as per engineering judgement and the designer can adopt this speed or review / refine this value on the basis of his specific experience and other data.

### EXAMPLES - 1 TO 7

Decide the belt speed for wheat, lignite, coal less hard, hard coal, limestone less hard, hard limestone, and granite, for following situations.

- Lumps of good shape, maximum size
- Lumps of good shape, 1/2 maximum size
- Lumps of good shape, 1/4 maximum size
- Lumps of bad shape, maximum size
- Lumps of bad shape, 1/2 maximum size
- Lumps of bad shape, 1/4 maximum size

Decide the above speed considering easy feed zone to belt feeder, and also considering difficult feed zone to belt feeder. The material bulk densities are as below :

Wheat :  $770 \text{ kg/m}^3$

Lignite :  $800 \text{ kg/m}^3$

Coal less hard :  $800 \text{ kg/m}^3$

Coal hard :  $800 \text{ kg/m}^3$

Limestone less hard :  $1400 \text{ kg/m}^3$

Hard limestone :  $1400 \text{ kg/m}^3$

Granite :  $1440 \text{ kg/m}^3$

Following example -5 and 7 have only been presented here.

Example - 5 : limestone, less hard :

Referring to table-3 and graph figure-5D, the values of  $A_f$  and  $L_f$  are as below :

The value of  $A_f = 24$

$L_f = 27$  (Maximum size and good lumps)

$L_f = 21$  ( $\frac{1}{2}$  Maximum size and good lumps)

$L_f = 17$  ( $\frac{1}{4}$  Maximum size and good lumps)

$L_f = 38$  (Maximum size and bad lumps)

$L_f = 27$  ( $\frac{1}{2}$  Maximum size and bad lumps)

$L_f = 21$  ( $\frac{1}{4}$  Maximum size and bad lumps)

The bulk density factor  $D_f = 0.95$ , as density is greater than  $1000 \text{ kg / m}^3$

For  $L_f$  less than or equal to 25, the feed zone factor  $F_f = 1.0$ , for easy feed zone.

For  $L_f$  less than or equal to 25, the feed zone factor  $F_f = 0.9$ , for difficult feed zone.

For  $L_f$  greater than 25, the feed zone factor  $F_f = 0.9$ , for easy feed zone.

For  $L_f$  greater than 25, the feed zone factor  $F_f = 0.8$ , for difficult feed zone.

The belt speed values in different situations are as below:

Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 27) \div 100] \times 0.95 \times 0.9 = 0.2531 \text{ mps}$

Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 27) \div 100] \times 0.95 \times 0.8 = 0.2249$  mps  
 $\frac{1}{2}$  Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 21) \div 100] \times 0.95 \times 1 = 0.304$  mps  
 $\frac{1}{2}$  Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 21) \div 100] \times 0.95 \times 0.9 = 0.2736$  mps  
 $\frac{1}{4}$  Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 17) \div 100] \times 0.95 \times 1 = 0.3192$  mps  
 $\frac{1}{4}$  Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 17) \div 100] \times 0.95 \times 0.9 = 0.2872$  mps  
Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 38) \div 100] \times 0.95 \times 0.9 = 0.2154$  mps  
Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 38) \div 100] \times 0.95 \times 0.8 = 0.1915$  mps  
 $\frac{1}{2}$  Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 27) \div 100] \times 0.95 \times 0.9 = 0.253$  mps  
 $\frac{1}{2}$  Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 27) \div 100] \times 0.95 \times 0.8 = 0.2249$  mps  
 $\frac{1}{4}$  Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 24 - 21) \div 100] \times 0.95 \times 1 = 0.304$  mps  
 $\frac{1}{4}$  Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 24 - 21) \div 100] \times 0.95 \times 0.9 = 0.2736$  mps  
The above calculated speeds are to be multiplied by pressure factor and lump numerical dimension factor, if applicable. In general lumps would be somewhat "bad".

Example - 7 : Granite :

Referring to table-3 and graph figure – 5D, the values of Af and Lf are as below :

The value of Af = 40

Lf = 42 (Maximum size and good lumps)

Lf = 32 ( $\frac{1}{2}$  Maximum size and good lumps)

Lf = 26 ( $\frac{1}{4}$  Maximum size and good lumps)

Lf = 60 (Maximum size and bad lumps)

Lf = 42 ( $\frac{1}{2}$  Maximum size and bad lumps)

Lf = 32 ( $\frac{1}{4}$  Maximum size and bad lumps)

The bulk density factor Df = 0.9, as density is greater than 1000 kg / m<sup>3</sup>

For Lf greater than 25, the feed zone factor Ff = 0.9, for easy feed zone.

For Lf greater than 25, the feed zone factor Ff = 0.8, for difficult feed zone.

The belt speed (mps) values in different situations are as below:

Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 42) \div 100] \times 0.95 \times 0.9 = 0.147$  mps

Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 42) \div 100] \times 0.95 \times 0.8 = 0.131$  mps

$\frac{1}{2}$  Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 32) \div 100] \times 0.95 \times 0.9 = 0.1812$

$\frac{1}{2}$  Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 32) \div 100] \times 0.95 \times 0.8 = 0.1611$

$\frac{1}{4}$  Maximum size, good lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 26) \div 100] \times 0.95 \times 0.9 = 0.202$  mps

$\frac{1}{4}$  Maximum size, good lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 26) \div 100] \times 0.95 \times 0.8 = 0.1793$

Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 60) \div 100] \times 0.95 \times 0.9 = 0.0855$  mps

Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 60) \div 100] \times 0.95 \times 0.8 = 0.076$  mps

$\frac{1}{2}$  Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 42) \div 100] \times 0.95 \times 0.9 = 0.147$  mps

$\frac{1}{2}$  Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 42) \div 100] \times 0.95 \times 0.8 = 0.131$

$\frac{1}{4}$  Maximum size, bad lumps, easy feed,  $v = [0.1 + 0.4 \times (100 - 40 - 32) \div 100] \times 0.95 \times 0.9 = 0.1812$  mps

$\frac{1}{4}$  Maximum size, bad lumps, difficult feed,  $v = [0.1 + 0.4 \times (100 - 40 - 32) \div 100] \times 0.95 \times 0.8 = 0.1611$

The above calculated speeds are to be multiplied by pressure factor and lump numerical dimension factor, if applicable. In general lumps would be “bad”.

## Chapter 6: BELT FEEDER CROSS SECTION FEATURES

This chapter has **34 pages**. Following 7 pages write-up is typical.

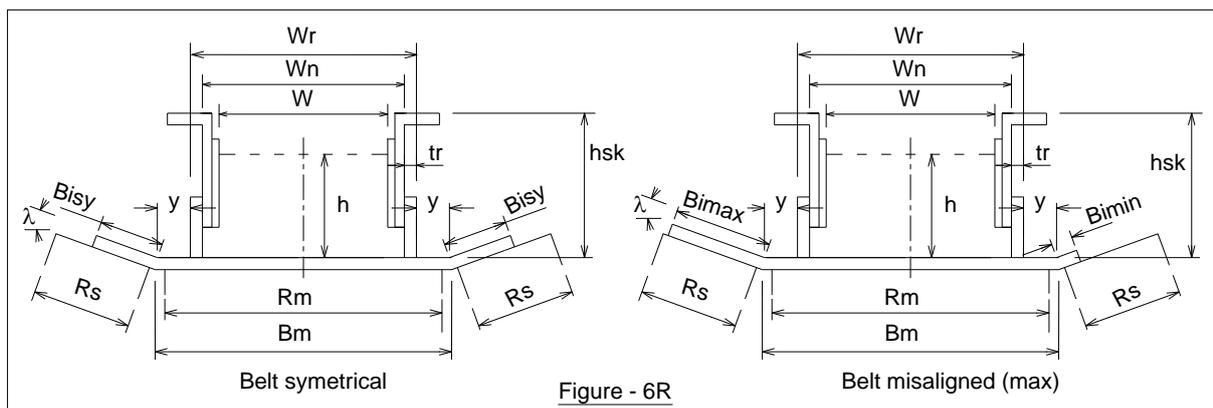
### 6.5.0 BELT FEEDER CROSS SECTION DETAILS (BEYOND FEED ZONE)

This topic establishes the main technical data / features for belt feeders, for cross section in conveying zone i.e. beyond feed zone. Finally, this data have been summarised in table-4, table-5 and table-6. Most of the reasons for this data have been already explained in preceding part of the chapter, and some of the reasons would be clear, as the book progresses.

The conveying zone cross section fundamental parameters viz. material layer width (skirt board width), and height values have been already analysed in foregoing cl. 6.2.0, cl.6.3.0 and 6.4.0. These values become important input for the exercise here.

#### 6.5.1 Picking type belt feeder cross section features (conveying zone)

The cross section of this belt feeder is shown in figure-6R. The aim of this exercise is to decide the values of all dimensions appearing in this figure-6R.



#### Input data :

B: Belt width in mm. This is fixed during belt feeder design.

Lp : Pulley face width in mm. This is as per ISO / DIN in accordance with belt width.

Emin : Minimum edge margin in mm. This is the distance from outside of skirt rubber to belt edge, when belt has maximum allowable misalignment. This value is decided considering functional needs, as explained under cl. 6.2.0. The numerical values of Emin are mentioned in table-4, and are to be used as input for this exercise.

y : The distance between skirt rubber outside to belt bending point (belt kink), theoretical, in mm. This value has been selected as stated in table. The belt will have radial shape at theoretical bending point. This radial shape will have minimum natural dimension, when being pressed by material. It is advisable that skirt rubber should be some what away from this bending point, so that there would not be undue pressure between belt and skirt rubber, when belt is empty. This value depends upon thickness / stiffness of belt, and designer should decide

this value as per need. The values indicated in table are for average condition. More value of  $y$  is better for belt, but it reduces the skirt board width and cross section area. The listed values are compromise of conflicting needs between more room for the belt radius and reduction in cross section.

$t_s$  : skirt plate thickness in mm. This has been mentioned in table for average conditions. The designer can review this as per his choice and its implication on other parameters.

$t_l$  : Thickness of liner on skirt plate in mm. This has been mentioned in table for average conditions. The designer can review this as per his choice and its implication on other parameters.

$t_r$  : Skirt rubber thickness, 16 mm as an average.

$h$  : Material layer height in skirt board, mm (conveying zone), as a factor (ratio) of  $W$ , such as  $0.58 W$ ,  $0.65 W$ ,  $0.71 W$  etc. as decided by designer.

### Output

The aforesaid input data enables to derive following output values in accordance with geometric reasons. Refer figure-6R. Please note that for picking type belt feeder, the roller dimensions are fixed in this exercise to suit their function in belt feeder. The arbitrary dimensional values of picking type idlers should not be mixed up here i.e. values used for picking type conveyor are for different purpose, and need not be valid here.

$$W_n = 2B - L_p - 2 \cdot E_{min} - 2 \cdot t_r = 2B - L_p - 2 \cdot E_{min} - 32 \text{ mm} \quad (\text{as per formula in cl.6.3.1})$$

$$W_r = W_n + 2 \cdot t_r = W_n + 32 \text{ mm}$$

$$W = W_n - 2 \cdot t_s - 2 \cdot t_l \text{ mm}$$

$$B_m = W_r + 2 \cdot y \text{ mm} \quad (B_m \text{ is belt flat portion, theoretical}).$$

$$B_{isy} = (B - B_m) \div 2 \text{ mm} \quad (B_{isy} \text{ is inclined belt width, when belt is symmetrical}).$$

$$B_{imin} = E_{min} - y \text{ mm} \quad (B_{imin} \text{ is inclined belt width, minimum, when belt is misaligned})$$

$$B_{imax} = B - B_m - B_{imin} \text{ mm} \quad (B_{imax} \text{ is inclined belt width, maximum, when belt is misaligned})$$

$$E_{min} = B_{imin} + y \text{ mm} \quad (\text{This is actually input data}).$$

$$E_{max} = B_{imax} + y \text{ mm} \quad (\text{This is maximum edge margin when belt is misaligned})$$

$$E_{sy} = B_{isy} + y \text{ mm} \quad (\text{Belt edge margin when belt is symmetrical on idlers})$$

$$R_m = B_m - 10 \text{ mm} \quad (R_m \text{ is middle roller length and } 10 \text{ mm is gap between rollers, for belt width less than } 2000 \text{ mm})$$

OR

$$R_m = B_m - 15 \text{ mm} \quad (R_m \text{ is middle roller length and } 15 \text{ mm is gap between rollers, for belt width equal to or greater than } 2000 \text{ mm}).$$

$$R_s = B_{imax} - 5 \text{ mm} \quad (R_s \text{ is side roller length and } 5 \text{ mm is half gap between rollers, for belt width less than } 2000 \text{ mm}).$$

OR

$$R_s = B_{imax} - 7.5 \text{ mm} \quad (R_s \text{ is side roller length and } 7.5 \text{ mm is half gap between rollers, for belt width } 2000 \text{ mm and more}).$$

$$h_{sk} = h + 100 \text{ mm or } 1.5 \times h \text{ whichever is more. (For skirt board length within } 1.5 \times W \text{ from exit of feed zone).}$$

$$h_{sk} = h + 100 \text{ mm or } 1.35 \times h \text{ whichever is more. (For skirt board length beyond } 1.5 \times W \text{ from exit of feed zone). If one intends to have uniform height for skirt board, then it would be necessary to adopt preceding norm.}$$

$$A_n = W \cdot h \div (1000 \times 1000) \text{ m}^2 \quad (A_n \text{ is material nominal cross section area})$$

### Example-7

Calculate cross section important features based on following input data, for 2400 mm belt, for conveying zone of picking type belt feeder. Refer figure-6R for nomenclatures. The designer's input are :

$B = 2400\text{mm}$ ,  $L_p = 2700\text{mm}$ ,  $E_{min} = 130\text{ mm}$ ,  $y = 90\text{ mm}$ ,  $t_s = 12\text{ mm}$ ,  $t_l = 18\text{ mm}$ ,  $h = 0.71 W$

#### Solution :

$$W_n = 2B - L_p - 2 \cdot E_{min} - 32\text{ mm} = 2 \times 2400 - 2700 - 2 \times 130 - 32 = 1808\text{ mm}$$

$$W_r = W_n + 2 \cdot t_r = 1808 + 2 \times 16 = 1840\text{ mm}$$

$$W = W_n - 2 \cdot t_s - 2 \cdot t_l = 1808 - 2 \times 12 - 2 \times 18 = 1748\text{ mm}$$

$$B_m = W_r + 2 \cdot y = 1840 + 2 \times 90 = 2020\text{ mm}$$

$$B_{isy} = (B - B_m) \div 2 = (2400 - 2020) \div 2 = 190\text{ mm}$$

$$B_{imin} = E_{min} - y = 130 - 90 = 40\text{ mm}$$

$$B_{imax} = B - B_m - B_{imin} = 2400 - 2020 - 40 = 340\text{ mm}$$

$$E_{min} = B_{imin} + y = 40 + 90 = 130\text{ mm} \text{ (This is just cross check).}$$

$$E_{max} = B_{imax} + y = 340 + 90 = 430\text{ mm}$$

$$E_{sy} = B_{isy} + y = 190 + 90 = 280\text{ mm}$$

$$R_m = B_m - 15 = 2020 - 15 = 2005\text{ mm}$$

$$R_s = B_{imax} - 7.5 = 340 - 7.5 = 332.5\text{ mm}$$

$h_{sk} = h + 100 = 0.71 \times 1748 + 100 = 1341\text{ mm}$  OR  $1.5 \times h = 1.5 \times 1241.08 = 1862\text{ mm}$ . So, the value is 1862 mm. (For skirt board length 1.5 W from exit of feed zone).

$h_{sk} = h + 100 = 0.71 \times 1748 + 100 = 1341\text{ mm}$  OR  $1.35 \times h = 1.35 \times (0.71 \times 1748) = 1676\text{ mm}$ . So, the value is 1676 mm. (For skirt board length beyond 1.5 W from exit of feed zone).

$$A_n = W \cdot h \div (1000 \times 1000) = 1748 \times 0.71 \times 1748 \div (1000 \times 1000) = 2.16941\text{ m}^2$$

In case of DIN standard for 3 equal rollers, the total developed length along rollers =  $900 \times 3 + 15 \times 2 = 2730\text{ mm}$ . This value for picking type idler as per above derivation is  $2005 + 333 + 333 + 15 + 15 = 2701\text{ mm}$ , these are quite close.

As would be observed by the reader, the chosen value of  $y$  is very important, in context of belt bending radial zone at kink. Less thick belt for less difficult material would not be problematic. But strong carcass belt with thick rubber should be given careful thought for its bending behaviour at kink, when empty and loaded. The value of  $y$  should be adopted in conjunction with belt specifications, on case to case basis. The value of  $y$  should be somewhat less than  $E_{min}$ .

#### Picking type belt feeder

For effectiveness or for meaningful purpose of picking type idler,  $y < E_{min}$ , so that some portion of belt width remains on side roller, and it does not become flat belt feeder, in worst situation.

The required value of  $y$  is sensitive to belt. The unusual stiff and thick rubber belt bending in radial zone can require more value of  $y$ . The increase of  $y$  and thereby also the increase of  $E_{min}$  will result into lesser cross section of material layer. The required  $y$  value is also influenced by troughing angle. The shallow troughing angle reduces the problem of belt bending. As against this, more troughing angle helps to prevent spillage of leaked material. The required value of  $y$ , as per belt thickness and stiffness, cannot be ignored. Some time it may make use of this type of belt feeder uneconomical (or may prevent its use).

### **3-roll troughing idler belt feeder**

The table mentions  $\lambda = 12.5^\circ$ . One can use more value of  $\lambda$  say up to  $20^\circ$ , if transition length, belt width etc. permit the same. More value of troughing angle is favorable to prevent spillage of leaked material. The scope for use of this belt feeder for expanding width skirt board is limited, because skirt plate cannot pass across the idler kink. So only small value of width gradient is possible. Other option is to use comparatively smaller middle roller and longer side rollers to have somewhat more gradient on width. Even in such case, the skirt board construction would be complicated because it would be expanding on inclined side rollers.

### **Flat belt feeder**

The flat belt feeder do not have constrains similar to picking type or 3-roller type belt feeder, but it has only one issue of fear for “possible” spillage of leaked material. It is compact and can be constructed exceptionally strong. The short belt feeder will not have chances for spillage of leaked material. One can use larger value of  $E_{min}$ , if need be, to reduce the chances of spillage, to suit application conditions. This belt feeder with more (i.e. sufficient) value of  $E_{min}$  can sometimes be the only and economical choice when application of very heavy class is resulting into very stiff and thick belt and skirt board is also of expanding type. In such case, the other option would be picking type belt feeder with sufficiently narrow skirt board, but with reduced capacity (larger belt width).

### **ALLOWABLE LUMP SIZE**

The allowable maximum lump size is in accordance with following proportion between lump size and skirt board net width, as discussed in chapter-8 cl.8.17.2.

The values mentioned below are for skirt board of constant width. In case of skirt board of tapering width; the value at tail end side could be considered about 10% less than specified value.

Opening width =  $3.40 \times$  (maximum lump size) : for less abrasive material, and hopper (including vertical portion) of limited height.

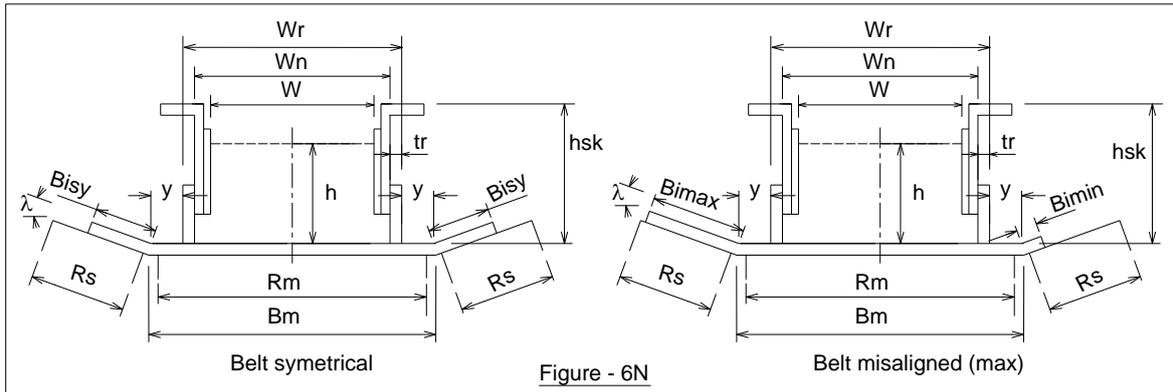
Opening width =  $4.25 \times$  (maximum lump size) : for less abrasive material, and hopper (including vertical portion) of more height.

Opening width =  $4.25 \times$  (maximum lump size) : for highly abrasive material, and hopper (including vertical portion) of limited height.

Opening width =  $5.00 \times$  (maximum lump size) : for highly abrasive material, and hopper (including vertical portion) of large height.

**Table-4 : Picking type belt feeder, skirt board cross section data, beyond hopper outlet.**

All dimensions are in mm. Table mentions brief description of nomenclatures. Refer cl. 6.5.1, for full description of nomenclature and formulae to derive the various values mentioned in this table. The values marked \* are input (i.e. decided / selected by designer). The other values are consequence of the input.



Belt width B *	Pulley face width Lp *	Misaligned belt edge-margins		Skirt rubber to kink point y *	Misaligned belt Incline belt width		Symmetrci belt		Roller length		Thickness		
		Minimum Emin *	Maximum Emax		Bimin	Bimax	Edge margin Esy	Incline belt Bisy	Middle Rm	Sides Rs	Rubber tr *	Skirt plate ts *	Liner tl *
500	600	60	160	45	15	115	110	65	360	110	16	6	8
650	750	60	160	45	15	115	110	65	510	110	16	6	8
800	950	65	215	50	15	165	140	90	610	160	16	6	10
900	1050	70	220	55	15	165	145	90	710	160	16	6	10
1000	1150	75	225	60	15	165	150	90	810	160	16	6	10
1200	1400	85	285	65	20	220	185	120	950	215	16	8	10
1400	1600	90	290	70	20	220	190	120	1150	215	16	8	12
1600	1800	95	295	70	25	225	195	125	1340	220	16	10	12
1800	2000	100	300	75	25	225	200	125	1540	220	16	10	14
2000	2300	120	420	85	35	335	270	185	1620	330	16	10	16
2400	2700	130	430	90	40	340	280	190	2010	335	16	12	18

Belt width B *	Skirt board widths			Skirt plates height hsk (beyond 1.5 W) hsk			Material cross section area m <sup>2</sup>		
	Outside of rubbers Wr	Outside of plates Wn	Inside of liners W	For h=0.58W	For h=0.65W	For h=0.71W	For h=0.58W	For h=0.65W	For h=0.71W
500	280	248	220	228	243	256	0.02807	0.03146	0.03436
650	430	398	370	315	341	363	0.07940	0.08899	0.09720
800	520	488	456	364	400	437	0.12060	0.13516	0.14763
900	610	578	546	428	479	523	0.17291	0.19378	0.21166
1000	700	668	636	498	558	610	0.23461	0.26292	0.28719
1200	830	798	762	597	669	730	0.33677	0.37742	0.41226
1400	1020	988	948	742	832	909	0.52125	0.58416	0.63808
1600	1210	1178	1134	888	995	1087	0.74585	0.83587	0.91303
1800	1400	1368	1320	1034	1158	1265	1.01059	1.13256	1.23710
2000	1460	1428	1376	1077	1207	1319	1.09816	1.23069	1.34430
2400	1840	1808	1748	1369	1534	1675	1.77219	1.98608	2.16941

## Chapter 7: MATERIAL FLOW, HOPPER TO BELT FEEDER

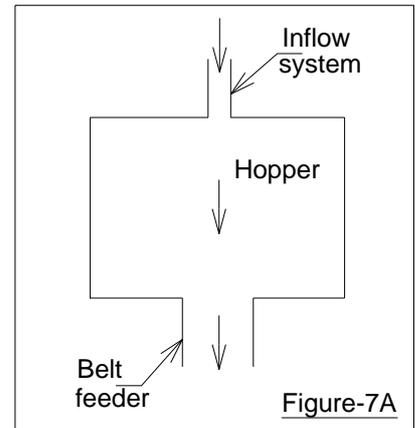
This chapter has **54 pages**. Following 8 pages write-up is typical.

### MATERIAL FLOW FROM HOPPER TO BELT FEEDER

The hopper outlet is flange connected with skirt board. Thus hopper and skirt board forms continuous enclosed space for material. The material at hopper outlet is carried away by belt feeder. Thus, belt feeder is continuously creating cavity in material, at hopper bottom. Hence material in hopper descends down to fill in the cavity being created by belt feeder. This appears as falling level of material in hopper. In a continuously operating system; the material so lost in hopper, is replenished by in-flow system at hopper top. In a continuously operating system the flow would be balanced each time (instant), or with respect to time cycle / interval. Figure-7A depicts schematically the system of in-flow to hopper and out-flow from hopper to belt feeder. In general, the in-flow system will have comparatively very high velocity and hence material cross section of very small value. The hopper material has very large cross section and so very small velocity. The belt feeder speed is very less compared to in-flow system and hence its material cross section is large compared in-flow system. However, in comparison to hopper its flow cross section is quite small and thereby material velocity in belt feeder is quite large compared to velocity in hopper zone. In balanced flow system (i.e. without accumulation / loss):

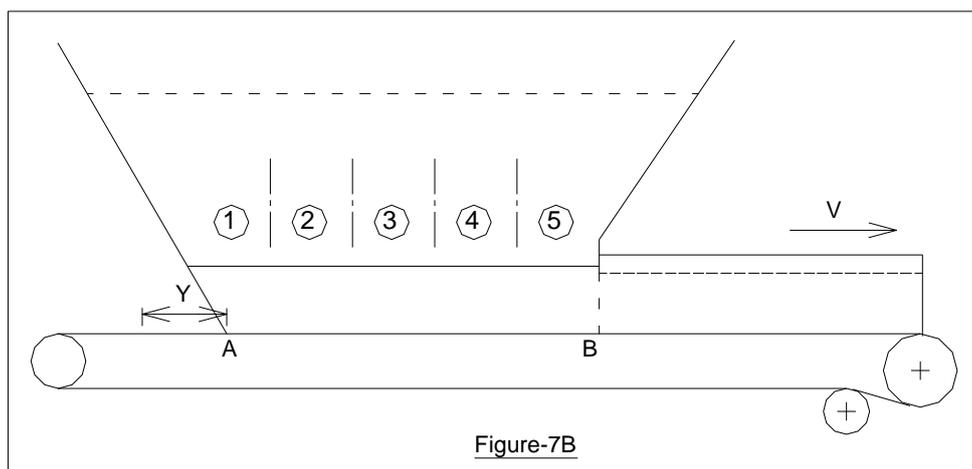
(In-flow system material cross section) x (its velocity) = (Hopper material cross section) x (material velocity in hopper) = (belt feeder material cross section) x (belt velocity) = (Hopper outlet area) x (Average velocity of material across outlet).

The foregoing description provides general information about flow velocity, right from in-flow system to belt feeder. This also considers as if bulk density is constant.



### BASIC CONDITION FOR FAIRLY UNIFORM FLOW AT HOPPER OUTLET

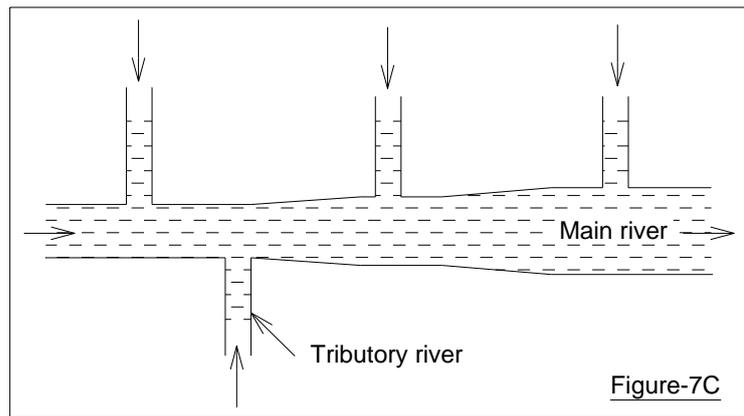
The figure-7B shows hopper and belt feeder schematic arrangement. Consider that hopper outlet is divided into 5 equal compartments by imaginary line. The belt segment of Y length (equal to compartment length) is to pick-



up say 5 tonnes of material from hopper during its travel from A to B. Now bulk material under gravity thrust create potential for each compartment to put full load of 5 tonne on belt section Y when it comes beneath, i.e. gravity force will just flood in material without keeping room for next compartment. So, the belt feeder arrangement needs to be such that when segment Y comes below compartment -1, it will just take / accept ideally 1 tonne of material in spite of material push. When section-Y reaches to compartment-2, it should take 1 more tonne i.e. here load capacity should be totally 2 tonnes. Likewise at 3<sup>rd</sup> compartment, the section-Y capacity should increase to 3 tonne so that although it is already carrying 2 tonnes, it will take 1 tonne from 3<sup>rd</sup> compartment. Ultimately, at 5<sup>th</sup> compartment it will take 1 more tonne with load carrying capacity of 5 tonne.

**Thus, for uniform draw out from hopper outlet, the basic condition is that feeder capacity to draw material from hopper should increase progressively from inlet end to exit end.**

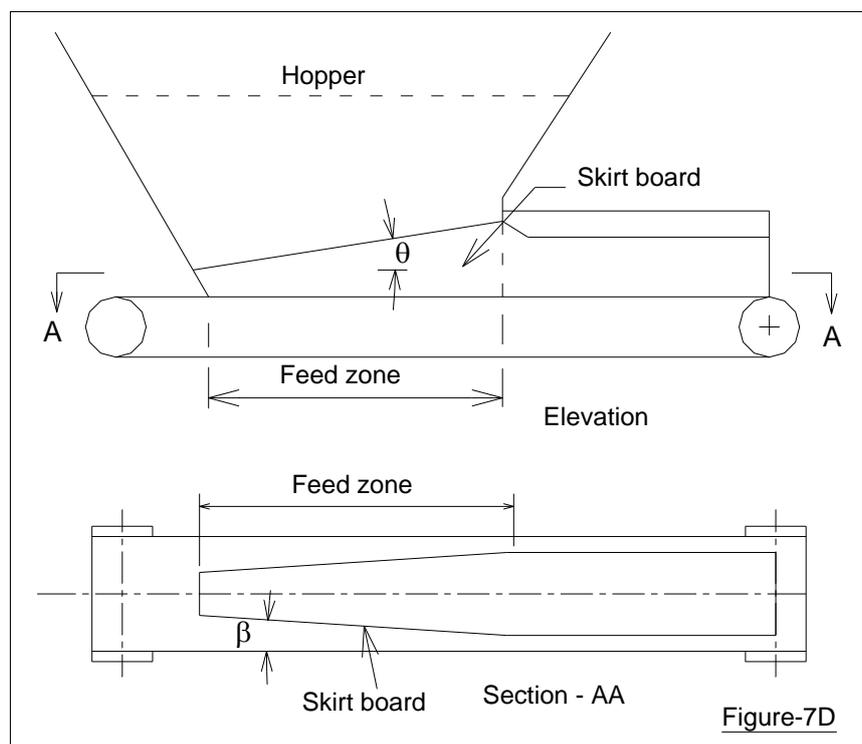
The common and similar (but not identical) example is river, where the river widens in direction of flow so that it can accept water from downstream area (figure-7C).



In a screw feeder this requirement of uniform draw out is achieved by progressively increasing the screw diameter, pitch, etc. For the belt feeder, this condition is fulfilled by gradually increasing the flow cross section, from inlet end to outlet end, so that all zones at hopper outlet get fairly equal opportunity to add material into belt feeder flow.

The other consideration is that the gradual enlargement of cross section, reduces the interference / conflict within body of material and thereby improves belt feeder performance and life.

The belt feeder flow cross section can be increased by increasing the skirt board width (alone) or by increasing height alone or by both. However, to maintain proper flow in bottom part of hopper, it is not possible to increase width and height in isolation.





feeder flow rates across vertical planes at entry point and exit point of this portion. The difference between these two flow rates of belt feeder, is the material flow rate across horizontal plane from hopper into belt feeder, in this portion.

For the first compartment, no material is entering from tail end side i.e. in-flow at EoEo is zero. Hence for first compartment, the belt feeder flow rate at E1E1 is also the input in to belt feeder from compartment-1.

Flow rate across interface, into compartment-1 = Flow rate across E1E1 - zero = Flow across E1E1

Flow rate across interface, into compartment-2 = Flow rate across E2E2 - Flow rate across E1E1

Flow rate across interface, into compartment-3 = Flow rate across E3E3 - Flow rate across E2E2

Flow rate across interface, into compartment-4 = Flow rate across E4E4 - Flow rate across E3E3

Flow rate across interface, into compartment-5 = Flow rate across E5E5 - Flow rate across E4E4

Total inflow in 5 compartments of belt feeder = sum of above

Using the equation for flow at E1E1, E2E2, E3E3, E4E4 and E5E5, the flow into belt feeder from interface of each imaginary compartment, can be derived as mentioned above.

### Example-2

Calculate flow pattern from hopper outlet to belt feeder (i.e. across interface); for following data for 1600mm flat belt feeder, having material shear at interface.

$W_e = 1.124$  m,  $W_i = 0.563$  m,  $h_e = 0.89$  m,  $W_e = 1.0$  m

$H_i = 0.23$  m,  $L = 5.5$  m,  $V = 0.3$  mps,  $K = 0.555$

Also calculate the flow magnitudes for feed zone portion on left side of center line, and for feed zone portion on right side of center line. The left side is towards rear end and right side is towards head end.

### Solution

The calculations are considering 5 compartments of feed zone length.

$$G_e = (h_e - h_i) \div L = (1.0 - 0.23) \div 5.5 = 0.14$$

$$G_p = (W_e - W_i) \div 2 \cdot L = (1.124 - 0.563) \div (2 \times 5.5) = 0.051$$

$$L_z = h_e \div G_e = 1.0 \div 0.14 = 7.142857143$$

$$\therefore 2 \cdot L_z = 14.28571429$$

Flow rate across section E1E1

$$= (h_e - 0.8 \cdot L \cdot G_e) \cdot (W_e - 1.6 \cdot L \cdot G_p) [L_z \cdot (1 + K) + 0.8 \cdot L \cdot (1 - K)] \cdot V \div 2 \cdot L_z$$

$$= (1.0 - 0.8 \times 5.5 \times 0.14) \cdot (1.124 - 1.6 \times 5.5 \times 0.051) [7.142857143 \times (1 + 0.555) + 0.8 \times 5.5 \times (1 - 0.555)] \times 0.3 \div 14.28571429$$

$$= 0.071137257 \text{ m}^3/\text{sec}$$

$$= 256.1 \text{ m}^3/\text{hr}$$

Flow rate across section E2E2

$$= (1.0 - 0.6 \times 5.5 \times 0.14) \times (1.124 - 1.2 \times 5.5 \times 0.051) \times [7.142857 \times (1.555) + 0.6 \times 5.5 \times (0.445)] \times 0.3 \div 14.285714$$

$$= 0.1118735 \text{ m}^3/\text{sec}$$

$$= 402.74 \text{ m}^3/\text{hr}$$

Flow rate across section E3E3

$$\begin{aligned}
&= (1.0 - 0.4 \times 5.5 \times 0.14) \times (1.124 - 0.8 \times 5.5 \times 0.051) \times [7.142857 \times (1.555) + 0.4 \times 5.5 \times (0.445)] \times 0.3 \div \\
&14.285714 \\
&= 0.158002 \text{ m}^3/\text{sec} \\
&= 568.8 \text{ m}^3/\text{hr}
\end{aligned}$$

Flow across section E4E4

$$\begin{aligned}
&= (1.0 - 0.2 \times 5.5 \times 0.14) \times (1.124 - 0.4 \times 5.5 \times 0.051) \times [7.142857 \times (1.555) + 0.2 \times 5.5 \times (0.445)] \times 0.3 \div \\
&14.285714 \\
&= 0.208457 \text{ m}^3/\text{sec} \\
&= 750.44 \text{ m}^3/\text{hr}
\end{aligned}$$

Flow across section E5E5

$$\begin{aligned}
&= h_e \cdot W_e \cdot (1 + K) \cdot V \div 2 \\
&= 1.0 \times 1.124 \times (1 + 0.555) \times 0.3 \div 2 \\
&= 0.262173 \text{ m}^3/\text{sec} \\
&= 943.8228 \text{ m}^3/\text{hr}
\end{aligned}$$

Using the above values of flow across E1E1, E2E2, E3E3, E4E4 and E5E5, the flow into compartment-1, compartment-2, compartment-3, compartment-4 and compartment-5, counting from rear end is as below :

$$\text{Flow into compartment-1 of belt feeder} = \text{Flow across E1E1} - \text{zero} = 256.1 \text{ m}^3/\text{hr}$$

$$\text{Flow into compartment-2 of belt feeder} = \text{Flow across E2E2} - \text{Flow across E1E1} = 402.74 - 256.1 = 146.64 \text{ m}^3/\text{hr}$$

$$\text{Flow into compartment-3 of belt feeder} = \text{Flow across E3E3} - \text{Flow across E2E2} = 568.8 - 402.74 = 166.06 \text{ m}^3/\text{hr}$$

$$\text{Flow into compartment-4 of belt feeder} = \text{Flow across E4E4} - \text{Flow across E3E3} = 750.44 - 568.8 = 181.64 \text{ m}^3/\text{hr}$$

$$\text{Flow into compartment-5 of belt feeder} = \text{Flow across E5E5} - \text{Flow across E4E4} = 943.82 - 750.44 = 193.38 \text{ m}^3/\text{hr}$$

$$\text{Total inflow in 5 compartments of belt feeder} = \text{sum of above} = 943.82 \text{ m}^3/\text{hr}$$

The total inflow from all 5 compartments matches to the flow rate across E5E5, which is finally outflow at exit end.

The inflow values in individual sections are 256.1, 146.64, 166.06, 181.64 and 193.38 m<sup>3</sup>/hr. It is not possible to make these values identical, because it would need differing values of  $\theta$  and  $\beta$  for each section. This is not practical from construction and other reasons, and exact matching is also not necessary.

Now, calculations are to be done for flow magnitude for feed zone portion, which is on tail side of center line, and flow magnitude for feed zone portion, which is on head side of center line. Here, center line means center line of feed zone. This can be done using data for each compartment as below. The flow on tail side (i.e. center line to rear side) is  $\Sigma ZT$ . The flow on head side (i.e. center line to forward side) is  $\Sigma ZH$ .

$$\begin{aligned}
\Sigma ZT &= (\text{compartment-1}) + (\text{compartment-2}) + (\text{half of compartment-3}) \\
&= 256.1 + 146.64 + 0.5 \times 166.06 \\
&= 485.77 \text{ m}^3/\text{hr} \text{ (This is 51.47\% of total).}
\end{aligned}$$

$$\begin{aligned}
\Sigma ZH &= (\text{half of compartment-3}) + (\text{compartment-4}) + (\text{compartment-5}) \\
&= 0.5 \times 166.06 + 181.64 + 193.38
\end{aligned}$$

= 458.05 m<sup>3</sup>/hr (This is 48.53% of total).

Total  $\Sigma ZT + \Sigma ZH = 485.77 + 458.05 = 943.82$  m<sup>3</sup>/hr

This result can be said as an excellent matching of flow, on both sides of center line of feed zone.

In this example,  $G_e = 0.14$  i.e.  $\theta = 7.96961^\circ$ , and  $G_p = 0.051$  i.e.  $\beta = 2.919555^\circ$ . The reader to note that the values of  $\theta$  and  $\beta$  will be in large digits and unusual figures, because they are derivations of pre-decided dimensions. Referring to chapter-8, cl.8.14.5, the hopper outlet adapter wall angle would be  $20.016^\circ$  from vertical (i.e.  $70^\circ$  to horizontal), according to these values of  $G_e$  and  $G_p$  and formula given in the said clause.

As would be seen from this numerical example, it is not possible to have exactly equal flow from each compartment. The exactly equal flow will need differing values of  $\beta$  or  $\theta$  or both, for each compartment. This is not practical from feeder construction point of view. So, the designer is to see that at least there is reasonable balance of in-flow into feeder, for first half of feed zone and second half of feed zone.

Some imbalance between them is not directly harmful to belt feeder but would result in to imbalance in hopper emptying process, and material top face would be at lower level where there is greater flow at underneath outlet portion. The material top face would be at higher level where the flow is less at underneath outlet portion. This implies that material in hopper is not descending vertically down, but it is also simultaneously shifting horizontally at a very slow rate, towards the outlet section, which is emptying fast. Such imbalance is more of concern for tall hoppers (bin / silo / bunker), if the same results into undesirable flow pattern in hopper. In general, lesser value of  $\theta$  and  $\beta$  would tend to increase flow in the rear zone. The more value of  $\theta$  and  $\beta$  i.e. higher values of taper (rapidly expanding cross section) will tend to put more material into forward zone. This statement will help the designer in manipulating the values of  $\theta$  and  $\beta$  to achieve approximate balance of flow.

### **Ready to use tables**

The book includes ready to use flow balancing tables (17 pages). These tables enables designer to select the skir-board expansion features close to requirement, and thereby the subsequent design work becomes easy and quick.

**Enclosed two pages show the typical tables.**

**$\Sigma ZT\%$  : Percentage of flow at interface, for feed zone half length, toward tail side.**

Analysis basis: Flat belt feeder. The values are fairly applicable to picking type and 3-equal roll belt feeders. The values are % of total flow, for feed zone half length from tail side to feed zone center line.

The values are  $\Sigma ZH\% = 100 - \Sigma ZT\%$ . L is feed zone length (not feeder length).

Wi minimum = 0.25 We. hi minimum = 0.15 m.

**The indicated values are  $\Sigma ZT\%$**

Belt : 1200 mm L : 4.80 m K = 0.5625					
We : 0.762 m he = 0.875 x We = 0.667 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.8517	1.7034	2.5552	3.4069
		619 mm	477 mm	334 mm	190 mm
1.4926	542	84.29	75.58	66.86	58.13
2.9852	417	77.50	69.49	61.47	53.44
4.4779	291	70.23	62.97	55.71	48.43
5.9705	165	62.48	56.03	49.56	43.09

Belt : 1200 mm L : 6.50 m K = 0.5625					
We : 0.762 m he = 0.875 x We = 0.667 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.6293	1.2586	1.8879	2.5172
		619 mm	476 mm	333 mm	190 mm
1.1041	542	84.28	75.56	66.85	58.12
2.2081	416	77.48	69.46	61.45	53.43
3.3122	291	70.21	62.95	55.69	48.42
4.4162	165	62.48	56.02	49.56	43.09

Belt : 1200 mm L : 1.50 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.6964	5.3928	8.0892	10.7856
		621 mm	479 mm	336 mm	191 mm
5.4256	620	84.81	76.11	67.32	58.42
10.8513	474	78.24	70.21	62.11	53.90
16.2769	324	70.85	63.58	56.24	48.81
21.7026	165	62.39	55.99	49.53	42.98

Belt : 1200 mm L : 2.00 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.0328	4.0656	6.0983	8.1311
		620 mm	478 mm	335 mm	191 mm
4.1551	617	84.65	75.93	67.17	58.34
8.3102	470	77.98	69.95	61.88	53.75
12.4653	320	70.60	63.33	56.02	48.66
16.6204	165	62.36	55.94	49.49	42.98

Belt : 1200 mm L : 2.70 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		1.5103	3.0207	4.5310	6.0413
		620 mm	477 mm	334 mm	191 mm
3.1170	615	84.55	75.82	67.07	58.29
6.2341	467	77.83	69.80	61.74	53.66
9.3511	317	70.45	63.18	55.89	48.57
12.4681	165	62.34	55.91	49.46	42.98

Belt : 1200 mm L : 3.60 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		1.1346	2.2692	3.4038	4.5383
		619 mm	477 mm	334 mm	191 mm
2.3540	614	84.49	75.76	67.02	58.26
4.7079	466	77.74	69.71	61.67	53.61
7.0619	316	70.37	63.10	55.82	48.52
9.4159	165	62.33	55.90	49.45	42.98

Belt : 1200 mm L : 4.80 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.8517	1.7034	2.5552	3.4069
		619 mm	477 mm	334 mm	190 mm
1.7724	613	84.46	75.73	66.99	58.24
3.5449	465	77.70	69.66	61.63	53.58
5.3173	315	70.33	63.06	55.78	48.50
7.0898	165	62.33	55.89	49.44	42.98

Belt : 1200 mm L : 6.50 m K = 0.5					
We : 0.762 m he = We = 0.762 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.6293	1.2586	1.8879	2.5172
		619 mm	476 mm	333 mm	190 mm
1.3119	613	84.44	75.71	66.97	58.23
2.6238	464	77.67	69.64	61.60	53.56
3.9358	315	70.30	63.03	55.76	48.48
5.2477	165	62.33	55.88	49.43	42.98

**$\Sigma ZT\%$  : Percentage of flow at interface, for feed zone half length, toward tail side.**

Analysis basis: Flat belt feeder. The values are fairly applicable to picking type and 3-equal roll belt feeders. The values are % of total flow, for feed zone half length from tail side to feed zone center line.

The values are  $\Sigma ZH\% = 100 - \Sigma ZT\%$ . L is feed zone length (not feeder length).

Wi minimum = 0.25 We. hi minimum = 0.15 m.

**The indicated values are  $\Sigma ZT\%$**

Belt : 1400 mm L : 1.80 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.7643	5.5286	8.2929	11.0572
		764 mm	590 mm	413 mm	235 mm
5.0060	663	84.23	75.59	66.86	58.02
10.0120	503	77.14	69.23	61.24	53.14
15.0180	338	69.32	62.21	55.03	47.75
20.0240	165	60.58	54.36	48.09	41.73

Belt : 1400 mm L : 2.40 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.0845	4.1690	6.2535	8.3380
		763 mm	588 mm	412 mm	235 mm
3.8219	661	84.07	75.41	66.71	57.94
7.6437	499	76.90	68.98	61.02	53.00
11.4656	334	69.10	61.98	54.83	47.62
15.2874	165	60.55	54.31	48.05	41.73

Belt : 1400 mm L : 3.10 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		1.6184	3.2368	4.8552	6.4735
		763 mm	587 mm	411 mm	235 mm
2.9871	659	83.99	75.32	66.63	57.90
5.9741	497	76.77	68.85	60.91	52.93
8.9612	332	68.98	61.86	54.72	47.55
11.9483	165	60.53	54.29	48.02	41.73

Belt : 1400 mm L : 4.00 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		1.2564	2.5128	3.7691	5.0255
		763 mm	587 mm	411 mm	235 mm
2.3284	658	83.93	75.27	66.58	57.87
4.6568	495	76.70	68.78	60.84	52.88
6.9852	331	68.91	61.79	54.66	47.51
9.3136	165	60.52	54.27	48.01	41.73

Belt : 1400 mm L : 5.50 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.9148	1.8297	2.7445	3.6593
		762 mm	587 mm	411 mm	235 mm
1.7004	658	83.90	75.23	66.55	57.85
3.4008	494	76.64	68.72	60.79	52.85
5.1013	330	68.85	61.74	54.61	47.48
6.8017	165	60.51	54.26	48.00	41.73

Belt : 1400 mm L : 7.50 m K = 0.5625					
We : 0.938 m he = 0.875 x We = 0.821 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		0.6713	1.3426	2.0139	2.6852
		762 mm	586 mm	411 mm	235 mm
1.2497	657	83.88	75.20	66.53	57.84
2.4994	494	76.61	68.69	60.76	52.83
3.7491	330	68.83	61.71	54.59	47.46
4.9987	165	60.51	54.25	47.99	41.73

Belt : 1400 mm L : 1.80 m K = 0.5					
We : 0.938 m he = We = 0.938 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.7643	5.5286	8.2929	11.0572
		764 mm	590 mm	413 mm	235 mm
5.8102	755	84.54	75.87	67.11	58.23
11.6204	568	77.62	69.66	61.62	53.47
17.4306	373	69.77	62.61	55.38	48.06
23.2408	165	60.67	54.45	48.17	41.79

Belt : 1400 mm L : 2.40 m K = 0.5					
We : 0.938 m he = We = 0.938 m					
$\theta$ degrees	hi mm	$\beta$ degrees and Wi mm			
		2.0845	4.1690	6.2535	8.3380
		763 mm	588 mm	412 mm	235 mm
4.4632	751	84.35	75.66	66.93	58.13
8.9264	561	77.32	69.36	61.35	53.29
13.3897	367	69.47	62.32	55.13	47.88
17.8529	165	60.64	54.40	48.12	41.79

## Chapter 8: MATERIAL PRESSURES / FORCES IN HOPPER (I.E. HOPPER BIN, SILO AND BUNKER)

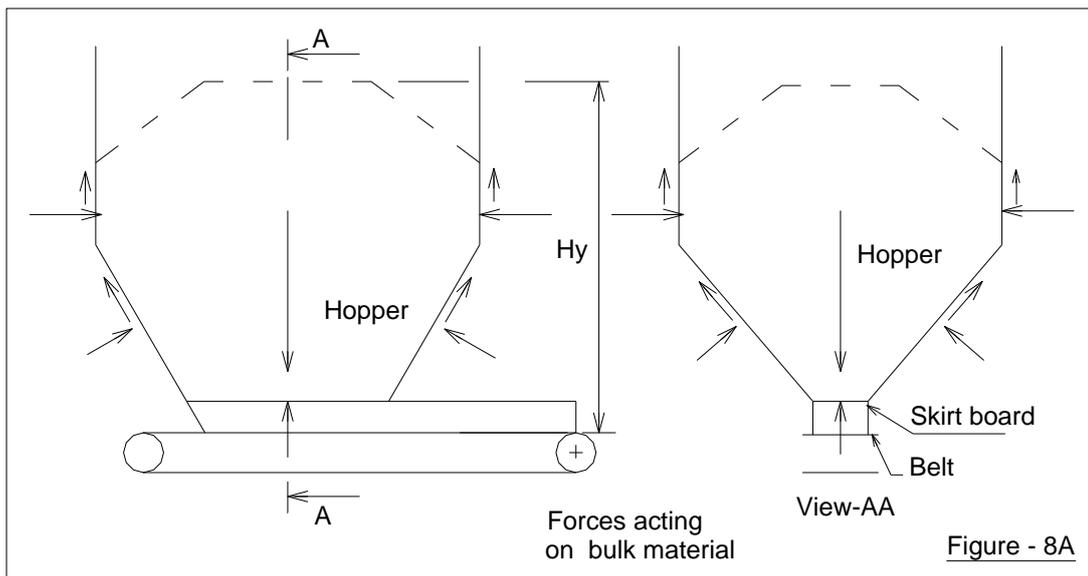
This chapter has **98 pages**. Following 23 pages write-up is typical.

### MATERIAL PRESSURES / FORCES IN HOPPER (I.E. HOPPER, BIN, SILO AND BUNKER)

The bulk material in hopper will try to flow out at bottom opening, unless prevented by barrier. The belt feeder is located directly below the hopper outlet. Thus belt feeder acts as a barrier to material's uncontrolled flow out (drain out) at bottom opening. In other words, belt feeder supports the material at hopper outlet. Therefore, the belt feeder will be subjected to material pressure / force which is prevailing across its outlet. The material pressure / force across outlet has prominent effect on belt feeder design and construction. This chapter discusses the calculation of material pressure / forces at interface of hopper and belt feeder, and then converts into a convenient model, for use in belt feeder design. The pressure / force value across hopper outlet, as calculated in this chapter, becomes an important input to belt feeder design.

### GENERAL

Figure-8A shows hopper and belt feeder arrangement. The hopper is filled with bulk material and there is also in-flow of bulk material at top opening of hopper. Simultaneously, the belt feeder draws out the material from hopper outlet at bottom. In a continuously operating plant, the system would be in a balanced state with respect



to in-flow and out-flow. The hopper remains filled with the material, but it will have a fluctuation in its level, depending upon filling and outflow patterns or their cyclic variation.

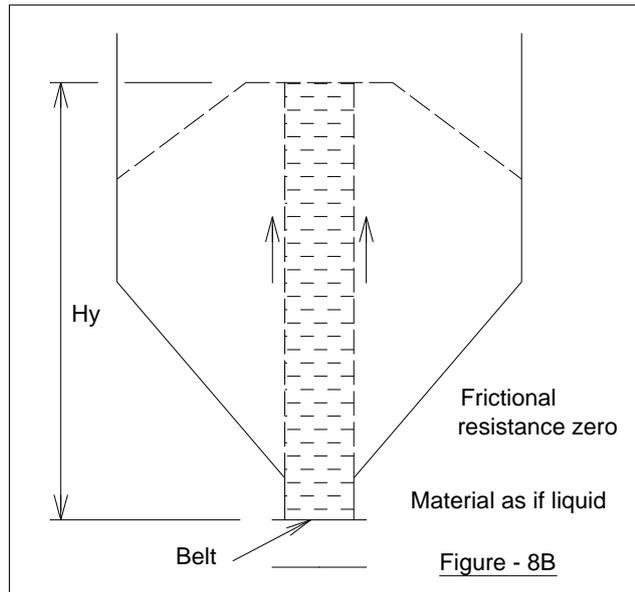
The bulk material in hopper is subjected to downward gravity force. It is slowly moving down at steady speed but not accelerating (i.e. speed is not getting increased continuously, which is not occurring in installation). So, bulk material in hopper is under balanced state of forces. The downward acting gravity force on material is balanced by following forces as shown in figure 8A:

- Hopper vertical walls frictional resistance to material downward motion. The gravity force results into side spread of material and thereby frictional grip on hopper walls.
- Hopper bottom walls normal reaction (i.e. perpendicular to walls).

- Hopper bottom walls frictional resistance acting against material downward motion.
- The belt feeder vertical reaction.

The vertical components of all the forces adds to zero (vector sum), because, material is in a state of balance i.e. gravity downward force is balanced by upward components of all the earlier mentioned forces (frictions and reactions).

The next issue is the magnitude of material weight portion, which is pressing on belt feeder. Referring to figure-8B, if it would have been liquid, the pressure at belt level would have been just  $\gamma \cdot g \cdot H_y$  and the force would be this pressure multiplied by liquid (material) support area of belt feeder. This is so, because liquid repose angle is zero and it does not offer shear resistance (in context of



negligible slide velocity applicable to this case). The material column  $H_y$  is not subjected to any shear / frictional resistance by material (liquid) surrounding this column, and hence pressure according to its full height  $H_y$  acts at bottom. In case of material, the downward motion (tendency of motion), relative to surrounding material, is opposed by the shear / frictional resistance of material surrounding this column. So the pressure value at bottom is less compared to the liquid.

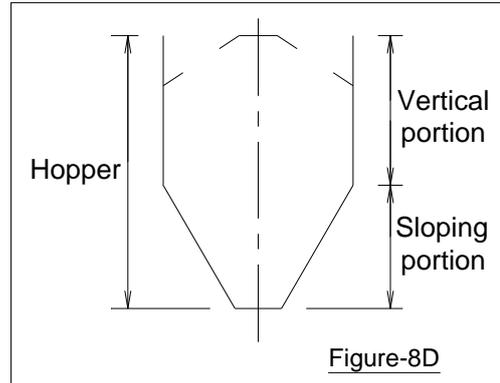
Thus it is evident that the entire weight of material column from bottom to top, is not resting on belt feeder. In fact, the major portion of this material column weight, when it tries to move down, is getting transferred to surrounding material. Hence in this very simplistic analysis, the pressure (weight force) at hopper outlet would be quite less compared to weight of full column.

The issue of less pressure (force) at hopper outlet, can also be understood by simplistic approach to arching characteristic of material. As everyone knows from day to day experience, the bulk material has arching characteristic / ability. In view of this, when material is removed from a portion close to the bottom support, the entire material does not fall down or flow out like liquid, but tends to form cave due to arching.

This book and chapter is concerned with the material pressure across hopper outlet, which imposes forces on belt feeder. Now, pressure across hopper outlet depends upon pressure values in hopper at various points. In fact, outlet pressure is consequence of pressure values from material top face to bottom outlet. Therefore, the chapter does provide the basic information to enable the calculation of pressure at relevant points in hopper. However, it is not necessary to entail the hopper elaborate design entire procedure onto belt feeder design. Hence, this chapter presents calculation procedure for the material forces across hopper outlet, in a manner relevant to belt feeder, avoiding material testing etc. required for more exact results. This is befitting to the need of belt feeder. The literature on hopper (bin / bunker / silo) design generally concerns with hopper (silo / bin) of great height. But more number of belt feeders are used for installations where hopper height is quite less, and this aspect needs to be given due importance while formulating general approach to belt feeder design, so that unnecessary complexities are not imposed, where not warranted.

## TECHNICAL UNDERSTANDING OF PRESSURE VALUES

The material pressure values have differing basis / reasons for vertical upper portion and bottom converging portion. Therefore, these sections have different formulae for pressure values, as described in this chapter. Again these pressure values are different when material is flowing out at bottom outlet; and when material is not flowing out at bottom outlet. The pressure situation in hopper has been named as dynamic pressures, when the material is flowing out at bottom outlet (this is often called as emptying pressures). The pressure situation in hopper has been named as static pressures, when the material is not flowing out at bottom outlet (this can best be said as no-emptying pressures).



But non-emptying is not convenient and hence, the word static has been chosen. Now, as the static word has been chosen for this case, the first case is named as dynamic pressure).

The dynamic (emptying) pressure values are comparatively more definite as compared to static (non-emptying) pressure values, at outlet. In fact, both values are reasonably predicted values for engineering requirements. The static (i.e. non-emptying) pressure values signify the maximum values during usual situation. For example in tall hopper, if material remains static for short duration, then it will have pressure values close to dynamic situation. It can reach the calculated static pressure values for standstill condition of routine nature. Possibly, it may not cover dead static situation of abnormal nature. The issue is subjective, and cannot be quantified in terms of time, as a general rule. However, it appears that the same would depend upon daily temperature variation and compressibility of particular bulk material.

The filling of material in hopper can occur simultaneous to emptying, or may not occur simultaneously. The dynamic (emptying) pressure are the same irrespective of filling or not filling, provided the hopper is of sufficient height. The filling of material in tall hopper is to be always done above intersection level (i.e. hopper should not be emptied below this level). The filling of material in such hopper, when there is no on-going emptying, will 'possibly' bring static pressure values close to calculated pressure values, somewhat quicker. The statement is for hopper of sufficient height.

Now, as regards converging portion of hopper, the pressure values also depend upon geometric shape of hopper. Therefore, this chapter includes topics for pressure calculation, for **belt feeder** needs, for following situations (total of all cases for vertical portion and bottom converging portion).

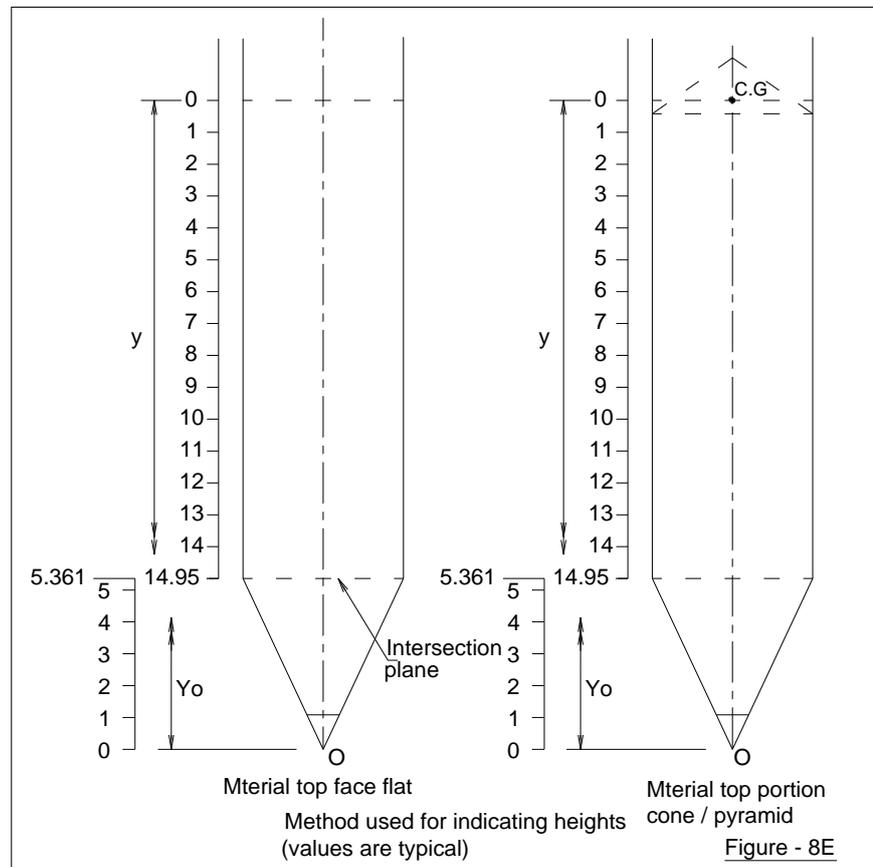
- The pressure values for vertical portion. Refer cl. 8.5.0 These values are adequate for dynamic as well as static situation, in context of belt feeder interface.
- The pressure values for horizontal bottom silo, (i.e. hopper converging portion nearly horizontal, say sides up to  $10^\circ$  incline to horizontal), static situation. Refer cl. 8.8.1.
- The pressure values for horizontal bottom silo, (i.e. hopper converging portion nearly horizontal, say sides up to  $10^\circ$  incline to horizontal), dynamic situation. Refer cl. 8.8.2.
- Pressure values for steep converging portion of hopper, dynamic (emptying) situation. Refer cl. 8.9.1.

- Pressure values for steep converging portion of hopper, static (non-emptying) situation. Refer cl. 8.9.2.
- Pressure values for less-steep converging portion of hopper, static (non-emptying) situation. Refer cl. 8.10.1
- Pressure values for less-steep converging portion of hopper, dynamic (emptying) situation. Refer cl. 8.10.2

The hopper (bin) design literature is concerned with vertical pressure in material, but **more prominently to pressure values on hopper wall**. As against this, the book subject belt feeder is only concerned with **vertical pressure in material, particularly across outlet**. However, the formulae for pressure on wall have been also mentioned in most of the cases as useful 'side information'.

### METHOD FOR DEPICTING HEIGHT

The bulk material feeding in hopper will create inclined top faces most of the time. It will rarely have the flat top face. However, in this chapter, the top face in all figures has been shown flat for convenience. Whenever the top face is not flat, its reference point at top is the CG of the top portion of the bulk material, as depicted in figure-8E (right hand side). That means depth measurement from top level will be from flat face or from CG of the top portion. This depth value to be used in various formulae, as applicable.



In case of bottom converging portion, various formulae require height measurement from the apex point at the bottom. Hence, in this case the measurement, would be the height from apex, as shown in figure-8E.

### MATERIAL PRESSURE IN VERTICAL PORTION OF HOPPER (i.e. BIN / SILO)

This formula is mainly known as Janssen formula (1895). It provides pressure values in vertical portion of hopper. The main considerations in this formula are :

- The vertical gravity force acting on each element of bulk material, create vertical pressure in body of bulk material.

- The vertical pressure creates side pressure (horizontal pressure) due to spreading tendency of bulk material. This side pressure acts on hopper wall; creating friction grip between hopper wall and bulk material
- The compression or settling or downward motion of bulk material results into situation, whereby upper portion of bulk material is not able bear fully on lower portion of bulk material. The effect is that the pressure values increase at diminishing rate, as the depth increases.

Figure-8F shows the material in vertical portion of hopper. Consider a material slice of thickness  $dy$  at depth  $y$  from top face. The nomenclature in figure-8F implies following quantities :

$y$  : Depth from top, at the point of analysis, m  
 $\phi$  : Material usual repose angle, degree  
 $K$  : Ratio of horizontal and vertical pressure. Here average value,  $K = (1 - \sin 0.9\phi)$ . Use tested value when necessary.

$P_v$  : Vertical pressure in bulk material at depth  $y$ . This acts downwards on upper face of slice,  $N/m^2$

$P_v + dP_v$  : Vertical pressure in bulk material at depth  $y + dy$ . This acts upward on lower face of slice,  $N/m^2$

$A$  : Cross section area of slice i.e. cross section area of hopper (bin). This is uniform for vertical portion. Janssen formula and this derivation is applicable to vertical portion only,  $m^2$

$P_n$  : Horizontal pressure in bulk material, at depth  $y$ .  
 The hopper (bin) wall applies same pressure on slice, as shown in figure-8F. This is considered as  $P_n$  along slice thickness instead of average of  $P_n$  and  $P_n + dP_n$ . The reason for this is mathematical and is not the subject here, (like multiplication among increments, etc)  $N/m^2$

$\mu_s$  : Friction coefficient between hopper wall and slice.

$C_r$  : Circumference of slice edge, m

$R$  :  $A \div C_r$ , which is known as 'hydraulic' radius, m

$\gamma$  : Bulk density,  $kg/m^3$ . The formula considers this of uniform value, with respect to depth.

The slice is about to slide down (settle down), but is stable in vertical direction (i.e. it is not accelerating in vertical direction). The 'about to slide down' situation arises due to compressible nature of underneath material. During hopper discharge, this slice actually moves downward at slow speed, whereby it is also stable during hopper emptying. Thus, this formula is applicable to bulk material in hopper, during no out-flow as well as during out-flow situation (i.e. static and dynamic situation as applicable to installation in running plant).

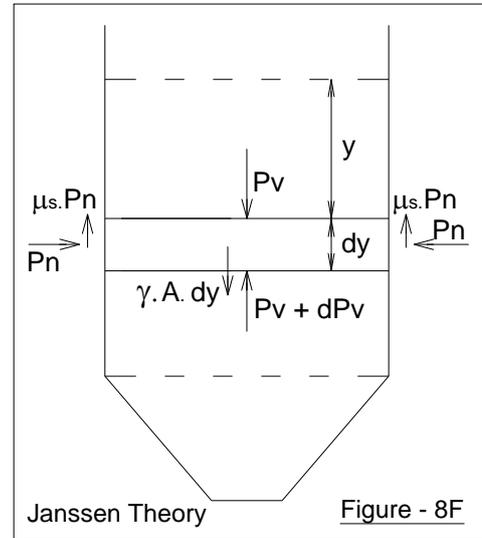
Now, as the slice is stable in vertical direction; the opposing forces in vertical direction are equal. This provides following equation.

$$P_v \cdot A + A \cdot dy \cdot \gamma \cdot g = (P_v + dP_v) \cdot A + \mu_s \cdot C_r \cdot dy \cdot P_n$$

But,  $P_n = K \cdot P_v$ , where  $K$  is factor for horizontal pressure

$$\therefore A \cdot P_v + A \cdot \gamma \cdot g \cdot dy = A \cdot (P_v + dP_v) + \mu_s \cdot C_r \cdot K \cdot P_v \cdot dy$$

The mathematical solution of this equation gives following formula for vertical pressure  $P_v$  and horizontal pressure  $P_n$ , at depth  $y$  from top.



$$P_v = \frac{\gamma \cdot g \cdot R}{\mu_s \cdot K} \cdot \left[ 1 - \frac{1}{e^{\frac{\mu_s \cdot K \cdot y}{R}}} \right] \quad \text{N/m}^2$$

$$P_n = K \cdot P_v = \frac{\gamma \cdot g \cdot R}{\mu_s} \cdot \left[ 1 - \frac{1}{e^{\frac{\mu_s \cdot K \cdot y}{R}}} \right] \quad \text{N/m}^2$$

The value of R for mostly used shape is as below (partly this is actual and partly this is equivalent applicable).

Circular cross section of diameter d :

$$R = \frac{A}{C_r} = \frac{\pi \cdot d^2}{4} \cdot \frac{1}{\pi \cdot d} = \frac{d}{4}$$

Square cross section of sides of length a :

$$R = \frac{A}{C_r} = \frac{a^2}{4 \cdot a} = \frac{a}{4}$$

Rectangular cross section, side lengths a and b ; where a is less than b

$$\text{For calculating pressure along side a : } R = \frac{a}{4}$$

$$\text{For calculating pressure along side b : } R = \frac{a \cdot b}{2 \cdot (a + b)}$$

The value of P<sub>v</sub> and P<sub>n</sub> can be maximum, when the value of equation in bracket is equal to one. It is obvious that this can occur when y is infinite. Accordingly,

$$P_{v \max} = \frac{\gamma \cdot g \cdot R}{\mu_s \cdot K}$$

$$P_{n \max} = K \cdot \frac{\gamma \cdot g \cdot R}{\mu_s \cdot K} = \frac{\gamma \cdot g \cdot R}{\mu_s}$$

It would be clear from numerical example that P<sub>v</sub> becomes nearly maximum at very limited height, and there after its increase is at insignificant rate.

The factor K in formula is ratio of horizontal pressure divided by vertical pressure. There are differing opinions about the value of factor K applicable to material situation in hopper (bin), ranging from Rankine factor (active) to other values. One view is to use Rankine factor (active) for static pressure situation (this will give less horizontal pressure but more vertical pressure, as if friction is not fully effective). Then, higher value for emptying (dynamic) condition, which will give less vertical pressure and more horizontal pressure. This book uses the value as mentioned, i.e.  $K = 1 - \sin \phi_i \approx 1 - \sin (0.9\phi)$ . Also safety of feeder necessitates vertical pressure somewhat in upper range and hence, K value as calculated above is not enhanced by factor like 1.1.

$\mu_s$  is friction coefficient between hopper wall and material. The author's opinion is that it should be either the said friction coefficient or material internal friction coefficient whichever is less. Because the transfer of holding force applicable to body of bulk material is finally getting transferred through internal friction grip between material particles / layers. If the internal friction coefficient is less, then material thin layer (in relation to particle /

lump size) in contact with wall will act as imaginary liner, and the body of bulk material will experience friction resistance according to this imaginary liner.

**Example-1 :**

Calculate the vertical pressure  $P_v$  and horizontal pressure  $P_n$ , for vertical portion of hopper, for following application.

Material : Crushed coal, Bulk density  $\gamma$  :  $800 \text{ kg/m}^3$ , Repose angle  $\phi = 36^\circ$  (usual repose angle)

Surface friction coefficient  $\mu_s$  : 0.47 (usual value), basis welded steel flat surface, surface quality somewhat below average, for calculation here. The designer can also consider it 0.44 as per table-2.

Hopper (bin) cross section : square 5 m x 5 m

Material depth in vertical portion : 15 m (tall height has been chosen to understand pressure variation)

Calculate the value of  $P_v$  and  $P_n$  at every one meter depth from top face of material. Also calculate the value of  $P_v$  for infinite depth.

**Solution :**

$$R = (\text{hopper side length}) \div 4 = 1.25.$$

$$K = (1 - \sin 0.9 \phi) = [1 - \sin (0.9 \times 36)] = 0.4642$$

$$P_{v0} \text{ at zero meter depth, } P_{v0} = 0.$$

$$P_{n0} = K \cdot P_{v0} = 0.4642 \times 0 = 0 \text{ N/m}^2$$

$$P_{v1} = \frac{\gamma \cdot g \cdot R}{\mu_s \cdot K} \cdot \left[ 1 - \frac{1}{e^{\frac{\mu_s \cdot K \cdot y}{R}}} \right] \text{ N/m}^2$$

$$P_{v1} = \frac{800 \times 9.81 \times 1.25}{0.47 \times 0.4642} \cdot \left[ 1 - \frac{1}{e^{\frac{0.47 \times 0.4642 \times 1}{1.25}}} \right] = 44964 \times \left[ 1 - \frac{1}{2.718^{0.1745392}} \right]$$

$$= 44964 \times \left[ 1 - \frac{1}{1.190675} \right] = 7201 \text{ N/m}^2$$

$$P_{n1} = K \cdot P_{v1} = 0.4642 \times 7201 = 3343 \text{ N/m}^2$$

$P_v$  at 15 meter depth,  $P_{v15}$  :

$$P_{v15} = \frac{\gamma \cdot g \cdot R}{\mu_s \cdot K} \cdot \left[ 1 - \frac{1}{e^{\frac{\mu_s \cdot K \cdot y}{R}}} \right] \text{ N/m}^2$$

$$P_{v15} = \frac{800 \times 9.81 \times 1.25}{0.47 \times 0.4642} \cdot \left[ 1 - \frac{1}{e^{\frac{0.47 \times 0.4642 \times 15}{1.25}}} \right] = 44964 \times \left[ 1 - \frac{1}{2.718^{2.618088}} \right]$$

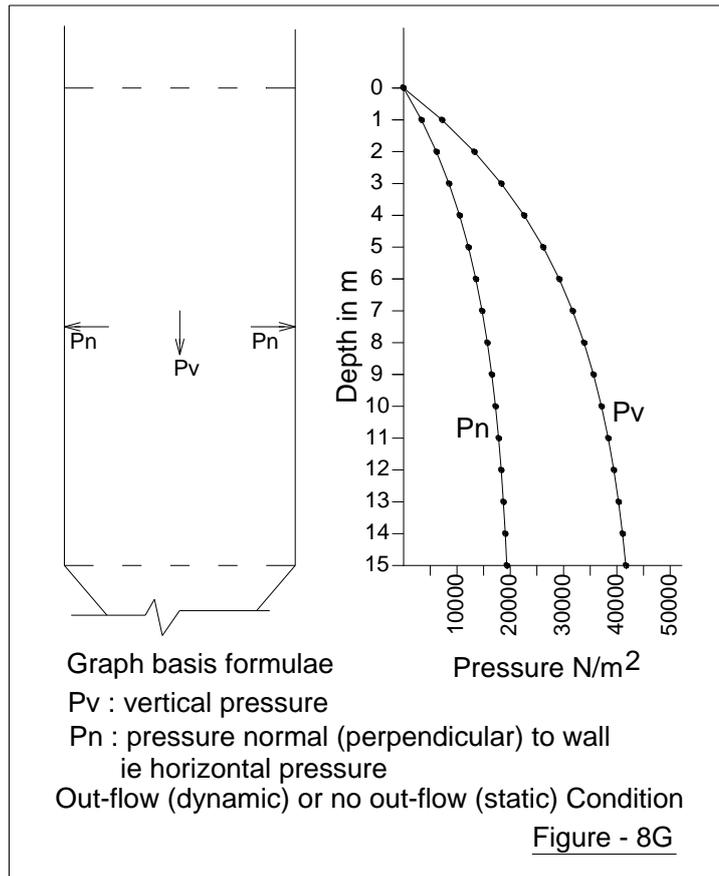
$$= 44964 \times \left[ 1 - \frac{1}{13.70576} \right] = 41683.33 \text{ N/m}^2$$

$$P_{v15} \approx 41683 \text{ N/m}^2$$

$$P_{n15} = K \cdot P_{v15} = 0.4642 \times 41683 = 19349 \text{ N/m}^2$$

The values of Pv and Pn in the range zero to 15 m are as below :

Pv0	=	0	N/m <sup>2</sup>
Pv1	=	7201	N/m <sup>2</sup>
Pv2	=	13249	N/m <sup>2</sup>
Pv3	=	18328	N/m <sup>2</sup>
Pv4	=	22594	N/m <sup>2</sup>
Pv5	=	26177	N/m <sup>2</sup>
Pv6	=	29186	N/m <sup>2</sup>
Pv7	=	31714	N/m <sup>2</sup>
Pv8	=	33836	N/m <sup>2</sup>
Pv9	=	35618	N/m <sup>2</sup>
Pv10	=	37116	N/m <sup>2</sup>
Pv11	=	38373	N/m <sup>2</sup>
Pv12	=	39429	N/m <sup>2</sup>
Pv13	=	40316	N/m <sup>2</sup>
Pv14	=	41061	N/m <sup>2</sup>
Pv15	=	41683	N/m <sup>2</sup>



Pn0	=	0	N/m <sup>2</sup>
Pn1	=	3343	N/m <sup>2</sup>
Pn2	=	6150	N/m <sup>2</sup>
Pn3	=	8508	N/m <sup>2</sup>
Pn4	=	10488	N/m <sup>2</sup>
Pn5	=	12151	N/m <sup>2</sup>

Pn6	=	13548	N/m <sup>2</sup> ,	Pn7	=	14721	N/m <sup>2</sup> ,	Pn8	=	15706	N/m <sup>2</sup> ,
Pn9	=	16533	N/m <sup>2</sup> ,	Pn10	=	17228	N/m <sup>2</sup> ,	Pn11	=	17812	N/m <sup>2</sup> ,
Pn12	=	18302	N/m <sup>2</sup> ,	Pn13	=	18714	N/m <sup>2</sup> ,	Pn14	=	19059	N/m <sup>2</sup> ,
Pn15	=	19349	N/m <sup>2</sup>								

Pv max (here, it means hopper depth is infinite), is as below :

$$Pv \text{ max} = \frac{\gamma \cdot g \cdot R}{\mu s \cdot K} = \frac{800 \times 9.81 \times 1.25}{0.47 \times 0.4642} = 44964.11 \text{ N/m}^2$$

The reader to avoid confusion for suffix maximum. As far as this particular hopper is concerned

Pv15 = 41683 N/m<sup>2</sup> is its maximum value. However, absolute maximum Pvmax as referred to infinite depth is 44964 N/m<sup>2</sup>

As can be seen nearly 92.7% of absolute maximum value reaches just at 15 m depth. Only, 7.3% will add into this if this depth extends to infinite. Figure-8G shows the values of Pv and Pn, as calculated above, at depth ranging from zero meter to 15 meter.

## PRESSURES IN BULK MATERIAL, STEEP HOPPER

This topic described the pressure values in bulk material in steep hopper. Refer cl. 8.12.0 for identification of steep hopper. The dynamic (emptying at outlet) pressure values are explained in following cl. 8.9.1. The static (non-emptying at outlet) pressure values are covered in subsequent cl. 8.9.2.

### Steep Hopper converging portion, dynamic pressure

This topic explains the pressure values within the body of bulk material, in steep converging portion of hopper. Originally, Walker, Walters, Enstand (and others) contributed during course of time, for analysis to calculate pressure values in converging portion of hopper, just few decades ago.

As explained earlier in cl. 8.6.0 last para, for such steep hopper; the pressure values in bulk material at outlet level is also the pressure value applicable on belt feeder.

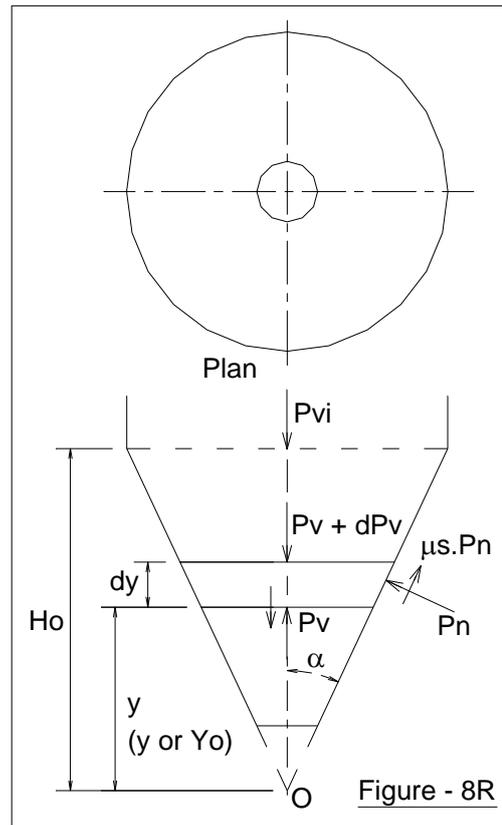


Figure-8R shows conical converging portion of steep hopper (bin / silo). The entire body of bulk material is to be considered as moving downward. Therefore, the material slice shown in this figure moves down vertically. By large, this motion can be considered of stable nature, for calculation of forces / pressure within the body of bulk material. The presence of inertial forces, attributed to difference in velocity at intersection level and at outlet level, is of insignificant value in comparison to other forces / pressure, and hence the same is ignored. Therefore, magnitude of pressure / forces within body of bulk material is calculated considering the stable / steady downward motion of this slice. This implies that the sum of downward vertical forces, is equal to the sum of upward vertical forces. The equation relates to only vertical forces (components) because the slice motion is in vertical direction.

Nomenclature :

- $P_v$  : Vertical pressure in bulk material, general notation,  $N/m^2$
- $P_{vi}$  : Vertical pressure in bulk material, at intersection,  $N/m^2$
- $P_n$  : Pressure perpendicular (normal) to wall, general notation,  $N/m^2$
- $\mu_s$  : Friction coefficient between hopper wall and slice (material). As an average, consider this value 0.9 x (usual i.e. mean value of friction coefficient) for calculation in 'this' topic.
- $\phi_s$  : Surface to material, friction angle,  $\phi_s = \tan^{-1} \mu_s$
- $\phi_i$  : Material internal effective friction angle. As an average, consider this value same as usual (mean value) repose angle, for calculation in 'this' topic. Or when necessary, use tested mean value of internal effective friction angle + 10%.
- $\gamma$  : Bulk density,  $kg/m^3$ . The formula considers this of uniform value, with respect to depth.

Ho : Vertical height from apex to intersection, m

y : Vertical height from apex to slice, m. For convenience in derivation, this is mentioned y. however, in final result it is renamed as Yo

$\alpha$  : Converging portion half angle i.e. angle between hopper side and vertical, degree.

Ke : Ratio of Pn to Pv, during emptying (dynamic) condition i.e.  $P_n = K_e \cdot P_v$

As the y is in increasing order from apex, so depiction of Pv and Pv + dPv is also in ascending order from apex.

Referring figure-8R, the derivation is as below.

Slice bottom face radius =  $y \cdot \tan \alpha$

Slice top face radius =  $(y + dy) \cdot \tan \alpha$

Slice average (midpoint) radius =  $(y + dy \div 2) \cdot \tan \alpha$

Downward force-1: Due to pressure on slice top.

$$\text{Force} = \pi (y + dy)^2 (\tan^2 \alpha) \cdot (P_v + dP_v)$$

$$= \pi (\tan^2 \alpha) \cdot (y^2 + 2ydy + dy^2) \cdot (P_v + dP_v)$$

$$= \pi (\tan^2 \alpha) \cdot (y^2 P_v + 2y dy P_v + dy^2 P_v + y^2 dP_v + 2ydy dP_v + dy^2 dP_v)$$

$dy^2 P_v$ ,  $2y dy dP_v$  and  $dy^2 dP_v$  are very small compared to other values and hence same can be ignored in summation, due to their smaller value compared to others, as per mathematical rule.

$$\therefore \text{Force} = \pi (\tan^2 \alpha) \cdot (y^2 P_v + 2y dy P_v + y^2 dP_v)$$

$$= \pi (\tan^2 \alpha) \cdot (y^2 P_v + 2y P_v dy + y^2 dP_v)$$

Downward force-2: Due to slice weight.

$$\text{Slice average radius} = \left( y + \frac{dy}{2} \right) \cdot \tan \alpha$$

$$\text{Slice average cross section} = \pi \cdot \left( y + \frac{dy}{2} \right)^2 \cdot \tan^2 \alpha$$

Slice weight = (average cross section) x (thickness perpendicular to cross section) .  $\gamma \cdot g$

$$\text{Slice weight} = \pi \cdot (\tan^2 \alpha) \cdot \left( y + \frac{dy}{2} \right)^2 dy \cdot \gamma \cdot g$$

$$= \pi \cdot \gamma \cdot g \cdot (\tan^2 \alpha) \cdot \left( y^2 + y dy + \frac{dy^2}{4} \right) dy$$

$$= \pi \cdot \gamma \cdot g \cdot (\tan^2 \alpha) \cdot \left( y^2 dy + y dy dy + \frac{dy^2}{4} dy \right)$$

Ignoring  $y dy dy$  and  $dy^2 \cdot dy \div 4$ , in summation of  $y^2 dy$ , as per mathematical rule. The slice weight is as below.

$$\text{Slice weight} = \pi \cdot \gamma \cdot g \cdot (\tan^2 \alpha) \cdot y^2 \cdot dy$$

Upward force-1 : Due to pressure at bottom.

$$\text{Upward force} = \pi (y \cdot \tan \alpha)^2 \cdot P_v = \pi \cdot (\tan^2 \alpha) \cdot y^2 \cdot P_v$$

Upward force-2 : Due to normal reaction from wall.

Slice average (midpoint) radius =  $(y + dy \div 2) \cdot \tan \alpha$

$$\text{Slice perimeter} = 2 \pi \cdot (y + dy \div 2) \cdot \tan \alpha$$

$$\text{Slice inclined face length} = dy \div \cos \alpha$$

$$\text{Slice contact area with wall} = 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha}$$

$$\text{Normal force} = 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha} \cdot P_n$$

$$\text{Normal force vertical component} = 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha} \cdot P_n \cdot \sin \alpha$$

$$= 2 \pi (\tan^2 \alpha) \left( y dy + \frac{dy^2}{2} \right) \cdot P_n$$

$$= 2 \pi (\tan^2 \alpha) \cdot P_n \cdot y \cdot dy$$

But  $P_n = K_e \cdot P_v$ . Therefore, normal force vertical component =  $2 \pi (\tan^2 \alpha) \cdot K_e \cdot P_v \cdot y \cdot dy$

Upward force-3 due to wall friction.

$$\text{Normal force} = 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha} \cdot P_n \quad (\text{as before})$$

$$\text{Friction force} = \mu_s \cdot 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha} \cdot P_n$$

$$\text{Frictional force vertical component} = \mu_s \cdot 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot \frac{dy}{\cos \alpha} \cdot P_n \cdot \cos \alpha$$

$$= \mu_s \cdot 2 \pi \left( y + \frac{dy}{2} \right) \cdot (\tan \alpha) \cdot dy \cdot P_n$$

$$= \mu_s \cdot 2 \pi \cdot (\tan \alpha) \left( y dy + \frac{dy^2}{2} \right) \cdot K_e \cdot P_v$$

$$= \mu_s \cdot 2 \pi \cdot (\tan \alpha) \cdot K_e \cdot P_v \cdot y \cdot dy$$

Equating downward forces sum to upward forces sum

$$\pi (\tan^2 \alpha) \cdot (y^2 P_v + 2y P_v dy + y^2 dP_v) + \pi \cdot \gamma \cdot g \cdot (\tan^2 \alpha) \cdot y^2 \cdot dy = \pi \cdot (\tan^2 \alpha) \cdot y^2 \cdot P_v + 2 \pi (\tan^2 \alpha) \cdot K_e \cdot P_v \cdot y \cdot dy + \mu_s \cdot 2 \pi \cdot (\tan \alpha) \cdot K_e \cdot P_v \cdot y \cdot dy$$

$$\text{Dividing both the sides by } \pi \cdot (\tan^2 \alpha)$$

$$y^2 P_v + 2y P_v dy + y^2 dP_v + \gamma \cdot g \cdot y^2 \cdot dy = y^2 \cdot P_v + 2 \cdot K_e \cdot P_v \cdot y \cdot dy + \mu_s \cdot 2 \cdot K_e \cdot P_v \cdot y \cdot dy \div (\tan \alpha)$$

$$\therefore 2y P_v dy + y^2 dP_v + \gamma \cdot g \cdot y^2 \cdot dy = 2 \cdot K_e \cdot P_v \cdot y \cdot dy + \mu_s \cdot 2 \cdot K_e \cdot P_v \cdot y \cdot dy \div \tan \alpha$$

$$\therefore y^2 dP_v = 2 \cdot K_e \cdot P_v \cdot y \cdot dy + [(\mu_s \cdot 2 \cdot K_e \cdot P_v \cdot y \cdot dy) \div (\tan \alpha)] - 2y P_v dy - \gamma \cdot g \cdot y^2 \cdot dy$$

Dividing both the sides by  $y^2 dy$

$$\therefore \frac{dP_v}{dy} = \frac{2 \cdot K_e \cdot P_v}{y} + \frac{\mu_s \cdot 2 \cdot K_e \cdot P_v}{y \cdot \tan \alpha} - \frac{2 \cdot P_v}{y} - \gamma \cdot g$$

$$\therefore \frac{dP_v}{dy} = \frac{P_v}{y} \left[ 2 \cdot K_e + \frac{\mu_s \cdot 2 \cdot K_e}{\tan \alpha} - 2 \right] - \gamma \cdot g$$

$$\therefore \frac{dP_v}{dy} = \frac{P_v}{y} \left[ 2 \left( \frac{K_e \cdot \mu_s}{\tan \alpha} + K_e \right) - 2 \right] - \gamma \cdot g$$

If  $N = 2 \left( \frac{K_e \cdot \mu s}{\tan \alpha} + K_e \right) - 2$  (where N is constant for specific application)

$$\frac{dP_v}{dy} = N \frac{P_v}{y} - \gamma \cdot g$$

This equation is a linear differential equation of first order and first degree. Therefore, its solution is derived by integrating factor (IF) method. The solution results into following equation.

$$P_v = \frac{\gamma \cdot g \cdot y}{N-1} + y^N \left[ \frac{P_{vi} - \frac{\gamma \cdot g \cdot Ho}{N-1}}{Ho^N} \right] = \frac{\gamma \cdot g \cdot y}{N-1} + \frac{y^N \cdot P_{vi}}{Ho^N} - \frac{y^N \cdot \gamma \cdot g \cdot Ho}{(N-1) \cdot Ho^N}$$

$$= \frac{\gamma \cdot g \cdot y}{N-1} - \frac{\gamma \cdot g \cdot Ho \cdot y^N}{(N-1) \cdot Ho^N} + P_{vi} \cdot \left( \frac{y}{Ho} \right)^N$$

One can use any one of the above equation to calculate  $P_v$ . However, its more convenient (easy to remember) form is as below :

$$P_v = \frac{\gamma \cdot g \cdot y}{N-1} - \frac{\gamma \cdot g \cdot Ho \cdot y^N}{(N-1) \cdot Ho^N} + P_{vi} \cdot \left( \frac{y}{Ho} \right)^N$$

$$= \frac{\gamma \cdot g \cdot y}{N-1} \frac{Ho}{Ho} - \frac{\gamma \cdot g \cdot Ho \cdot y^N}{(N-1) \cdot Ho^N} + P_{vi} \cdot \left( \frac{y}{Ho} \right)^N$$

$$= \left( \frac{\gamma \cdot g \cdot Ho}{N-1} \right) \cdot \left[ \left( \frac{y}{Ho} \right) - \left( \frac{y}{Ho} \right)^N \right] + P_{vi} \cdot \left( \frac{y}{Ho} \right)^N$$

As y is measured from apex -O, it is named  $Y_o$  to distinguish it from y used to measure depth from top. Therefore, equation is as below , where  $y = Y_o$

$$P_v = \left( \frac{\gamma \cdot g \cdot Ho}{N-1} \right) \cdot \left[ \left( \frac{Y_o}{Ho} \right) - \left( \frac{Y_o}{Ho} \right)^N \right] + P_{vi} \left( \frac{Y_o}{Ho} \right)^N$$

In equation for N, the multiplier 2 to bracketed value is related to shape i.e. shape factor. It is 2 for cone or pyramid shaped hopper, but its value is different for rectangular shape hopper. Replacing this '2' by shape factor  $C_s$ , the equation for N is as below :

$$N = C_s \left( \frac{K_e \cdot \mu s}{\tan \alpha} + K_e \right) - 2$$

Where  $C_s = 2$  for circular or square cross section of hopper, as derived in this topic.

$C_s = (1 + a \div b)$  for rectangular cross section of hopper, having width = a and length = b as per norms.

Sometimes hopper top (intersection) cross section is square, but bottom outlet is rectangle. In this case, the engineering approximation can be to use  $C_s$  value as an average of square and rectangle.

### Value of Ke

The formula for vertical pressure in converging portion of hopper, requires an important input value of Ke where :

$$K_e = P_n \div P_v$$

$P_v$  = vertical pressure in bulk material

$P_n$  = Bulk material pressure value perpendicular (normal) to hopper wall at a level common to  $P_v$ .

Refer book for derivation of formula for  $K_e$ .

### Example-3 (Steep hopper)

Calculate vertical pressure in hopper converging portion, at every 0.5m interval from hopper apex during out-flow (emptying) condition, for following application. The data are same as for example-1, but have been repeated here for convenience.

Hopper size at intersection = 5 m x 5 m

Hopper size at outlet = 0.7 m x 0.7 m and alternatively 0.7 m x 2.1 m

Hopper wall inclination to vertical,  $\alpha = 20^\circ$ , and is steep hopper.

Material coal, size (-) 50 mm,

Bulk density =  $800 \text{ kg/m}^3$

Material usual repose angle,  $\phi = 36^\circ$

Friction coefficient of wall surface and material, usual value,  $\mu_s = 0.47$

Vertical pressure at intersection,  $P_{vi} = 41683 \text{ N/m}^2$  (designer can apply surge / safety factor if need be).

### Solution

Apex to intersection height,  $H_o = 5 \div (2 \times \tan 20) = 6.8687 \text{ m}$

Apex to outlet height =  $0.7 \div (2 \times \tan 20) = 0.9616 \text{ m}$

Hence value of  $Y_o$  for calculation are,  $Y_o = 0.5, 0.9616, 1.0, 1.5, 2.0, 2.5, 3.0, 3.5, 4.0, 4.5, 5.0, 5.5, 6.0, 6.5$  and  $6.8687 \text{ m}$ .

For 'this' calculation  $\mu_s$  is 10% lower than the usual (mean) value. Hence  $\mu_s = 0.9 \times 0.47 = 0.423$

$\therefore$  Friction angle  $\phi_s$  for hopper wall and material, for this calculation  $\phi_s = \tan^{-1} 0.423 = 22.9284 \text{ degrees}$ .

For 'this' calculation the value of  $\phi_i$  is same as usual repose angle. Hence  $\phi_i = 36 \text{ degrees}$ . Or when necessary use tested mean value of internal effective friction angle + 10%.

$$\begin{aligned} \Psi &= \phi_s + \sin^{-1} \left( \frac{\sin \phi_s}{\sin \phi_i} \right) \\ &= 22.9284 + \sin^{-1} \left( \frac{\sin 22.9284}{\sin 36} \right) = 22.9284 + 41.5133 = 64.4417^\circ \end{aligned}$$

$$K_e = \frac{1 + 0.2535877}{1 - (-0.146596)} = \frac{1.2535877}{1.146590} = 1.093318$$

$C_s = 2.0$  for 0.7m x 0.7 m outlet.

$C_s = (1 + 0.7 \div 2.1) = 1.33333$  for 0.7 x 2.1 m outlet.

$$N = Cs \left( \frac{Ke \cdot \mu s}{\tan \alpha} + Ke \right) - 2$$

$$= 2 \times 1.093318 \times \left( \frac{0.423}{\tan 20} + 1 \right) - 2 = 2.727907 \quad \dots \text{for } 0.7 \text{ m outlet}$$

$$N = 1.33333 \times 1.093318 \times \left( \frac{0.423}{\tan 20} + 1 \right) - 2 = 1.151930 \quad \dots \text{for } 0.7 \text{ m} \times 2.1 \text{ m outlet}$$

Pressure values for square 0.7m x 0.7 m outlet.

Pressure at Y = 0.5 m

$$Pv0.5 = \left[ \frac{\gamma \cdot g \cdot Ho}{N - 1} \right] \cdot \left[ \left( \frac{Yo}{Ho} \right) - \left( \frac{Yo}{Ho} \right)^N \right] + Pvi \cdot \left[ \frac{Yo}{Ho} \right]^N \quad N/m^2$$

$$= \left[ \frac{800 \times 9.81 \times 6.8687}{2.727907 - 1} \right] \times \left[ \left( \frac{0.5}{6.8687} \right) - \left( \frac{0.5}{6.8687} \right)^{2.727907} \right] + 41683 \times \left[ \frac{0.5}{6.8687} \right]^{2.727907}$$

$$= 31197 \times (0.072793978 - 0.0007868686) + 41683 \times 0.0007868686 = 2246 + 33 = 2279 \quad N/m^2$$

$$Pn = Ke \cdot Pv = 1.0933182279 \times 2279 = 2492 \quad N/m^2$$

By similar calculations, the value of Pv0 = 0, Pv0.5 = 2279, Pv0.9616 = 4416, Pv1 = 4596, Pv1.5 = 6978, Pv2 = 9445, Pv2.5 = 12020, Pv3 = 14720, Pv3.5 = 17563, Pv4 = 20566, Pv4.5 = 23746, Pv5 = 27119, Pv5.5 = 30699, Pv6 = 34502, Pv6.5 = 38543, Pv6.8687 = 41683 N/m<sup>2</sup>

By similar calculations, the value of Pn0 = 0, Pn0.5 = 2492, Pn0.9616 = 4828, Pn1 = 5025, Pn1.5 = 7629, Pn2 = 10327, Pn2.5 = 13142, Pn3 = 16093, Pn3.5 = 19202, Pn4 = 22486, Pn4.5 = 25962, Pn5 = 29650, Pn5.5 = 33564, Pn6 = 37722, Pn6.5 = 42140, Pn6.8687 = 45572 N/m<sup>2</sup>

Figure-8V, depicts the pressure values in converging portion of the hopper.

Pressure values for rectangle 0.7m x 2.1 m outlet.

Pressure at Y = 0.5 m

$$Pv0.5 = \left[ \frac{\gamma \cdot g \cdot Ho}{N - 1} \right] \cdot \left[ \left( \frac{Yo}{Ho} \right) - \left( \frac{Yo}{Ho} \right)^N \right] + Pvi \cdot \left[ \frac{Yo}{Ho} \right]^N \quad N/m^2$$

$$= \left[ \frac{800 \times 9.81 \times 6.8687}{1.15193 - 1} \right] \times \left[ \left( \frac{0.5}{6.8687} \right) - \left( \frac{0.5}{6.8687} \right)^{1.15193} \right] + 41683 \times \left[ \frac{0.5}{6.8687} \right]^{1.15193}$$

$$= 354805 \times 0.0239047 + 41683 \times 0.0488892 = 8481 + 2038 = 10519 \quad N/m^2$$

$$Pn = Ke \cdot Pv = 1.093318 \times 10519 = 11500 \quad N/m^2$$

By similar calculations, the value of  $P_{v0} = 0$ ,  $P_{v0.5} = 10519$ ,  $P_{v0.9616} = 17156$ ,  $P_{v1} = 17639$ ,  $P_{v1.5} = 23217$ ,  $P_{v2} = 27723$ ,  $P_{v2.5} = 31395$ ,  $P_{v3} = 34379$ ,  $P_{v3.5} = 36775$ ,  $P_{v4} = 38655$ ,  $P_{v4.5} = 40075$ ,  $P_{v5} = 41078$ ,  $P_{v5.5} = 41701$ ,  $P_{v6} = 41973$ ,  $P_{v6.5} = 41919$ ,  $P_{v6.8687} = 41683 \text{ N/m}^2$

By similar calculations, the value of  $P_{n0} = 0$ ,  $P_{n0.5} = 11500$ ,  $P_{n0.9616} = 18757$ ,  $P_{n1} = 19286$ ,  $P_{n1.5} = 25383$ ,  $P_{n2} = 30310$ ,  $P_{n2.5} = 34325$ ,  $P_{n3} = 37588$ ,  $P_{n3.5} = 40207$ ,  $P_{n4} = 42262$ ,  $P_{n4.5} = 43815$ ,  $P_{n5} = 44912$ ,  $P_{n5.5} = 45593$ ,  $P_{n6} = 45890$ ,  $P_{n6.5} = 45830$ ,  $P_{n6.8687} = 45572 \text{ N/m}^2$

Figure-8V, depicts the pressure values in converging portion of the hopper. This example is to understand pressure values and it does not indirectly imply use of belt feeder for the same.

#### Comments

As could be seen from graph figure-8V, the  $P_v$  value at intersection is the same as in vertical portion, but  $P_n$  value generally increases at intersection compared to vertical portion.

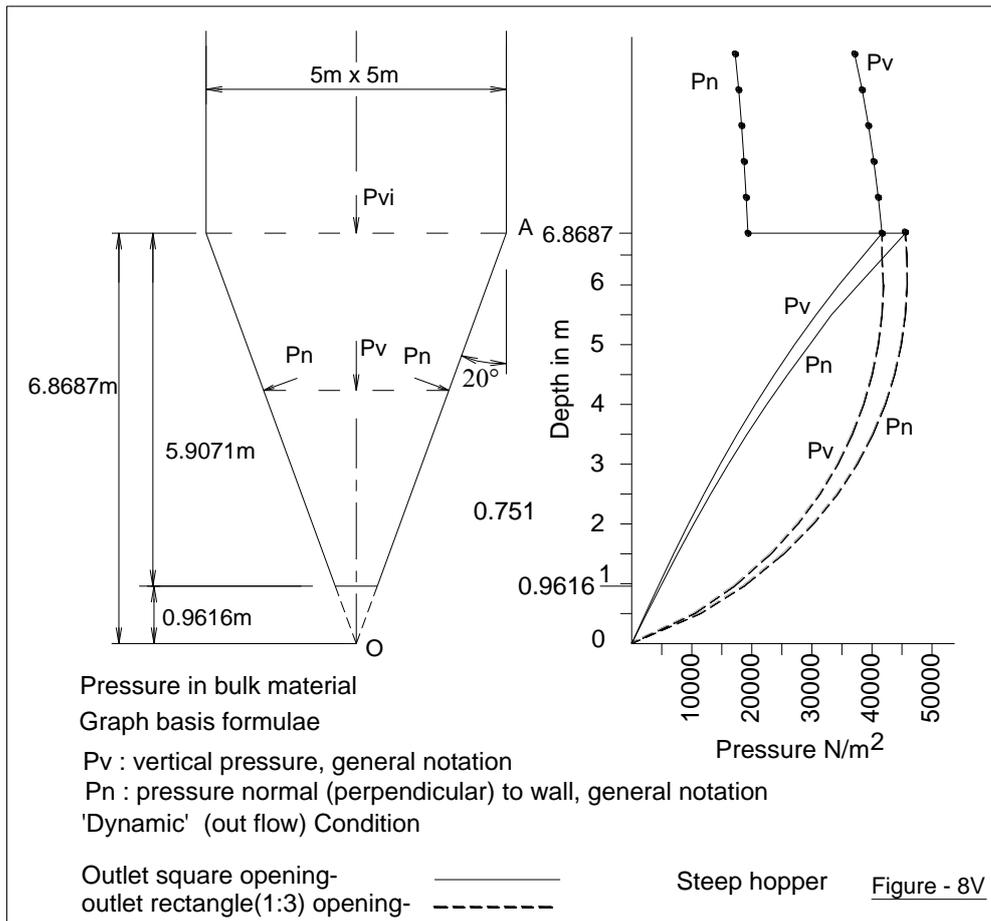
The  $P_v$  value as well as  $P_n$  values diminish as one approaches towards apex. These values are zero at apex. This continued reduction in pressure towards outlet is attributed to arch stress condition of material in converging portion. The flow behaviour is such that it maintains this stress condition during outflow as well as during short time stoppage of outflow (i.e. it will not instantly acquire static pressure values).

The formula analysis indicates that the graph shape can bulge-out or bulge-in depending upon parameters. It also indicates that the graph shape near outlet (to apex) is nearly straight line. This feature is useful for equivalent model to decide outlet force (i.e. material force acting on belt feeder, when skirt board width is of expanding type). This nearly linear shape of graph at outlet results into  $\{\text{material vertical force equivalent column height}\} \div \{\text{skirt board width}\} = \text{constant}$ , which is named as  $C_2$ .

The material pressure values (particularly  $P_n$ ) can have fluctuation (surges) due to roughness in hopper wall surface in vertical portion. Therefore, hopper (bin) design considers the pressure amplification factor on pressure values calculated as per Janssen formula.

Such pressure surge can arise / vanish during material flow in vertical portion of hopper. The average value can be taken as 1.25 and could be up to 1.6 where more reliable (safe) design is required for hopper (refer DIN for contractual needs). However, for pressure values at outlet, which is concern of belt feeder, these surges in  $P_{vi}$  have partial influence, due to nature of the formula. However, designer can certainly apply this amplification (surge) factor on  $P_{vi}$ , if he so decides.

Also, reader to note that safety considerations for hopper and belt feeder need not be same. So, designer can use appropriate value of amplification factor on  $P_{vi}$ , for belt feeder.



**Example-5** (The data are for explaining calculation and need not imply its use). This is less-steep hopper. Calculate vertical pressure in hopper converging portion, at every 0.5 m interval from hopper apex during no-outflow (non-emptying) condition and outflow (emptying) condition, for following application. The data are same (except wall angle) as for example-4, but have been repeated here for convenience.

Hopper size at intersection = 5 m x 5 m

Hopper size at outlet = 0.7 m x 0.7 m and alternatively 0.7 m x 2.1 m

Hopper wall inclination to vertical,  $\alpha = 40^\circ$ , and is less-steep.

Material size (-) 50 mm,

Bulk density =  $800 \text{ kg/m}^3$

Material usual (mean) repose angle,  $36^\circ$

Friction coefficient, wall surface and material, usual (mean) value 0.47.

Vertical pressure at intersection,  $P_{vi} = 41683 \text{ N/m}^2$

### Solution

For the calculation here,  $\mu_s = 0.9 \times 0.47 = 0.423$

Static pressure calculation 0.7 m x 0.7 m opening

This is square opening. So,  $C_s = 2$

The apex to intersection height,  $H_o = 5 \div (2 \times \tan 40) = 2.979$

The apex to outlet height =  $0.7 \div (2 \times \tan 40) = 0.4171$

For this calculation,  $K = 1.1 \times [1 - \sin(0.9 \phi')] = 1.1 \times [1 - \sin(0.9 \times 36)] = 0.5106$

$$\mu_{se} = \frac{(1 - K)}{2 \cdot \tan \alpha} = \frac{(1 - 0.5106)}{2 \times \tan 40} = 0.291622$$

$$N = \frac{0.8 \cdot Cs \cdot \mu_{se}}{\tan \alpha} = \frac{0.8 \times 2 \times 0.291622}{\tan 40} = 0.55606$$

Pv0.5 at height 0.5 m from apex as below.

$$\begin{aligned} P_{v0.5} &= \left( \frac{\gamma \cdot g \cdot Ho}{N - 1} \right) \cdot \left[ \left( \frac{Yo}{Ho} \right) - \left( \frac{Yo}{Ho} \right)^N \right] + P_{vi} \cdot \left( \frac{Yo}{Ho} \right)^N \\ &= \left( \frac{800 \times 9.81 \times 2.979}{0.55606 - 1} \right) \times \left[ \left( \frac{0.5}{2.979} \right) - \left( \frac{0.5}{2.979} \right)^{0.55606} \right] + 41683 \times \left( \frac{0.5}{2.979} \right)^{0.55606} \\ &= -52663 \times (-0.202837) + 15451 \\ &= 10682 + 15451 = 26133 \text{ N/m}^2 \end{aligned}$$

$$F_f = 1 - \frac{0.2 \cdot \mu_{se}}{\mu_{se} + \tan \alpha} = 1 - \frac{0.2 \times 0.291622}{0.291622 + \tan 40} = 0.94842$$

$$\therefore P_n = P_v \cdot F_f = 26133 \times 0.94842 = 24785 \text{ N/m}^2$$

By similar calculations, the value of  $P_{v0} = 0$ ,  $P_{v0.4171} = 24244$ ,  $P_{v0.5} = 26133$ ,  $P_{v1} = 33739$ ,  $P_{v1.5} = 37904$ ,  $P_{v2} = 40240$ ,  $P_{v2.5} = 41388$ ,  $P_{v2.979} = 41683 \text{ N/m}^2$

By similar calculations, the value of  $P_{n0} = 0$ ,  $P_{n0.4171} = 22994$ ,  $P_{n0.5} = 24785$ ,  $P_{n1} = 31999$ ,  $P_{n1.5} = 35949$ ,  $P_{n2} = 38165$ ,  $P_{n2.5} = 39253$ ,  $P_{n2.979} = 39533 \text{ N/m}^2$

Figure-8Y, depicts the pressure values in converging portion of the hopper.

#### Dynamic pressure calculation 0.7 m x 0.7 m opening

The pressure around hopper walls is same as static pressure. The calculation for pressure across discharge will need the pressure value at height 1.75 m from outlet. This pressure is  $39249 \text{ N/m}^2$

The pressure across discharge is as below :

$$\begin{aligned} P_{vd} &= \frac{We \cdot \gamma \cdot g}{\left(1 + \frac{a}{b}\right) \cdot \tan \phi} \cdot \left[ 1 - \frac{1}{e^{2.5 \left(1 + \frac{a}{b}\right) \cdot \tan \phi}} \right] + \frac{P_{vs}}{e^{2.5 \left(1 + \frac{a}{b}\right) \cdot \tan \phi}} \\ P_{vd} &= \frac{0.7 \times 800 \times 9.81}{\left(1 + \frac{0.7}{0.7}\right) \times \tan (0.9 \times 36)} \times \left[ 1 - \frac{1}{e^{2.5 \left(1 + \frac{0.7}{0.7}\right) \times \tan (0.9 \times 36)}} \right] + \frac{39249}{e^{2.5 \left(1 + \frac{0.7}{0.7}\right) \times \tan (0.9 \times 36)}} \\ &= 4328 \times 0.9581 + 1644 = 5790 \text{ N/m}^2 \\ &= \text{value can be considered } 5790 \text{ to } 5790 \times 1.35 = 7816 \text{ N/m}^2 \end{aligned}$$

Static pressure calculation 0.7 m x 2.1 m opening

This is rectangle opening. So,  $C_s = 1 + 0.7 \div 2.1 = 1.33333$

The apex to intersection height,  $H_o = 5 \div (2 \times \tan 40) = 2.979$

The apex to outlet height =  $0.7 \div (2 \times \tan 40) = 0.4171$

For this calculation,  $K = 1.1 \times [1 - \sin(\phi)] \approx 1.1 \times [1 - \sin(0.9 \phi)] = 1.1 \times [1 - \sin(0.9 \times 36)] = 0.5106$

$$\mu_{se} = \frac{(1 - K)}{2 \cdot \tan \alpha} = \frac{(1 - 0.5106)}{2 \times \tan 40} = 0.291622$$

$$N = \frac{0.8 \cdot C_s \mu_{se}}{\tan \alpha} = \frac{0.8 \times 1.33333 \times 0.291622}{\tan 40} = 0.37071$$

Pv0.5 at height 0.5 m from apex as below.

$$\begin{aligned} P_{v0.5} &= \left( \frac{\gamma \cdot g \cdot H_o}{N - 1} \right) \cdot \left[ \left( \frac{Y_o}{H_o} \right) - \left( \frac{Y_o}{H_o} \right)^N \right] + P_{vi} \cdot \left( \frac{Y_o}{H_o} \right)^N \\ &= \left( \frac{800 \times 9.81 \times 2.979}{0.37071 - 1} \right) \times \left[ \left( \frac{0.5}{2.979} \right) - \left( \frac{0.5}{2.979} \right)^{0.37071} \right] + 41683 \times \left( \frac{0.5}{2.979} \right)^{0.37071} \\ &= -37152 \times (-0.34817) + 21509 = 12935 + 21509 = 34444 \text{ N/m}^2 \end{aligned}$$

$$F_f = 1 - \frac{0.2 \cdot \mu_{se}}{\mu_{se} + \tan \alpha} = 1 - \frac{0.2 \times 0.291622}{0.291622 + \tan 40} = 0.94842$$

$$\therefore P_n = P_v \cdot F_f = 34444 \times 0.94842 = 32667 \text{ N/m}^2$$

By similar calculations, the value of  $P_{v0} = 0$ ,  $P_{v0.4171} = 32834$ ,  $P_{v0.5} = 34444$ ,  $P_{v1} = 40127$ ,  $P_{v1.5} = 42423$ ,  $P_{v2} = 43067$ ,  $P_{v2.5} = 42697$ ,  $P_{v2.979} = 41683 \text{ N/m}^2$

By similar calculations, the value of  $P_{n0} = 0$ ,  $P_{n0.4171} = 31140$ ,  $P_{n0.5} = 32667$ ,  $P_{n1} = 38057$ ,  $P_{n1.5} = 40235$ ,  $P_{n2} = 40845$ ,  $P_{n2.5} = 40494$ ,  $P_{n2.979} = 39533 \text{ N/m}^2$

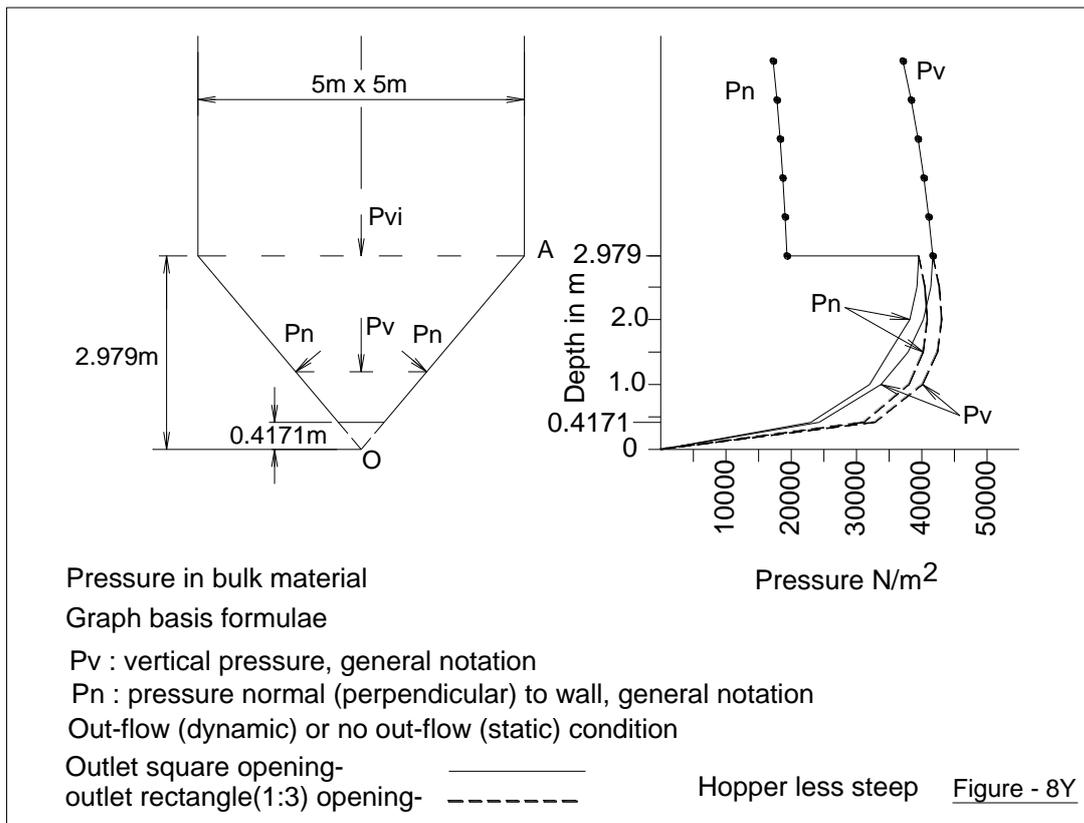
Figure-8Y, depicts the pressure values in converging portion of the hopper.

Dynamic pressure calculation 0.7 m x 2.1 m opening

The pressure around hopper walls is same as static pressure. The calculation for pressure across discharge will need the pressure value at height 1.75 m from outlet. This pressure is  $42901 \text{ N/m}^2$

The pressure across discharge is as below :

$$\begin{aligned} P_{vd} &= \frac{W_e \cdot \gamma \cdot g}{\left(1 + \frac{a}{b}\right) \cdot \tan \phi} \cdot \left[ 1 - \frac{1}{e^{2.5 \left(1 + \frac{a}{b}\right) \cdot \tan \phi}} \right] + \frac{P_{vs}}{e^{2.5 \left(1 + \frac{a}{b}\right) \cdot \tan \phi}} \\ P_{vd} &= \frac{0.7 \times 800 \times 9.81}{\left(1 + \frac{0.7}{2.1}\right) \times \tan (0.9 \times 36)} \times \left[ 1 - \frac{1}{e^{2.5 \times \left(1 + \frac{0.7}{2.1}\right) \times \tan (0.9 \times 36)}} \right] + \frac{42901}{e^{2.5 \times \left(1 + \frac{0.7}{2.1}\right) \times \tan (0.9 \times 36)}} \\ &= 6492 \times 0.87938 + 5174 = 10883 \text{ N/m}^2 \\ &= \text{value can be considered } 10883 \text{ to } 10883 \times 1.35 = 14692 \text{ N/m}^2 \end{aligned}$$



### TRANSITIONAL HOPPERS PRESSURE GRAPHS

In general, one comes across the material pressure impressive graphs mostly in context of tall hopper / silo, but rarely for transitional hoppers, although their installations are more numerous and material handling plant would be incomplete without these transitional hoppers. The depiction of pressure graphs only for tall hoppers, can create wrong impression about pressure values variation for shallow / transitional hoppers.

This topic shows following pressure graphs for typical transitional hoppers.

The hopper could be steep type when even residual material is objectionable. Alternatively, it can be less steep type, if such residual material is not objectionable. Hence, pressure graphs are shown for both the possibilities viz. steep hopper (approximately 17.5% away from boundary limit) and less steep hopper (approximately 7.5% from boundary line). Thus, following graphs are depicted in this topic.

(1) Steep hopper square outlet, static, (2) Steep hopper square outlet, dynamic, (3) Steep hopper rectangle 3:1 outlet, static (4) Steep hopper rectangle 3:1 outlet, dynamic, (5) Less-steep hopper square outlet, static and dynamic (as both have common value except across outlet), (6) Less-steep hopper rectangle 3:1 outlet, static and dynamic (as both have common value except across outlet).

The values for graphs are derived using following typical inputs to formulae.

Material usual repose angle : 35° Material bulk density,  $\gamma$  : 1000 kg/m<sup>3</sup>

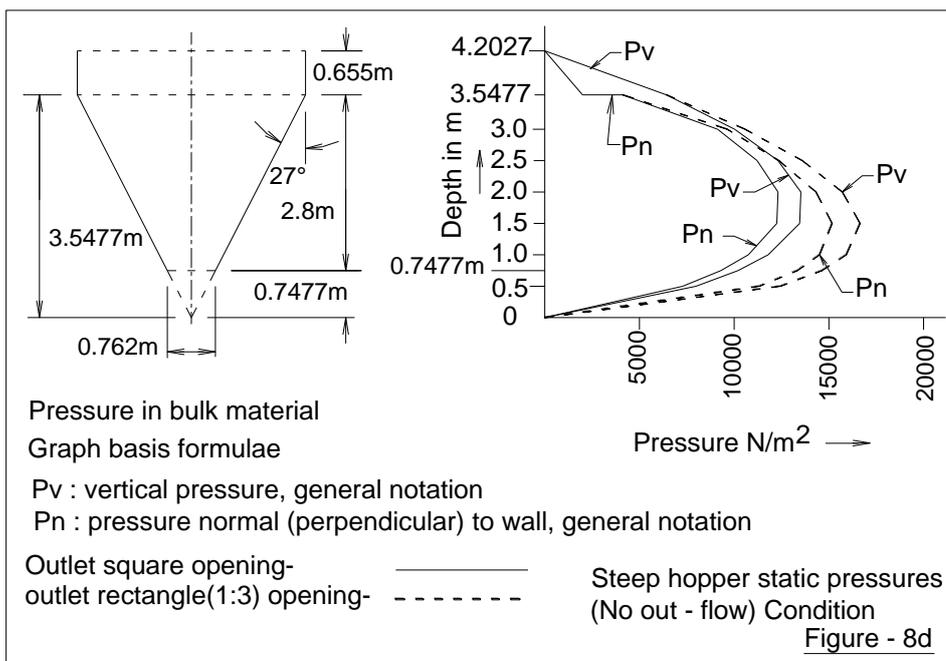
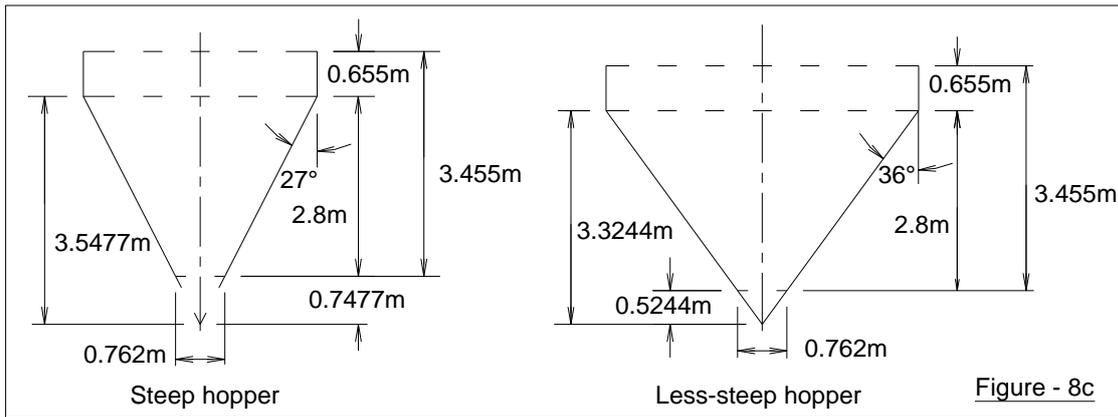
Friction coefficient, usual value, material to hopper wall : 0.45

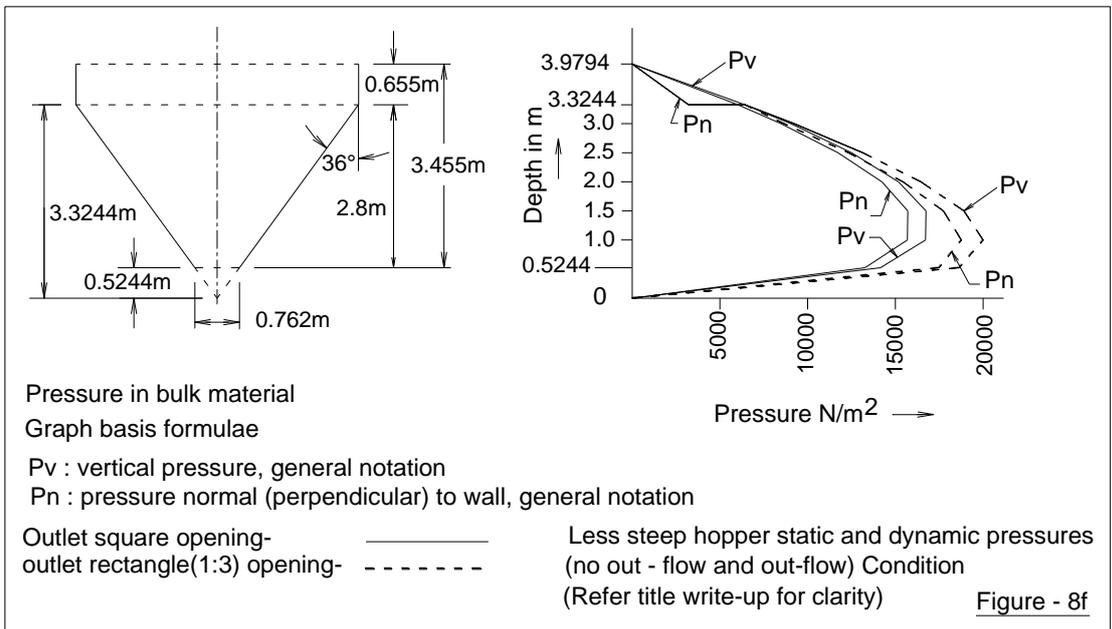
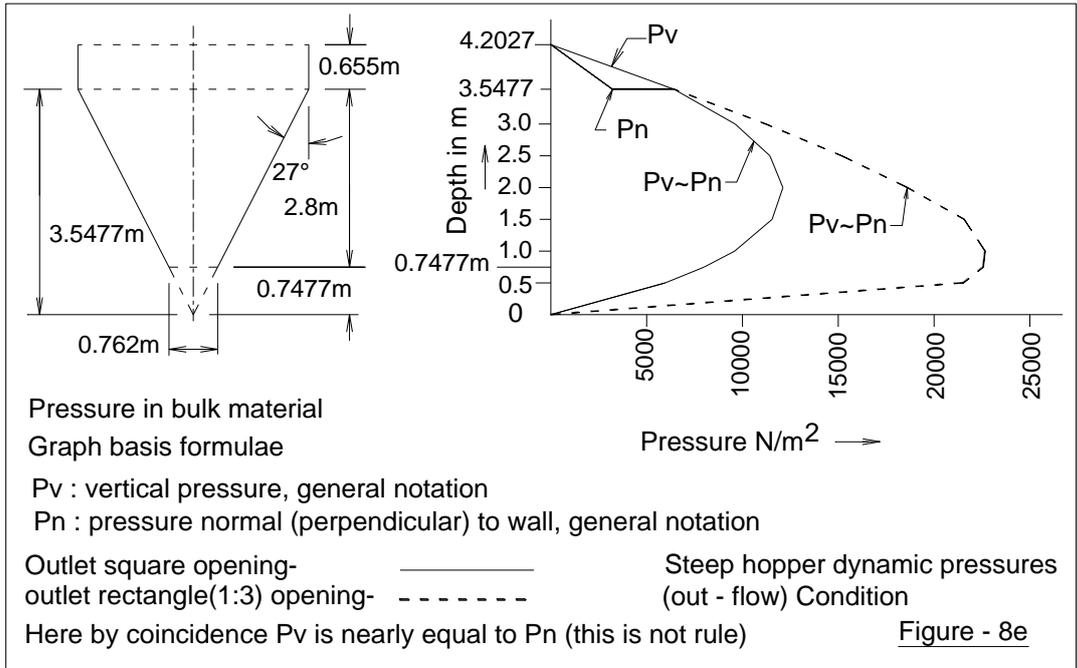
Hopper depth from outlet to top face : 3.5 m

Hopper outlet size : 0.762 m x 0.762 m and alternatively 0.762 m x 2.286 m

Hopper wall inclination to vertical,  $\alpha$  : 27°, for steep hopper

Alternatively : Hopper wall inclination to vertical,  $\alpha$  : 36°, for less-steep hopper





### TYPICAL VALUES OF $C_2$ FOR WIDELY USED INSTALLATIONS

The hopper and belt feeder can have varied arrangements, with differing dimensional features. The frequently used common arrangements from these have been chosen here to derive typical reference values for  $C_2$ . Also, dimensional features in these arrangements have been chosen such that the  $C_2$  value so derived becomes useful in wide range, as a general data.

The material bulk density  $\gamma$  is considered  $1000 \text{ kg/m}^3$ . The material density does not affect  $C_2$  value. So result would be applicable to any bulk density.

This topic derives the  $C_2$  value for following installations.

- 1) Reclaim hopper fed by pay-loader. The arrangement comprises of hopper, belt feeder and belt conveyor. The belt conveyor is at ground level or in trench. The hopper is of less steep type and outlet is square or rectangle 3:1.
- 2) Reclaim hopper fed by bulldozers. The arrangement comprises of hopper, belt feeder and belt conveyor. The belt feeder as well as belt conveyor are in tunnel. The hopper is of steep type or less steep type, and outlet is square or rectangle 3:1.
- 3) Unloading hopper for trucks. The belt feeder and conveyor are in tunnel. The hopper is of steep type or less steep type and outlet is square or rectangle 3:1
- 4) Tippler installations for unloading of wagons. Wagon capacity upto 80 tonnes. Hopper capacity upto 200 m<sup>3</sup> gross. The hopper is of steep type or less steep type and outlet is rectangle 5:1.
- 5) Tall hopper / silo installations, hopper of steep type or less steep type. The outlet is square or rectangle 3:1. (Not described here as reader can have idea from example - 3, 4, and 5).

Firstly, the  $C_2$  value will depend upon whether the hopper is of steep type or less steep type. So,  $C_2$  values are derived for following hopper types :

- For steep hopper, the used value of  $\alpha$  is approximately 20% less than boundary line value of  $\alpha$  for square outlet. In case of rectangle outlet, the used  $\alpha$  value is 30% less than boundary line value.
- For less steep hopper, the used value of  $\alpha$  is approx. 7.5% more than boundary line value of  $\alpha$ .

The mentioned boundary margins are typical boundary values considered here and do not imply rule. In application design, the designer can choose the boundary margins as explained in cl.8.12.0 last paragraph-Summary, best suited to his application.

Secondly, the  $C_2$  values are also affected by material flowability (repose angle) and friction coefficient between material and hopper wall. This can have very large (unlimited) combinations. However, to create ready reference,  $C_2$  values for feel of the subject, following two sets of input parameters have been considered.

- Grain type materials (like barley, wheat, rice, soya bean, castor beans, oat, maize, etc.), which have low value of repose angle and also the low value of friction coefficient between material and steel wall. This set of parameters, considers material usual repose angle equal to 26 degree and usual value of friction coefficient with wall as 0.28 (steel surface without protruding bolt, nuts and edges). This data would provide feel about  $C_2$  value for such application.
- Industrial average materials (like limestone, black coal, broken granite, ores, etc) which have average value of repose angle 36 degree and usual value of friction coefficient with wall as 0.47 (steel surface without protruding bolt, nuts and edges). This data would provide feel about  $C_2$  value for such application.

The reader to note that above mentioned two sets are for getting general idea about  $C_2$  value. It may also be noted that two materials of same repose angle can have different value of friction coefficients on wall. Therefore, friction coefficient value is chosen as a mean of average materials. Use  $C_2$  value preferably based on specific data, when dealing with construction design. Thus, we now have following combinations for calculations (steep hopper, less steep hopper and two sets of material data).

- Grain type material, steep hopper
- Grain type material, less steep hopper
- Industrial average material, steep hopper
- Industrial average material, less steep hopper

The boundary line value of  $\alpha$  and the chosen value of  $\alpha$  for above two sets of materials are as below.

#### Grain type materials, value of $\alpha$

For less steep hopper  $\alpha = 42^\circ$  for square and rectangular outlet.

For steep hopper  $\alpha = 31^\circ$  for square outlet and  $27^\circ$  for rectangular outlet.

#### Industrial average materials, value of $\alpha$

For less steep hopper  $\alpha = 36^\circ$  for square and rectangular outlet.

For steep hopper  $\alpha = 25^\circ$  for square outlet and  $22.5^\circ$  for rectangular outlet.

#### Belt feeder width

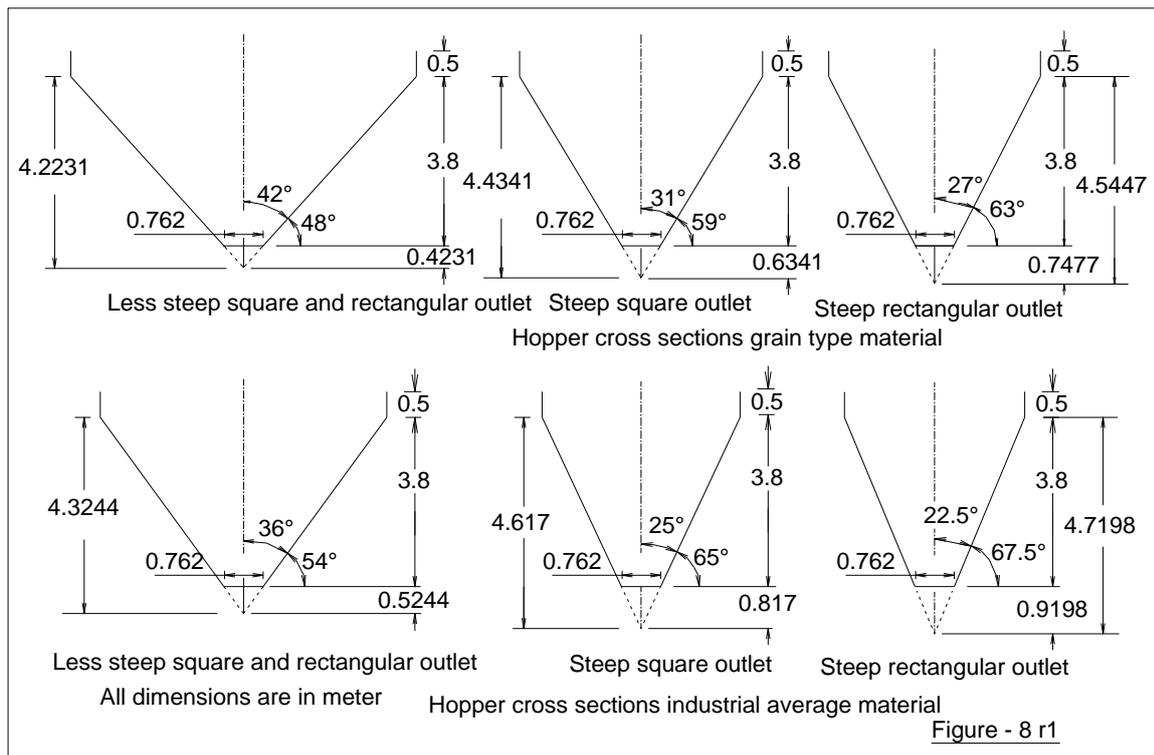
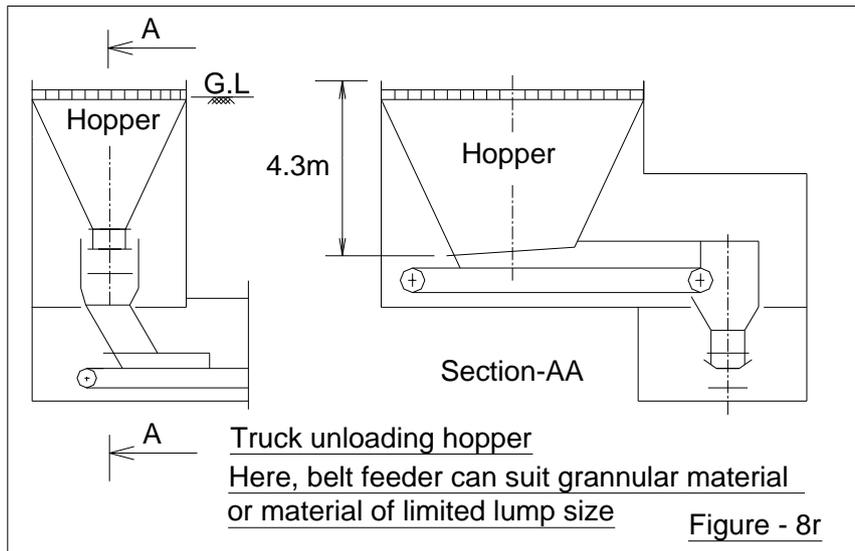
Belt feeder having 1200 mm wide belt and skirt board net width of 0.762 m (762 mm) has been considered for calculations. This  $C_2$  value derived by this does not get influenced by different belt width i.e. derived  $C_2$  value is applicable to any belt width.

Also, bulk density  $\gamma$  is considered  $1000 \text{ kg/m}^3$  for both the materials, for convenience. The bulk density does not affect  $C_2$  value. So, it is not necessary to consider lower value of bulk density for grain type material, for this exercise.

The book provides  $C_2$  value for typical installation. 1) Reclaim hopper for pay loader, 2) Underground reclaim hopper (fed by bulldozer) 3) Truck unloading hopper, 4) Side discharge wagon tipper installation, 5) Rotary wagon tipper installation. Typical values for truck unloading hopper are only mentioned here.

$C_2 = (\text{material pressure at outlet, as equivalent column height of material in metre}) \div (\text{outlet exit width metre})$

Refer next page



Case-1 : Grain type, less steep, static, square outlet.

$$C_2 = 3.34$$

Case-2 : Grain type, less steep, dynamic, square outlet.

$$C_2 = 1.35 \text{ to } 1.82$$

Case-3 : Grain type, less steep, static, rectangle outlet.

$$C_2 = 3.96$$

Case-4 : Grain type, less steep, dynamic, rectangle outlet.

$$C_2 = 2.00 \text{ to } 2.7$$

Case-5 : Grain type, steep, static, square outlet.

$$C_2 = 2.45$$

Case-6 : Grain type, steep, dynamic, square outlet.

$$C_2 = 1.42$$

Case-7 : Grain type, steep, static, rectangle outlet.

$$C_2 = 3.05$$

Case-8 : Grain type, steep, dynamic, rectangle outlet.

$$C_2 = 3.67$$

Industrial materials :

Case-1a : Average industrial material, less steep, static, square outlet.

$$C_2 = 2.07$$

Case-2a : Average industrial material, less steep, dynamic, square outlet.	$C_2 = 0.86$ to $1.16$
Case-3a : Average industrial material, less steep, static, rectangle outlet.	$C_2 = 2.83$
Case-4a : Average industrial material, less steep, dynamic, rectangle outlet.	$C_2 = 1.36$ to $1.84$
Case-5a : Average industrial material, steep, static, square outlet.	$C_2 = 1.35$
Case-6a : Average industrial material, steep, dynamic, square outlet.	$C_2 = 1.00$
Case-7a : Average industrial material, steep, static, rectangle outlet.	$C_2 = 1.95$
Case-8a : Average industrial material, steep, dynamic, rectangle outlet.	$C_2 = 2.46$

The above are the calculated direct values, specifically as per the input data mentioned under this clause. The values for general reference are as mentioned in final table.

## Chapter 9: BELT FEEDER FEED ZONE

This chapter has 48 **pages**. Following pages write-up is typical.

### BELT FEEDER FEED ZONE

The belt feeder feed zone is the most important portion of belt feeder. The feed zone has major influence on performance and life of belt feeder. The feed zone bears the material forces from hopper and converts the vertically descending flow in hopper into horizontal (nearly horizontal) flow by belt feeder. This changing of material movement by nearly  $90^\circ$  is accompanied by certain degree of turbulence and internal reshuffling and shearing of material. This results into various resistances, and also some element of uncertainty, particularly when dealing with lumpy material. Therefore, the design should be made in accordance with application conditions; giving considerations to material in-flow into hopper, this inflow cycle, lump size, abrasiveness and operating hours. The belt feeder and also many of the feeders are required to perform under arduous conditions and hence design approach needs to be on safer side. The design of any feeder to deal with granular material is comparatively easy. But the design efforts (application of mind) and risks (difference between actual and expected performance) is more when dealing with abrasive and lumpy material. Therefore, these aspects should receive due considerations while designing belt feeder.

As stated earlier, there is turbulence, internal reshuffle and shearing of material at feed zone. The changes in bulk material shape, cross section and flow path are caused by external forces / constraints in a complicated manner. The bulk materials are heterogeneous in nature. Hence, inspite of all analysis / projections; there remains some degree of uncertainty about the bulk material response to the situation (working arrangement). Therefore, an element of subjectivity cannot be avoided in design process and thereby selection of belt feeder constructional features.

Chapter-8 has already discussed a few items closely associated with feed zone such as material pressure at hopper outlet, equivalent column height, hopper outlet (adapter) wall angle cl.8.14.5, material shear at / near interface cl.8.16.0 etc., because these are common for both the chapters.

The belt feeder design and performance would be best if it provides maximum capacity, and if there is least (no) slip between material and belt as mentioned below.

- 1) For the specific belt width and speed, the belt feeder design should provide maximum possible capacity i.e. it should have maximum allowable height (depth) of material cross section at the exit end of feeding zone.
- 2) Smooth transfer of material from hopper to belt feeder i.e. material movement with least interference and turbulence. This would minimise instantaneous slip between lump and belt.

- 3) Absence (or least) portion of feed zone subjected to 'general' slip between material layer and belt. The slip between material and belt is highly detrimental to belt life, particularly for lumpy and abrasive material. The material layer is in dynamic (agitated) condition. The instantaneous slip between individual lump and belt cannot be avoided altogether, due to mutual interference and intermeshing of lumps. The statement of sr. no. 2 refers to instantaneous slip of localised nature. The statement of sr. no. 3 refers to 'general' slip between material layer portion as a whole, and belt.
- 4) Reasonably balanced flow across interface. Such flow balance is necessary for best performance of combined system of hopper and belt feeder, particularly for large sized hopper. This has more reflection on hopper performance and a system as a whole, and less as an individual item of belt feeder. This aspect has been already discussed in chapter-7.

The material flow behaviour in feed zone, depends upon various forces action on bulk material in feed zone. If the sum of propelling / pulling forces on specific body of bulk material, is sufficiently more than the sum of resisting forces, then slip would be the least. The aim of this chapter is to calculate the various forces in feed zone, and to know the effect of different parameters on these forces. Subsequently, this information can be utilised to choose right parameters for belt feeder. The chapter progressively explains the feed zone issues, by successive topics as below :

- Load equivalent model, cl.9.1.0 (for load from hopper).
- Bulk material block mass  $M_e$ , cl. 9.2.0 (equivalent to load from hopper).
- Force transfer between two bodies in contact, cl. 9.3.0
- Pushing / ejecting force  $F_{p1}$  at interface, cl.9.4.0
- Skirt board reaction force,  $F_{p2}$ , cl. 9.5.0
- Pulling / dragging force  $F_{p3}$  on material due to belt (friction grip), cl. 9.6.0
- Material shear resistance,  $F_{r1}$ , cl. 9.7.1
- Frictional resistance  $F_{r2}$  by skirt plates, cl. 9.7.2
- Material lift resistance  $F_{r3}$  in feed zone, cl. 9.7.3
- Flow behaviour in feed zone, cl. 9.8.0
- Material general shear not at interface, cl.9.9.0
- Review general shear plane, cl. 9.9.3

## **BULK MATERIAL LOAD EQUIVALENT MODEL**

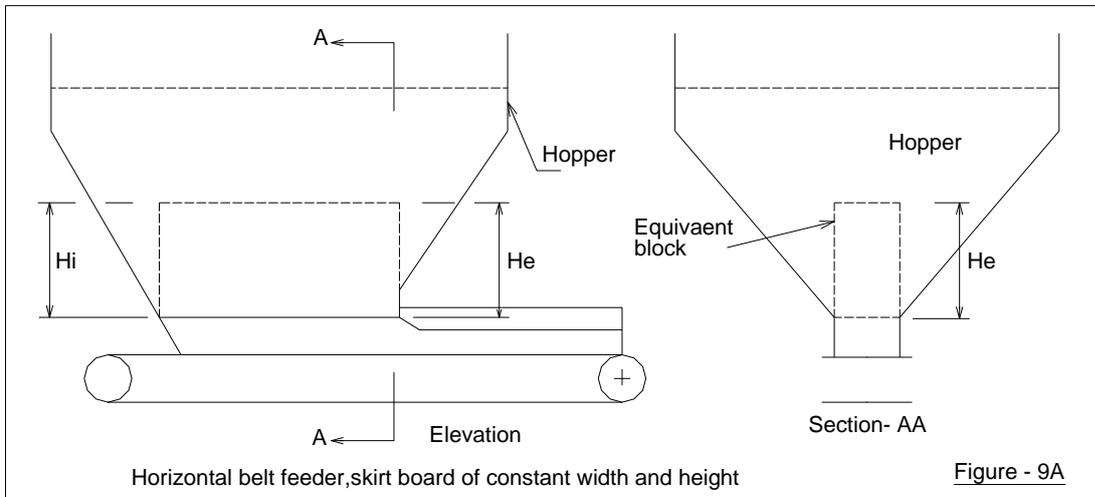
As discussed in chapter-8 the material in hopper, exerts certain pressure at interface of hopper and belt feeder. This pressure values multiplied by interface area, is the force exerted by material onto the belt feeder. The belt feeders are mostly horizontal or will have shallow inclination (higher inclination is generally avoided, but is not rule). So, the vertical pressure in bulk material has dominant effect, whereas the horizontal pressure effect is insignificant. Therefore, the belt feeders are customarily designed considering that the material force (load) is vertical, at interface.

The belt feeder design is concerned with magnitude of material force acting on belt feeder. It is convenient to account for vertical force (load) on belt feeder, by considering bulk material block of equivalent height resting at interface as shown in figure-9A, 9B, 9C and 9D. Thus in this equivalent model, although there is continuous entity of bulk material of real height in hopper, but its actual effect on belt feeder is represented by material region (block) freely standing on material layer on belt. There are no shear / frictional resistances on vertical

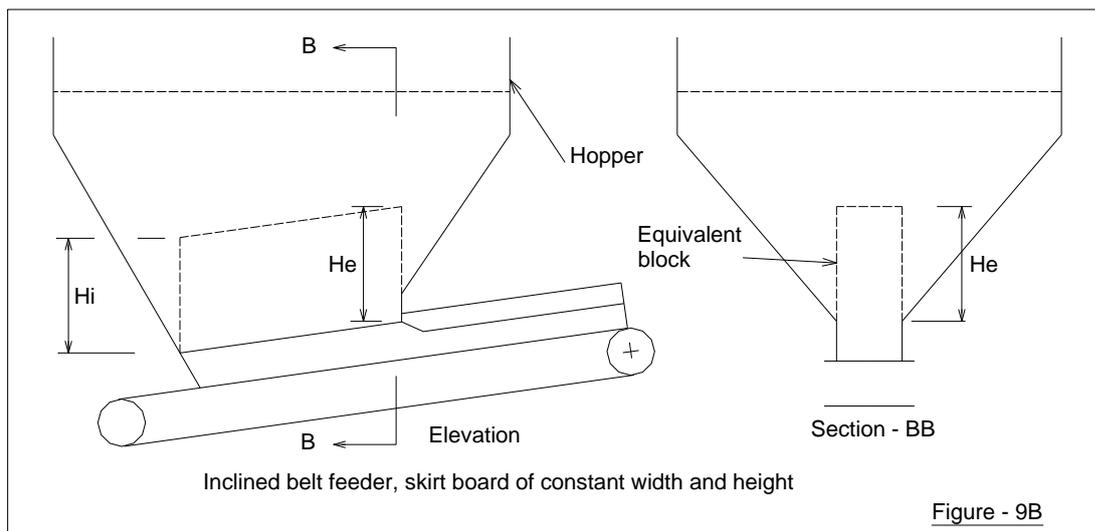
sides of this block, and there is no downward pressure by material which is above this block. The four sides of the block are vertical.

The block height is chosen such that its vertical force is equal to the actually occurring (expected) force in particular application. This material block height in a specific application is proportionate to skirt board width, by certain factor as discussed in chapter-8. This factor is named as  $C_2$ , wherein :

Block height =  $C_2 \times$  (skirt board inside net width), at each point on feed zone length.



Now, belt feeder, can have skirt board of constant width, and it can also have expanding width of skirt board (taper on width). For the skirt board of constant width, the block will also be of uniform height. In case of expanding skirt board, the block height will also increase gradually (linearly).



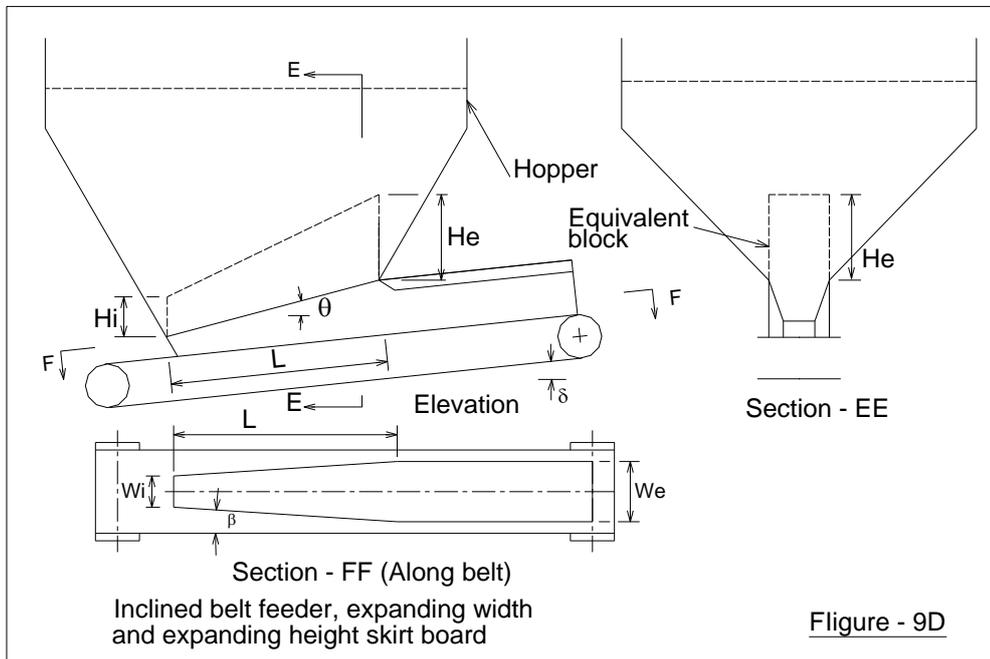
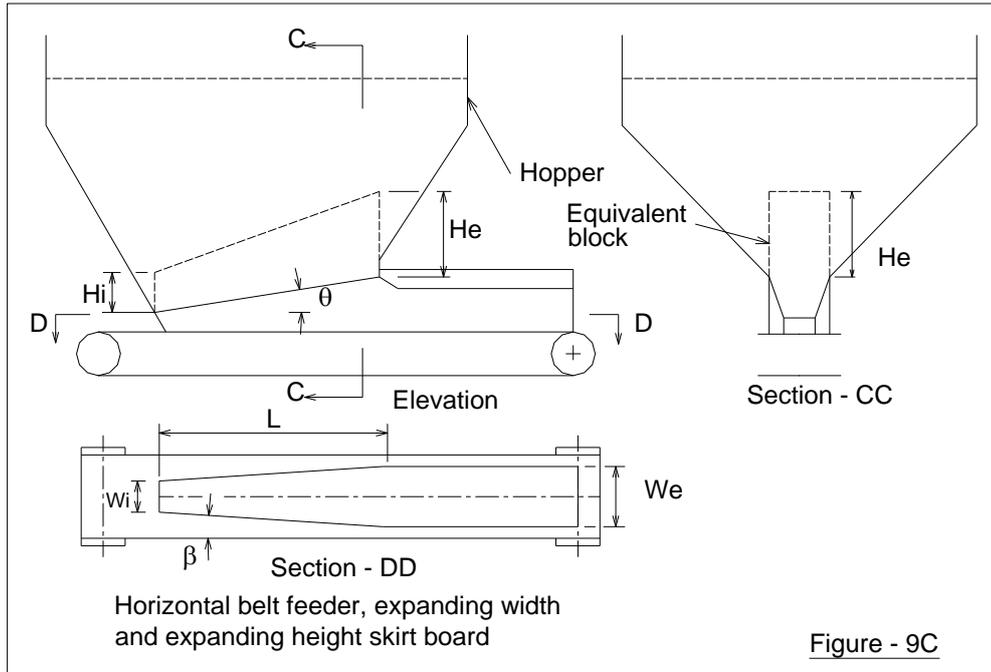
Following figures show belt feeder along with feed zone and block of equivalent model, for various arrangements of belt feeder.

Figure-9A : Horizontal belt feeder which has skirt board of constant width and constant height.

Figure-9B : Incline belt feeder which has skirt board of constant width and constant height.

Figure-9C : Horizontal belt feeder which has expanding width and expanding height of skirt board.

Figure-9D : Incline belt feeder which has expanding width and expanding height of skirt board.

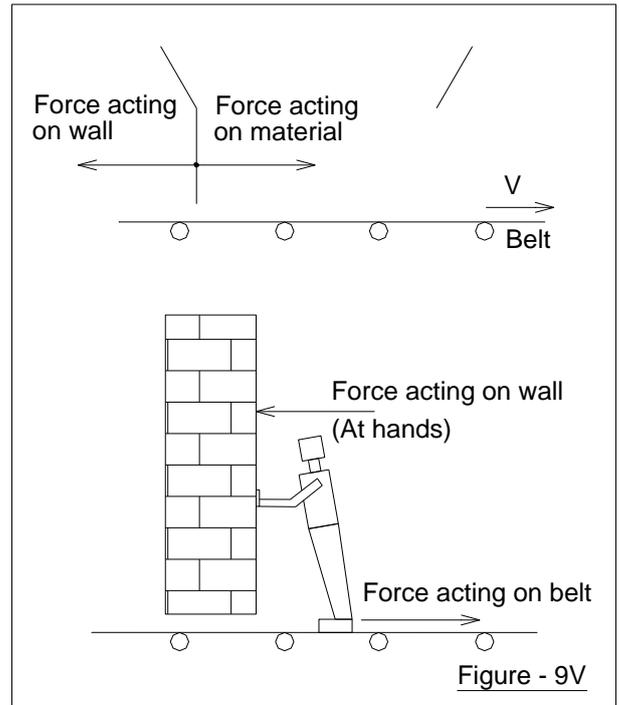


The reader to note that expanding width is also accompanied by expanding height as explained in chapter-8, cl.8.14.3 hence, figure-9C and 9D, include both these features concurrently (i.e. if there is expanding width; it will also have expanding height).

The skirt board having expansion on width, without expansion on height will not give proper result. Similarly, the skirt board having expansion on height, without expansion on width will not give proper result (blurred shear general plane).

**SKIRT BOARD REACTION FORCE  $F_{p2}$**

The bulk material in skirt board and bulk material in hopper has continuous entity. The effect of bulk material in hopper is accounted by equivalent model as per cl.-8.14.0 and cl.-9.1.0. Thus bulk material in skirt board and bulk material of equivalent block are resting on belt. The gravity force acting on this bulk material creates presence of vertical pressure within constrained body of bulk material. This vertical pressure also creates the presence of horizontal pressure within the body of bulk material as per Rankine factor or horizontal pressure factor. The Rankine factor has lower value and is considered here to compensate for constrained space within which material may not be able to spread effectively to generate force. Thus bulk material resting on belt is in pressurised state, vertically as well as horizontally.

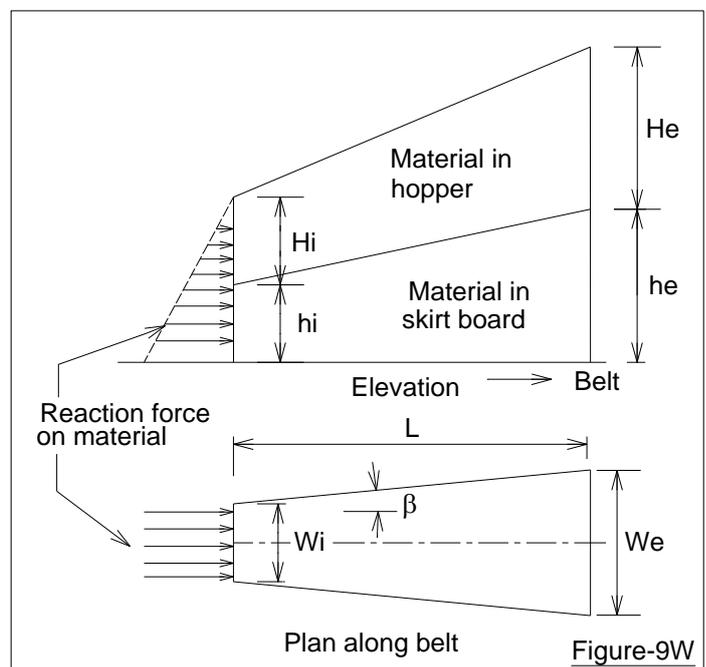


The bulk material on belt is prevented from spreading by skirt plates. Therefore, material is continuously applying thrust on skirt plates. The skirt plates are continuously applying reaction force on material. As would be seen the reaction force from skirt plates creates pushing force on material and thereby belt, as shown schematically in figure-9V. The situation is similar to a person standing on a roller surface and pushing wall. The person would move away from the wall by equal force. If the skirt board is of constant width, then the reaction force will be acting only from back plate, but the reaction force from side plates would cancel each other. In case of expanding skirt board the reaction force will be exerted on material from back plate and also from side plates. This topic decides the reaction force in following sequence :

- Reaction pushing force from back plate
- Reaction pushing force from side skirt plates

**Pushing force  $F_{p2a}$  from back plate**

This analysis considers belt being horizontal and back plate perpendicular to belt i.e. back plate in vertical plane. If the back plate is inclined to vertical, it does not change situation as its thrust direction remains horizontal. However, material entering at rear end is immediately tending to move forward. So, there may not be enough pressure and reaction force from back plate. This is subjective and is accounted by multiplier factor 0.5 to calculated value, for design safety.



Referring to figure-9W, generally  $We$ ,  $he$ ,  $\theta$ ,  $\beta$  and  $C_2$  are primary original dimension. The dimension  $hi$ ,  $Wi$ ,  $Hi$  and  $He$  are secondary in nature (i.e. derived from primary dimension). So, result is derived with reference to exit end dimension  $We$  and  $he$ .

$We$  : Skirt board exit end, m

$he$  : Skirt board material height at exit end, m

$\theta$  : Skirt board top face inclination to belt line

$Ge$  : Vertical gradient interface appearing in elevation,  $Ge = \tan\theta$

$\beta$  : Skirt plate side inclination to belt feeder centre line

$Gp$  : Skirt plate width gradient per side, appearing in plan,  $Gp = \tan\beta$

$He$  : Material equivalent block height at exit end, m

$C_2$  : Ratio of  $H \div W$ , which is constant.  $H = C_2 \cdot W$ , where  $W$  is skirt board width and  $H$  is block height at that location.

$\phi$  : Material repose angle, degrees

$$Wi = We - 2 \cdot Gp \cdot L$$

$$hi = he - Ge \cdot L$$

$$Hi = C_2 \cdot Wi = C_2 \cdot (We - 2 \cdot Gp \cdot L)$$

$$\text{Rankine factor } K = (1 - \sin\phi) \div (1 + \sin\phi)$$

$$\text{Horizontal pressure at rear end, interface level} = K \cdot \gamma \cdot g \cdot Hi = K \cdot \gamma \cdot g \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L)$$

$$\text{Horizontal pressure at rear end, belt level} = K \cdot \gamma \cdot g \cdot (hi + Hi)$$

$$= K \cdot \gamma \cdot g [ he - Ge \cdot L + C_2 \cdot (We - 2 \cdot Gp \cdot L) ]$$

$$\begin{aligned} \text{Average horizontal pressure} &= 0.5 \cdot K \cdot \gamma \cdot g \cdot [he - Ge \cdot L + C_2 \cdot (We - 2 \cdot Gp \cdot L) + C_2 \cdot (We - 2 \cdot Gp \cdot L)] \\ &= K \cdot \gamma \cdot g \cdot [0.5 \cdot (he - Ge \cdot L) + C_2 \cdot (We - 2 \cdot Gp \cdot L) ] \end{aligned}$$

$$\text{Area of back plate} = hi \cdot Wi = (he - Ge \cdot L) \cdot (We - 2 \cdot Gp \cdot L)$$

$$\text{Pushing force } F_{p2a} = (\text{Pressure}) \times (\text{Area}) \times (\text{Multiplier } 0.5 \text{ for reduced pressure effect})$$

$$= 0.5 K \cdot \gamma \cdot g \cdot [0.5 (he - Ge \cdot L) + C_2 \cdot (We - 2 \cdot Gp \cdot L)] \cdot (he - Ge \cdot L) \cdot (We - 2 \cdot Gp \cdot L) \text{ N}$$

Alternatively,

If values of  $Wi$ ,  $hi$  and  $C_2$  are known, then one can use following formula :  $Hi = C_2 \cdot Wi$

$$\text{Horizontal pressure at rear end, interface level} = K \cdot \gamma \cdot g \cdot Hi = K \cdot \gamma \cdot g \cdot C_2 \cdot Wi$$

$$\text{Horizontal pressure at rear end, belt level} = K \cdot \gamma \cdot g \cdot (hi + Hi) = K \cdot \gamma \cdot g \cdot (hi + C_2 \cdot Wi)$$

$$= K \cdot \gamma \cdot g \cdot C_2 \cdot Wi + K \cdot \gamma \cdot g \cdot hi$$

$$\text{Average horizontal pressure} = 0.5 [K \cdot \gamma \cdot g \cdot C_2 \cdot Wi + K \cdot \gamma \cdot g \cdot C_2 \cdot Wi + K \cdot \gamma \cdot g \cdot hi]$$

$$= 0.5 \cdot K \cdot \gamma \cdot g \cdot (hi + 2 \cdot C_2 \cdot Wi)$$

$$\text{Area} = hi \cdot Wi$$

$$\text{Pushing force } F_{p2a} = hi \cdot Wi \times 0.5 \cdot K \cdot \gamma \cdot g \cdot (hi + 2 \cdot C_2 \cdot Wi) \times (\text{multiplier } 0.5)$$

$$= 0.25 \cdot K \cdot \gamma \cdot g \cdot hi \cdot Wi \cdot (hi + 2 \cdot C_2 \cdot Wi)$$

The above multiplier 0.5 is for possibility of inadequate pressure between material and back plate.

## Pushing force $F_{p2b}$ from skirt board sides

Figure-9X middle portion and top portion schematically shows the material in skirt board and material equivalent in hopper. Belt line AA' is inclined at angle  $\delta$  to horizontal. Line AB and A'B' are inclined at angle  $\delta$  to vertical. Lines BC and B'C' are vertical. So line ABC and A'B'C' are not straight but are deviating by angle  $\delta$ . Normally  $\delta$  value being small these lines have been considered as vertical. So, material pressure at point A' will be corresponding to height A'B' + B'C'. The inaccuracy in result could be up to 3% or accuracy of calculation would be around 97%, which is adequate for engineering need. The derivation is based on figure-9X bottom portion.

The calculation can be made by integration and elaborate method, but the same would result into lengthy formula and inconvenient to use. It is sufficient to consider material side pressure as an average of side pressure at points A, B, B' and A', and then multiply it by skirt plate area to know pressing / reaction force. Hence, this method has been used.

Nomenclature :

We : Skirt board width at exit end, m

he : Skirt board height exit end, m

$\theta$  : Skirt board top face inclination to belt, degree;  $G_e = \tan\theta$

$\beta$  : Skirt plate inclination to belt feeder centre line, degree;  $G_p = \tan\beta$

$C_2$  : Material column factor, (constant along feed length)

L : Feed zone length along belt, m

$F_n$  : Force perpendicular to skirt plates, N

$\phi$  : Material repose angle, degree

Based on above :

$$W_i = W_e - 2 \cdot G_p \cdot L$$

$$h_i = h_e - G_e \cdot L$$

$$H_e = C_2 \cdot W_e$$

$$H_i = C_2 \cdot W_i = C_2 \cdot (W_e - 2 \cdot G_p \cdot L)$$

$$\text{Rankine factor } K = (1 - \sin\phi) \div (1 + \sin\phi)$$

$$\text{Side pressure at A} = K \cdot \gamma \cdot g \cdot (h_i + H_i) = K \cdot \gamma \cdot g \cdot [h_e - G_e \cdot L + C_2 \cdot (W_e - 2 \cdot G_p \cdot L)]$$

$$\text{Side pressure at B} = K \cdot \gamma \cdot g \cdot H_i = K \cdot \gamma \cdot g \cdot C_2 \cdot (W_e - 2 \cdot G_p \cdot L)$$

$$\text{Side pressure at B'} = K \cdot \gamma \cdot g \cdot H_e = K \cdot \gamma \cdot g \cdot C_2 \cdot W_e$$

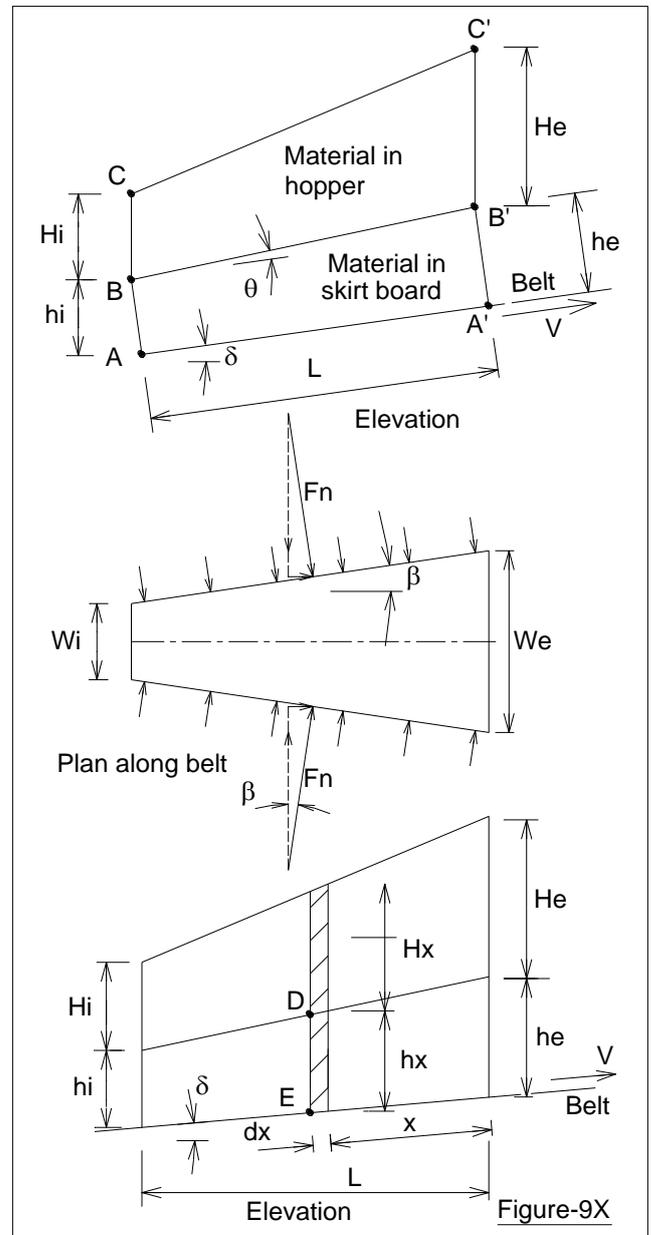


Figure-9X

$$\text{Side pressure at } A' = K \cdot \gamma \cdot g \cdot (H_e + h_e) = K \cdot \gamma \cdot g \cdot (C_2 \cdot W_e + h_e)$$

Average side pressure perpendicular to skirt plates :

$$= 0.25 K \cdot \gamma \cdot g \cdot [h_e - G_e \cdot L + C_2 \cdot W_e - 2 \cdot C_2 \cdot G_p \cdot L + C_2 \cdot W_e - 2 \cdot C_2 \cdot G_p \cdot L + C_2 \cdot W_e + C_2 \cdot W_e + h_e]$$

$$= 0.25 \cdot K \cdot \gamma \cdot g \cdot (2 \cdot h_e + 4 C_2 \cdot W_e - G_e \cdot L - 4 \cdot C_2 \cdot G_p \cdot L) \quad \text{N/m}^2$$

$$\text{Each skirt plate area} = 0.5 (h_e + h_i) \cdot L$$

( $h_e$  and  $h_i$  are actually perpendicular to  $L$ , although not in figure portion referred for derivation. The issue is insignificant for engineering calculations).

$$\therefore \text{Each skirt plate area} = 0.5 \cdot (h_e + h_e - G_e \cdot L) \cdot L = 0.5 \cdot (2 \cdot h_e - G_e \cdot L) \cdot L$$

The force on each skirt plate is the average pressure multiplied by area. This force is perpendicular to skirt plates as per Rankine factor. The force perpendicular to each skirt plate is  $F_n$ .

$$F_n = 0.125 K \cdot \gamma \cdot g \cdot L \cdot (2 h_e - G_e \cdot L) \cdot (2 \cdot h_e + 4 C_2 \cdot W_e - G_e \cdot L - 4 \cdot C_2 \cdot G_p \cdot L) \quad \text{N}$$

$$\text{Pushing force, } F_{p2b} = 2 \cdot F_n \cdot \sin\beta$$

$$F_{p2b} = 0.25 K \cdot \gamma \cdot g \cdot L \cdot (2 h_e - G_e \cdot L) \cdot (2 \cdot h_e + 4 C_2 \cdot W_e - G_e \cdot L - 4 \cdot C_2 \cdot G_p \cdot L) \cdot \sin\beta \quad \text{N}$$

### FLOW BEHAVIOUR IN FEED ZONE

The purpose of this chapter is to look into the qualitative aspects of material flow in feed zone. In this context, foregoing topics cl.9.4.0, 9.5.0 and 9.6.0 enable to calculate following forward forces which are trying to move the entire material in feed zone, in direction of belt travel (the entire body implies as if shear is taking place at interface).

- Ejecting / pushing force  $F_{p1}$  at interface
- Skirt-board reaction force  $F_{p2}$
- Pulling / dragging force  $F_{p3}$  by belt

The sum of these forward forces is  $F_p = F_{p1} + F_{p2} + F_{p3}$

The foregoing topics cl.9.7.1, 9.7.2 and 9.7.3 enable to calculate following resistances which are opposing the motion of entire body of material, along belt, in feed zone (the entire body implies as if shear is taking place at interface).

- Material shear resistance  $F_{r1}$  from interface
- Skirt board frictional resistance  $F_{r2}$
- Material lift resistance  $F_{r3}$

The sum of resistances (backward forces),  $F_r = F_{r1} + F_{r2} + F_{r3}$

It is obvious that if  $F_p > F_r$ ; then the entire body of material in skirt board will move forward (as applicable to belt feeder), as general shear along interface.

However, if  $F_p < F_r$ ; then entire body of material will not move forward, in singular mode. The shear will be occurring at plane which is more sloping, compared to interface i.e. shear plane angle  $\theta'$  is greater than interface angle  $\theta$ . The magnitude of  $\theta'$  is such that its  $F_{p'} > F_r'$ . The material ahead of such shear plane will move forward at regular pace, but material behind this shear plane will have sluggish forward motion, with more rubbing and abrasion on belt. Thus, this analysis provides the projected (likely) flow behaviour in feed zone. This analysis is to be utilised to determine / revise / refine the important parameters during design stage, as per following hints.

- 1) If the material is very abrasive or damaging in nature, then it is preferred that  $F_p > F_r$ , with respect to entire feed zone. Thus, designer should try to select feeder parameters in such application so as to have  $F_p > F_r$

or shear plane at least touching the junction of belt and back plate of skirt board. In the event if this is not feasible, then expect more wear of belt.

- 2) In case of non abrasive material, the shear plane termination before back plate can be tolerated, but still one can take some remedial measures such as comparatively less speed etc.
- 3) It would be observed that when material is under high pressure accompanied by tall skirt board, the same demands higher value of  $\theta$  and  $\beta$  for shear at interface, for proper position of shear plane. This would result into comparatively lesser length of feed zone, to have optimum belt life.
- 4) When the material is under high pressure and material is very damaging to belt (very abrasive, large lumps, sharp edges, etc) it is desirable that feed zone is restricted such that shear plane extends to and above the mid height of back plate, for proper life of belt. Such application can be tackled by feed zone of lesser length.
- 5) The shallow hopper can have shear at interface or close to interface, making it possible to have long feed zone length.
- 6) Thus this chapter analysis provides important hint / suggestions to review feed zone length, layout, belt speed etc. on case to case basis. The analysis also enables to recalculate flow balance condition in feed zone.
- 7) Flow balance review can be made by using the flow balance tables as below :

For shear at interface, use value of  $\Sigma ZT\%$  from table.

For shear plane intersecting back plate, read value of  $\Sigma ZT\%$  from table, for  $\beta$  and  $\theta'$ . The  $\Sigma ZT\%$  can be considered 1.05  $\Sigma ZT\%$  of table.

For shear plane intersecting belt, see value of  $\Sigma ZT\%$  from table, for  $\beta$  and  $\theta'$ . The  $\Sigma ZT\%$  can be considered 1.1  $\Sigma ZT\%$  of table, corresponding to applicable active length of feed zone.

The aforesaid additional factors are for opportunistic additional inflow in rear sluggish portion, which would be particularly a case when shear plane is directly intersecting the belt, and material behind this plane is trying to enter in to the active zone.

For the application which is very sensitive to flow balance, one has to calculate the flow distribution for the applicable shear plane (whether at interface or at other plane) when tabulated values are not matching with the applicable values. The designer is to refer the earlier chapter-7, which describes the calculation procedure.

- 8) It is clarified that flow balance at interface is of secondary importance, for transitional hoppers (such as for pay loader, reclaim hopper, truck unloading, wagon unloading etc.), because the flow from such hoppers is of cyclic nature. In case of unbalanced flow distribution at interface the belt feeder will tend to take more material from particular zone where level is high, however, as this level drops in each cycle, it will draw the material automatically from other zone (where material is present). Thus cyclic inflow in hopper will ensue its reasonable emptying from every side, in each cycle of few minutes (or 10 / 15 minutes). Thus making the flow balance issue of secondary nature. In such hoppers, the primary consideration should be to use  $\theta$  and  $\beta$  such that same result into least rubbing between material and belt i.e. shear at interface or shear plane intersecting back plate or minimum space between back plate and shear plane, when dealing with difficult materials.
- 9) Shear plane angle  $\theta'$  (which happens to be greater than  $\theta$ ) results in to functionally deep type adapter (extending its function into skirt board). The deep type adapter does not alter pressure pattern and  $C_2$  at interface.

### Example-6

Calculate value of  $F_p$  and  $F_r$  in feed zone, assuming shear at interface, for following application :

$h_e = 0.82$  m,  $h_i = 0.27$  m,  $H_e = 0.938 \times 3 = 2.81$  m,  $H_i = 0.4 \times 3 = 1.2$  m,  $We = 0.938$  m  
 $Wi = 0.4$  m,  $\theta = 5.710593^\circ$ ,  $Ge = 0.1$ ,  $\beta = 2.8^\circ$ ,  $Gp = 0.0489$ ,  $L = 5.5$  m,  
 $\delta = 2^\circ$ ,  $C_2 = 3$ ,  $\phi = 36^\circ$ ,  $\mu_s = 0.423$ ,  $Qd = 480$  mtph,  $\mu_b = \mu_m = 0.6346$ ,  $\gamma = 1000$  kg/m<sup>3</sup>  
Belt velocity  $V = 0.23$  mps.

Then also check whether assumption is correct.

### Solution

Firstly, this requires calculation of material block mass above interface

$$\text{Mass } M_e = \gamma \cdot C_2 [\cos(\delta + \theta)] \cdot \frac{L}{\cos\theta} \cdot \left[ We^2 - 2 Gp \cdot We \cdot L + \frac{4}{3} Gp^2 \cdot L^2 \right]$$

$$\text{Mass } M_e = 1000 \times 3 (\cos 7.7105) \times \frac{5.5}{\cos 5.710593} \cdot \left[ 0.938^2 - 2 \times 0.0489 \times 0.938 \times 5.5 + \frac{4}{3} \times 0.1^2 \times 5.5^2 \right]$$

$$= 16432.36 \times 0.471739 = 7751.789 \text{ kg}$$

$$F = 7751.789 \times 9.81 = 76045 \text{ N}$$

$$F_{p1} = F \cdot [\cos(\delta + \theta)] \cdot \sin\theta = 76045 \times \cos 7.710593 \times \sin 5.710593 = 7498.3 \text{ N}$$

$$K = (1 - \sin\phi) \div (1 + \sin\phi) = (1 - \sin 36) \div (1 + \sin 36) = 0.2596$$

$$F_{p2} = 0.25 \cdot K \cdot \gamma \cdot g \cdot h_i \cdot Wi \cdot (h_i + 2 \cdot C_2 \cdot Wi) + 0.25 K \cdot \gamma \cdot g \cdot L \cdot (2 h_e - Ge \cdot L) \cdot (2 \cdot h_e + 4 C_2 \cdot We - Ge \cdot L - 4 \cdot C_2 \cdot Gp \cdot L) \cdot \sin\beta$$

$$\therefore F_{p2} = 0.25 \times 0.2596 \times 1000 \times 9.81 \times 0.27 \times 0.4 \times (0.27 + 2 \times 3 \times 0.4) + 0.25 \times 0.2596 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.82 - 0.1 \times 5.5) \times (2 \times 0.82 + 4 \times 3 \times 0.938 - 0.1 \times 5.5 - 4 \times 3 \times 0.0489 \times 5.5) \times \sin 2.8$$

$$F_{p2} = 183.6 + 1700.1 = 1883.7 \text{ N}$$

Material mass  $M_s$  in skirt board

$$M_s = \gamma \cdot [6 h_e \cdot We \cdot L - 3 (Ge \cdot We + 2 Gp \cdot h_e) \cdot L^2 + 4 Ge \cdot Gp \cdot L^3] \div 6$$

$$= 1000 \times [6 \times 0.82 \times 0.938 \times 5.5 - 3 \times (0.1 \times 0.938 + 2 \times 0.0489 \times 0.82) \times 5.5^2 + 4 \times 0.1 \times 0.0489 \times 5.5^3] \div 6$$

$$= 1000 \times [25.3822 - 15.7901 + 3.2542] \div 6 = 2141.05 \text{ kg}$$

$$F_{p3} = \mu_b \cdot F \cdot [\cos(\delta + \theta)] \cdot [\cos\theta + \mu_m \cdot \sin\theta] + \mu_b \cdot M_s \cdot g \cdot \cos\delta$$

$$F_{p3} = 0.6346 \times 76045 \times [\cos 7.710593] \times [\cos 5.710593 + 0.6346 \times \sin 5.710593] + 0.6346 \times 2141.05 \times 9.81 \times \cos 2$$

$$= 47822.4 \times 1.058182 + 13320.8$$

$$F_{p3} = 63925.6 \text{ N}$$

$$\text{Total propelling force } F_p = F_{p1} + F_{p2} + F_{p3} = 7498.3 + 1883.7 + 63925.6 = 73307.6 \text{ N}$$

$$F_{r1} = \mu_m \cdot F \cdot [\cos(\delta + \theta)] \cdot \cos\theta$$

$$= 0.6346 \times 76045 \times \cos 7.710593 \times \cos 5.710593$$

$$F_{r1} = 47584.5 \text{ N}$$

$$F_{r2} = 0.25 \mu_s \cdot K \cdot \gamma \cdot g \cdot L \cdot (2 h_e - Ge \cdot L) \cdot (2 \cdot h_e + 4 C_2 \cdot We - Ge \cdot L - 4 \cdot C_2 \cdot Gp \cdot L) \text{ N}$$

$$= 0.25 \times 0.423 \times 0.2596 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.82 - 0.1 \times 5.5) \times (2 \times 0.82 + 4 \times 3 \times 0.938 - 0.1 \times 5.5 - 4 \times 3 \times 0.0489 \times 5.5) \text{ N}$$

$$= 1481.21 \times 1.09 \times 9.1186 = 14722.1 \text{ N}$$

$$F_{r3} = Qd \cdot g \cdot hf \div (3.6 V)$$

$$hf = (0.5 \times 5.5) \sin 2 = 0.095974 \text{ m}$$



### Case-1 : Shear plane intersecting back plate

Suppose shear plane is inclined at  $\theta'$  such that it is intersecting back plate as shown in figure-9c. The suffix ( ' ) relates to values corresponding to  $\theta'$ , such as  $Ge' = \tan\theta'$  etc. Firstly, the calculation requires the value of mass M1 of block DBB'. This block is in the form of wedge. Its mass is given by following formula :

$$BD = BA - AD = (he - L \cdot \tan\theta) - (he - L \cdot \tan\theta') = L \cdot (\tan\theta' - \tan\theta) = L \cdot (Ge' - Ge)$$

$$\begin{aligned} M1 &= \gamma \cdot (BD) \cdot L \cdot (Wi + Wi + We) \div 6 \\ &= \gamma \cdot L \cdot (Ge' - Ge) \cdot L \cdot (We - 2 \cdot Gp \cdot L + We - 2 \cdot Gp \cdot L + We) \div 6 \\ &= \gamma \cdot L^2 \cdot (Ge' - Ge) \cdot (3 \cdot We - 4 \cdot Gp \cdot L) \div 6 \end{aligned}$$

Now, to decide shear plane, one has to choose value of  $\theta'$  such that it satisfies following equation, by sufficient margin (i.e. factor 1.07 based on engineering judgement).

$$Fp1 + Fp2a + Fp2b + Fp3 \geq Fr1 + Fr2 + Fr3$$

The end result cannot be converted into simple short formula. Each of propelling force and resistance to be calculated as below and see that which value of  $\theta'$  makes them nearly equal. This exercise is very quick and simple by use of computer.

**Fp1** : This is pushing force on incline shear plane

$$Fp1 = F' \cdot [\cos(\delta + \theta')] \cdot \sin\theta' \quad N \quad (\text{similar to cl. 9.4.2})$$

$$\text{Here, } F' = (\text{Block mass BB'C'C} + \text{block mass DBB}') \cdot g = (Me + M1) \cdot g$$

Me value as per cl. 9.2.0 and M1 value as mentioned in this topic.

**Fp2a** : This is reaction force from skirt board back side, directly acting on material in motion.

$$hi' = he - L \cdot \tan\theta' = he - Ge' \cdot L$$

$$Wi' = Wi = We - 2 \cdot Gp \cdot L$$

$$\begin{aligned} \text{Vertical pressure at A} &= \gamma \cdot g \cdot (Hi + hi) = \gamma \cdot g \cdot (C_2 \cdot Wi + he - Ge \cdot L) \\ &= \gamma \cdot g \cdot [C_2(We - 2 \cdot Gp \cdot L) + he - Ge \cdot L] \end{aligned}$$

$$\text{Vertical pressure D} = \gamma \cdot g \cdot (Hi + BD) = \gamma \cdot g \cdot [C_2 \cdot (We - 2 \cdot Gp \cdot L) + L \cdot (Ge' - Ge)]$$

$$\text{Average vertical pressure} = 0.5 \cdot \gamma \cdot g \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge)]$$

The belt is tending to carry forward material near back plate. So, there may not be enough pressure. This is accounted by multiplying by 0.5 in the formula as below :

$$\begin{aligned} Fp2a &= K \cdot (hi' \cdot Wi) \cdot 0.5 \cdot \gamma \cdot g \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge)] \times 0.5 \\ &= 0.25 \cdot K \cdot \gamma \cdot g \cdot (hi' \cdot Wi) \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge)] \quad N \end{aligned}$$

**Fp2b** : This is reaction force from skirt board sides, directly acting on material in motion. The vertical pressure on skirt board can be considered as an average of vertical pressure at points A, D, B' and A'.

$$\text{Vertical pressure at A} = \gamma \cdot g \cdot [C_2(We - 2 \cdot Gp \cdot L) + he - Ge \cdot L]$$

$$\text{Vertical pressure at D} = \gamma \cdot g \cdot [C_2 \cdot (We - 2 \cdot Gp \cdot L) + L \cdot (Ge' - Ge)]$$

$$\text{Vertical pressure at B'} = \gamma \cdot g \cdot He = \gamma \cdot g \cdot C_2 \cdot We$$

$$\text{Vertical pressure at A'} = \gamma \cdot g \cdot (He + he) = \gamma \cdot g \cdot [C_2 \cdot We + he]$$

$$\text{Avg. vertical pressure} = 0.25 \gamma \cdot g \cdot [2 C_2 (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge) + 2 C_2 \cdot We + he]$$

$$\begin{aligned} \text{Area of each skirt plate for pressure} &= 0.5 (AD + he) \cdot L = 0.5 (he - Ge' \cdot L + he) \cdot L \\ &= 0.5 (2 he - Ge' \cdot L) \cdot L \end{aligned}$$

$$\text{The area of two skirt plates} = (2 he - Ge' \cdot L) \cdot L$$

$$Fp2b = 0.25 K \cdot \gamma \cdot g \cdot L [(2 he - Ge' \cdot L)] \cdot [2 C_2 (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge) + 2 C_2 \cdot We + he] \cdot \sin\beta$$

$$\therefore F_{p2b} = 0.25 K \cdot \gamma \cdot g \cdot L [(2 h_e - G e' \cdot L)] [2 h_e + 4 C_2 \cdot W e - 2 \cdot G e \cdot L + G e' \cdot L - 4 C_2 \cdot G p \cdot L] \cdot \sin \beta \text{ N}$$

**Fp3** : This is pulling force by belt, acting on material in motion.

$$\text{Here, } F' = (\text{Block mass BB'C'C} + \text{block mass DBB}') \cdot g = (M_e + M_1) \cdot g$$

This  $F'$  is same as mentioned under  $F_{p1}$ .

$$F_{p3} = \mu_b \cdot F' \cdot [\cos(\delta + \theta')] \cdot [\cos \theta' + \mu_m \cdot \sin \theta'] + \mu_b \cdot M_s' \cdot g \cdot \cos \delta \quad \text{N} \quad (\text{in a manner similar to cl.9.6.0})$$

Where,  $M_s' = \gamma \cdot [6 \cdot h_e \cdot W e \cdot L - 3 (G e' \cdot W e + 2 \cdot G p \cdot h_e) \cdot L^2 + 4 \cdot G e' \cdot G p \cdot L^3] \div 6 \quad \text{Kg}$  (in a manner similar to cl. 9.6.1)

**Fr1** : This is shear resistance, against material motion

$$F_{r1} = \mu_m \cdot F' \cdot [\cos(\delta + \theta')] \cdot \cos \theta' \quad \text{N} \quad (\text{in a manner similar to cl.9.7.1})$$

**Fr2** : Skirt board resistance  $F_{r2}$

The pressing force on skirt plates, as per  $F_{p2b}$  is as below.

$$\text{Pressing force} = 0.25 K \cdot \gamma \cdot g \cdot L [(2 h_e - G e' \cdot L)] [2 h_e + 4 C_2 \cdot W e - 2 \cdot G e \cdot L + G e' \cdot L - 4 C_2 \cdot G p \cdot L] \text{ N}$$

$$F_{r2} = 0.25 \mu_s \cdot K \cdot \gamma \cdot g \cdot L [(2 h_e - G e' \cdot L)] [2 h_e + 4 C_2 \cdot W e - 2 \cdot G e \cdot L + G e' \cdot L - 4 C_2 \cdot G p \cdot L] \text{ N}$$

**Fr3** : This is material lift resistance in feed zone

$$F_{r3} = Q_d \cdot G \cdot h_f \div (3.6 V) \quad \text{N}$$

$$\text{Where } h_f = (0.5 \cdot L) \cdot \sin \delta$$

As mentioned in the beginning of this topic, choose the value of  $\theta'$  such that it satisfies the following equation :

$$F_{p1} + F_{p2a} + F_{p2b} + F_{p3} \geq 1.07 \times (F_{r1} + F_{r2} + F_{r3})$$

This is quite easy and quick by use of computer. The  $\theta'$  value valid for this equation is

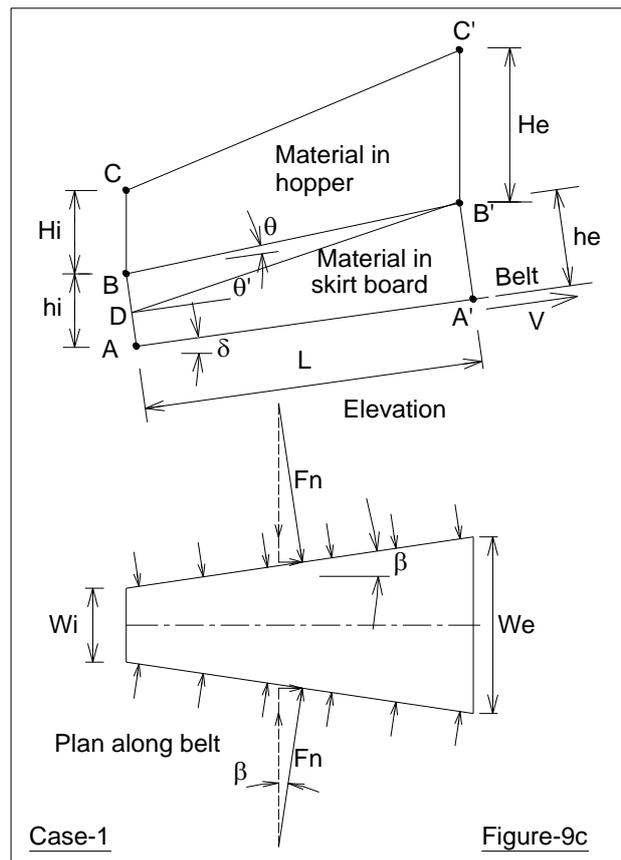
$$\theta < \theta' < \tan^{-1}(h_e \div L)$$

## MATERIAL GENERAL SHEAR NOT AT INTERFACE

The formulae in foregoing cl. 9.4.0, 9.5.0, 9.6.0 and 9.7.0 are for calculating propelling force and resistance when material shear is at interface. Now on calculating  $F_p$  and  $F_r$  on the basis of shear at interface, it might happen that  $F_p$  as above is not larger than  $1.07 F_r$  as above. This means material general shear will not occur at interface, but will be occurring at a plane more inclined than interface. The designer would like to know the probable position of this shear plane. This topic discusses and derives the likely position of such plane for general shear.

There are two possibilities viz. case-1 and case-2 as below :

Case-1 : Referring to figure-9c, the shear plane is intersecting back plate.



Case-2 : Referring to figure-9d, the shear plane is lower than back plate and is directly intersecting the belt within feed zone.

There are two distinct formulae for case-1 and case-2; to decide value of  $\theta'$  (i.e. angle of shear plane to belt).

The designer to proceed in following sequence to decide location of general shear plane:

- 4) First check whether shear is occurring at interface, as per foregoing clauses and examples-6 & 7 on the basis of values of  $F_p$  and  $F_r$ .
- 5) If  $F_p$  is not larger than  $1.07F_r$  as per serial no.1; then use formula of case-1. The cas-1 formula can be used for  $\theta'$  value maximum, till it touches point A of figure-9c.

$$\theta' \text{ maximum value} = \tan^{-1} (h_e \div L)$$

$$\theta < \theta' < \tan^{-1} (h_e \div L)$$

- 6) If  $F_p$  is still not larger than  $1.07F_r$  as per serial no. 2 above; then use formula of case-2. In this case  $\theta'$  has limitation as below :

$$\tan^{-1} (h_e \div L) < \theta' < 90^\circ$$

One will rarely cross 10 to 15 degree. However, this formula can enable to see the flow pattern at unlimited points within feed zone by choosing different values of  $\theta'$ .

### Case-1 : Shear plane intersecting back plate

Suppose shear plane is inclined at  $\theta'$  such that it is intersecting back plate as shown in figure-9c. The suffix ( ' ) relates to values corresponding to  $\theta'$ , such as  $Ge'$  =  $\tan\theta'$  etc. Firstly, the calculation requires the value of mass  $M_1$  of block  $DBB'$ . This block is in the form of wedge. Its mass is given by following formula :

$$BD = BA - AD = (h_e - L \cdot \tan\theta) - (h_e - L \cdot \tan\theta') = L \cdot (\tan\theta' - \tan\theta) = L \cdot (Ge' - Ge)$$

$$M_1 = \gamma \cdot (BD) \cdot L \cdot (W_i + W_i + W_e) \div 6$$

$$= \gamma \cdot L \cdot (Ge' - Ge) \cdot L \cdot (W_e - 2 \cdot G_p \cdot L + W_e - 2 \cdot G_p \cdot L + W_e) \div 6$$

$$= \gamma \cdot L^2 \cdot (Ge' - Ge) \cdot (3 \cdot W_e - 4 \cdot G_p \cdot L) \div 6$$

Now, to decide shear plane, one has to choose value of  $\theta'$  such that it satisfies following equation, by sufficient margin (i.e. factor 1.07 based on engineering judgement).

$$F_{p1} + F_{p2a} + F_{p2b} + F_{p3} \geq F_{r1} + F_{r2} + F_{r3}$$

The end result cannot be converted into simple short formula. Each of propelling force and resistance to be calculated as below and see that which value of  $\theta'$  makes them nearly equal. This exercise is very quick and simple by use of computer.

**F<sub>p1</sub>** : This is pushing force on incline shear plane

$$F_{p1} = F' \cdot [\cos(\delta + \theta')] \cdot \sin\theta' \quad N \quad (\text{similar to cl. 9.4.2})$$

$$\text{Here, } F' = (\text{Block mass } BB'C'C + \text{block mass } DBB') \cdot g = (M_e + M_1) \cdot g$$

$M_e$  value as per cl. 9.2.0 and  $M_1$  value as mentioned in this topic.

**F<sub>p2a</sub>** : This is reaction force from skirt board back side, directly acting on material in motion.

$$h_i' = h_e - L \cdot \tan\theta' = h_e - Ge' \cdot L$$

$$W_i' = W_i = W_e - 2 \cdot G_p \cdot L$$

$$\text{Vertical pressure at A} = \gamma \cdot g \cdot (H_i + h_i) = \gamma \cdot g \cdot (C_2 \cdot W_i + h_e - Ge \cdot L)$$

$$= \gamma \cdot g \cdot [C_2(W_e - 2 \cdot G_p \cdot L) + h_e - Ge \cdot L]$$

$$\text{Vertical pressure D} = \gamma \cdot g \cdot (H_i + BD) = \gamma \cdot g \cdot [C_2 \cdot (W_e - 2 \cdot G_p \cdot L) + L \cdot (Ge' - Ge)]$$

$$\text{Average vertical pressure} = 0.5 \cdot \gamma \cdot g \cdot [2 \cdot C_2 \cdot (W_e - 2 \cdot G_p \cdot L) + h_e - Ge \cdot L + L \cdot (Ge' - Ge)]$$

The belt is tending to carry forward material near back plate. So, there may not be enough pressure. This is accounted by multiplying by 0.5 in the formula as below :

$$Fp2a = K \cdot (hi' \cdot Wi) \cdot 0.5 \cdot \gamma \cdot g \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge)] \times 0.5$$

$$= 0.25 \cdot K \cdot \gamma \cdot g \cdot (hi' \cdot Wi) \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge)] \quad N$$

**Fp2b** : This is reaction force from skirt board sides, directly acting on material in motion. The vertical pressure on skirt board can be considered as an average of vertical pressure at points A, D, B' and A'.

$$\text{Vertical pressure at A} = \gamma \cdot g \cdot [C_2(We - 2 \cdot Gp \cdot L) + he - Ge \cdot L]$$

$$\text{Vertical pressure at D} = \gamma \cdot g \cdot [C_2 \cdot (We - 2 \cdot Gp \cdot L) + L \cdot (Ge' - Ge)]$$

$$\text{Vertical pressure at B}' = \gamma \cdot g \cdot He = \gamma \cdot g \cdot C_2 \cdot We$$

$$\text{Vertical pressure at A}' = \gamma \cdot g \cdot (He + he) = \gamma \cdot g \cdot [C_2 \cdot We + he]$$

$$\text{Avg. vertical pressure} = 0.25 \gamma \cdot g \cdot [2 C_2 (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge) + 2 C_2 \cdot We + he]$$

$$\text{Area of each skirt plate for pressure} = 0.5 (AD + he) \cdot L = 0.5 (he - Ge' \cdot L + he) \cdot L$$

$$= 0.5 (2 he - Ge' \cdot L) \cdot L$$

$$\text{The area of two skirt plates} = (2 he - Ge' \cdot L) \cdot L$$

$$Fp2b = 0.25 K \cdot \gamma \cdot g \cdot L [(2 he - Ge' \cdot L)] \cdot [2 C_2 (We - 2 \cdot Gp \cdot L) + he - Ge \cdot L + L \cdot (Ge' - Ge) + 2 C_2 \cdot We + he] \cdot \sin\beta$$

$$\therefore Fp2b = 0.25 K \cdot \gamma \cdot g \cdot L [(2 he - Ge' \cdot L)] [2 he + 4 C_2 \cdot We - 2 \cdot Ge \cdot L + Ge' \cdot L - 4 C_2 \cdot Gp \cdot L] \cdot \sin\beta \quad N$$

**Fp3** : This is pulling force by belt, acting on material in motion.

$$\text{Here, } F' = (\text{Block mass BB'C'C} + \text{block mass DBB}') \cdot g = (Me + M1) \cdot g$$

This F' is same as mentioned under Fp1.

$$Fp3 = \mu b \cdot F' \cdot [\cos(\delta + \theta')] \cdot [\cos\theta' + \mu m \cdot \sin\theta'] + \mu b \cdot Ms' \cdot g \cdot \cos\delta \quad N \quad (\text{in a manner similar to cl.9.6.0})$$

$$\text{Where, } Ms' = \gamma \cdot [6 \cdot he \cdot We \cdot L - 3 (Ge' \cdot We + 2 \cdot Gp \cdot he) \cdot L^2 + 4 \cdot Ge' \cdot Gp \cdot L^3] \div 6 \quad \text{Kg} \quad (\text{in a manner similar to cl. 9.6.1})$$

**Fr1** : This is shear resistance, against material motion

$$Fr1 = \mu m \cdot F' \cdot [\cos(\delta + \theta')] \cdot \cos\theta' \quad N \quad (\text{in a manner similar to cl.9.7.1})$$

**Fr2** : Skirt board resistance Fr2

The pressing force on skirt plates, as per Fp2b is as below.

$$\text{Pressing force} = 0.25 K \cdot \gamma \cdot g \cdot L [(2 he - Ge' \cdot L)] [2 he + 4 C_2 \cdot We - 2 \cdot Ge \cdot L + Ge' \cdot L - 4 C_2 \cdot Gp \cdot L] \quad N$$

$$Fr2 = 0.25 \mu s \cdot K \cdot \gamma \cdot g \cdot L [(2 he - Ge' \cdot L)] [2 he + 4 C_2 \cdot We - 2 \cdot Ge \cdot L + Ge' \cdot L - 4 C_2 \cdot Gp \cdot L] \quad N$$

**Fr3** : This is material lift resistance in feed zone

$$Fr3 = Qd \cdot G \cdot hf \div (3.6 V) \quad N$$

$$\text{Where } hf = (0.5 \cdot L) \cdot \sin\delta$$

As mentioned in the beginning of this topic, choose the value of  $\theta'$  such that it satisfies the following equation :

$$Fp1 + Fp2a + Fp2b + Fp3 \geq 1.07 \times (Fr1 + Fr2 + Fr3)$$

This is quite easy and quick by use of computer. The  $\theta'$  value valid for this equation is

$$\theta < \theta' < \tan^{-1}(he \div L)$$

In the foregoing derivation, we have considered shear plane commencing exactly at exit point, to avoid complexities in formula. Actually, it starts somewhat behind the exit point. Use the value of  $\theta'$  as per this derivation and draw this shear plane at angle  $\theta'$  from its actual starting point and see how long is the 'directly' active feed zone. This would provide engineering assessment of flow pattern in feed zone, which is the purpose of knowing the shear plane position. Thereby, the engineering judgement for magnitude of abrasion, velocity

gradient, average velocity etc. for comparative decision. The actual starting point of shear plane can be considered as below.

Distance from exit point :  $1.25 \times$  (skirt board width), for grain type free flowing granular materials.

Distance from exit point :  $0.75 \times$  (skirt board width), for other materials.

### Case-2 : Shear plane not reaching back plate

Assuming shear at interface and using their applicable formula, if  $F_p < 1.07 F_r$ ; then assumption is not correct and designer has to investigate as per case-1. If  $F_p$  is still less than  $1.07 F_r$  by using the formula as per case-1; then designer has to try for the next stage and use formulae as per this cl.9.9.2, to decide the value of  $\theta'$  and thereby the position of general shear plane.

This pattern of material shear in skirt board can arise for deep material layer, high pressure at interface, unfavorable value of friction coefficients, very long feed zone, inadequate gradients of skirt board expansion. In this pattern; the shear plane is not reaching the back plate. In actual examples, it would be observed that this pattern of shear occurs less frequently.

The hopper material pressure at interface remains unchanged, and part of skirt board functions as 'deep type' adapter.

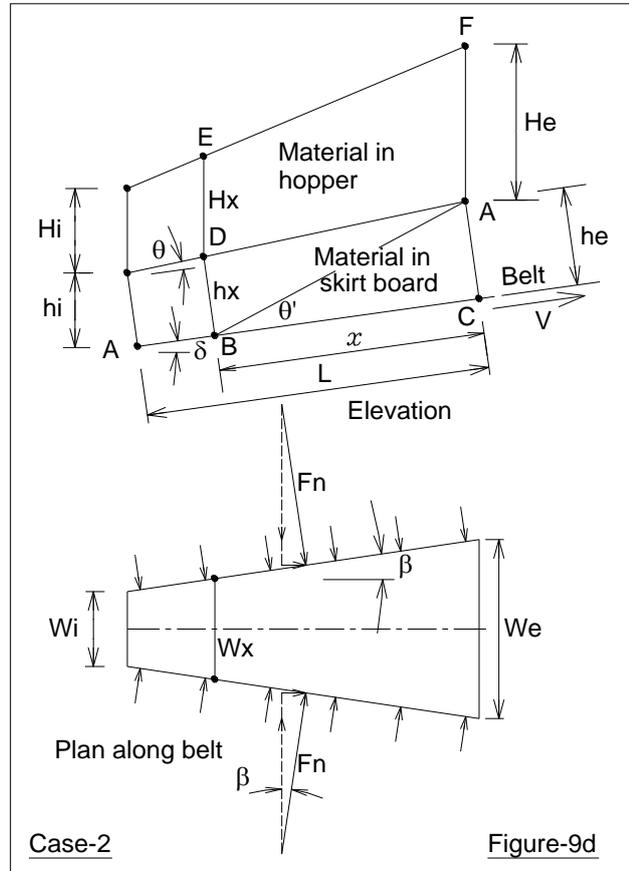
Figure-9d shows the skirt board elevation view. The belt feeder parameters are such that drag along bottom is unable to move full mass in skirt board. In this situation, the dragging force at bottom will disintegrate material body, creating its separation along line AB. The point-B will be located such that propelling forces sum is equal (somewhat greater) than the resistance to motion of material body ABC. The material outside of ABC will continuously add into active zone ABC. For the material body ABC; the dragging force in rear portion is sufficiently more compared to its resistance at rear side. So this more pushing force from rear will tend to keep the triangle intact for forward motion (i.e. it will avoid / reduce auxiliary shear lines within the said triangle). This analysis derives the formula to decide the plane of general shear, in applicable cases.

**Refer book for derivation of case-2.**

#### Example-8

Calculate shear plane location in feed zone of 1400 mm belt feeder of following data :

$W_e = 0.94 \text{ m}$ ,  $W_i = 0.687 \text{ m}$ ,  $h_e = 0.9 \text{ m}$ ,  $h_i = 0.79 \text{ m}$ ,  $C_2 = 4$ ,  $H_e = 0.94 \times 4 = 3.76 \text{ m}$ ,  
 $H_i = 0.687 \times 4 = 2.748 \text{ m}$ ,  $L = 5.5 \text{ m}$ ,  $\theta = 1.145763^\circ$ ,  $G_e = 0.02$ ,  $\beta = 1.31757^\circ$ ,  
 $G_p = 0.023$ ,  $\delta = 2^\circ$ ,  $\phi = 34^\circ$ ,  $\mu_s = 0.45$ ,  $\mu_b = \mu_m = 0.5914$ ,  $\gamma = 1000 \text{ kg/m}^3$ ,



Case-2

Figure-9d

$$Qd = 500 \text{ mtph}, \quad V = 0.22 \text{ mps}$$

The data have been intentionally selected so that calculation passes through different stages.  $\theta$  and  $\beta$  corresponds to adapter wall angle  $\alpha_1 \approx 22.5^\circ$  (i.e.  $67.5^\circ$  from horizontal).

### Solution

Checking whether general shear at interface.

$$Me = \gamma \cdot C_2 [\cos(\delta + \theta)] \cdot \frac{L}{\cos\theta} \cdot \left[ We^2 - 2 Gp \cdot We \cdot L + \frac{4}{3} Gp^2 \cdot L^2 \right]$$

$$Me = 1000 \times 4 (\cos 3.145763) \times \frac{5.5}{\cos 1.145763} \times \left[ 0.94^2 - 2 \times 0.023 \times 0.94 \times 5.5 + \frac{4}{3} \times 0.023^2 \times 5.5^2 \right]$$

$$= 14657 \text{ kg}$$

Material mass Ms in skirt board

$$Ms = \gamma \cdot [6 he \cdot We \cdot L - 3 (Ge \cdot We + 2 Gp \cdot he) \cdot L^2 + 4 Ge \cdot Gp \cdot L^3] \div 6$$

$$= 1000 \times [6 \times 0.9 \times 0.94 \times 5.5 - 3 \times (0.02 \times 0.94 + 2 \times 0.023 \times 0.9) \times 5.5^2 + 4 \times 0.02 \times 0.023 \times 5.5^3] \div 6$$

$$= 3793.5 \text{ kg}$$

$$F = Me \times 9.81 = 14657 \times 9.81 = 143785 \text{ N}$$

$$Fp1 = F \cdot [\cos(\delta + \theta)] \cdot \sin\theta = 143785 \times \cos 3.145763 \times \sin 1.145763 = 2871 \text{ N}$$

$$K = (1 - \sin\phi) \div (1 + \sin\phi) = (1 - \sin 34) \div (1 + \sin 34) = 0.2827$$

$$Fp2a = 0.25 \cdot K \cdot \gamma \cdot g \cdot hi \cdot Wi \cdot (hi + 2 \cdot C_2 \cdot Wi)$$

$$= 0.25 \times 0.2827 \times 1000 \times 9.81 \times 0.79 \times 0.687 \times (0.79 + 2 \times 4 \times 0.687) = 2366 \text{ N}$$

$$Fp2b = 0.25 K \cdot \gamma \cdot g \cdot L \cdot (2 he - Ge \cdot L) \cdot (2 \cdot he + 4 C_2 \cdot We - Ge \cdot L - 4 \cdot C_2 \cdot Gp \cdot L) \cdot \sin\beta$$

$$= 0.25 \times 0.2827 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.9 - 0.02 \times 5.5) \times (2 \times 0.9 + 4 \times 4 \times 0.94 - 0.02 \times 5.5 - 4 \times 4 \times 0.023 \times 5.5) \times \sin 1.31757$$

$$= 6444.42 \times 0.338148 = 2179 \text{ N}$$

$$Fp2 = 2366 + 2179 = 4545 \text{ N}$$

$$Fp3 = \mu_b \cdot F \cdot [\cos(\delta + \theta)] \cdot [\cos\theta + \mu_m \cdot \sin\theta] + \mu_b \cdot Ms \cdot g \cdot \cos\delta$$

$$Fp3 = 0.5914 \times 143785 \times [\cos 3.145763] \times [\cos 1.145763 + 0.5914 \times \sin 1.145763] + 0.5914 \times 3793.5 \times 9.81 \times \cos 2$$

$$= 84906.41 \times 1.011625697 + 21995.09 = 107888 \text{ N}$$

$$\text{Total propelling force } Fp = Fp1 + Fp2 + Fp3 = 2871 + 4545 + 107888 = 115304 \text{ N}$$

$$Fr1 = \mu_m \cdot F \cdot [\cos(\delta + \theta)] \cdot \cos\theta$$

$$= 0.5914 \times 143785 \times \cos 3.145763 \times \cos 1.145763$$

$$= 84889 \text{ N}$$

$$Fr2 = 0.25 \mu_s \cdot K \cdot \gamma \cdot g \cdot L \cdot (2 he - Ge \cdot L) \cdot (2 \cdot he + 4 C_2 \cdot We - Ge \cdot L - 4 \cdot C_2 \cdot Gp \cdot L)$$

$$= 0.25 \times 0.45 \times 0.2827 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.9 - 0.02 \times 5.5) \times (2 \times 0.9 + 4 \times 4 \times 0.94 - 0.02 \times 5.5 - 4 \times 4 \times 0.023 \times 5.5) = 42647 \text{ N}$$

$$Fr3 = Qd \cdot g \cdot hf \div (3.6 V)$$

$$hf = (0.5 \times 5.5) \sin 2 = 0.09597 \text{ m}$$

$$Fr3 = 500 \times 9.81 \times 0.09597 \div (3.6 \times 0.22) = 594 \text{ N}$$

$$\text{Total resistance } Fr = Fr1 + Fr2 + Fr3 = 84889 + 42647 + 594 = 128130 \text{ N}$$

Thus  $Fp < 1.07 Fr$ , and therefore shear plane is not at interface. Hence we have to try for shear plane by next stage calculation (i.e. Case-1).

### Checking for shear plane as per case-1

$\theta'$  maximum value =  $\tan^{-1}(h_e \div L) = 9.29^\circ$  When shear plane is passing at junction of belt and back plate of skirt-board.

The solution has been tried on computer. Accordingly when  $\theta' = 6.25^\circ$ ;  $F_p/F_r$  ratio is nearly 1.07 which is acceptable for solution. So, calculation are mentioned below for  $\theta' = 6.25^\circ$ .

$$\therefore Ge' = \tan\theta' = \tan 6.25 = 0.10952$$

$$M1 = \gamma \cdot L^2 \cdot (Ge' - Ge) \cdot (3 \cdot We - 4 \cdot Gp \cdot L) \div 6$$

$$= 1000 \times 5.5^2 \times (0.10952 - 0.02) \times (3 \times 0.94 - 4 \times 0.023 \times 5.5) \div 6 = 1044.35 \text{ kg}$$

$$Me = 14657 \text{ kg (same as earlier calculation).}$$

$$F' = (Me + M1) \times 9.81 = (14657 + 1044.35) \times 9.81 = 154030 \text{ N}$$

$$Fp1 = F' \cdot [\cos(\delta + \theta')] \cdot \sin\theta' = 154030 \times \cos 8.25 \times \sin 6.25 = 16595.65 \text{ N}$$

$$hi' = h_e - L \cdot \tan\theta' = 0.2976 \text{ m}$$

$$Wi' = Wi = 0.687 \text{ m}$$

$$Fp2a = 0.25 \cdot K \cdot \gamma \cdot g \cdot (hi' \cdot Wi') \cdot [2 \cdot C_2 \cdot (We - 2 \cdot Gp \cdot L) + h_e - Ge \cdot L + L \cdot (Ge' - Ge)]$$

$$= 0.25 \times 0.2827 \times 1000 \times 9.81 \times (0.2976 \times 0.687) \times [2 \times 4 \times (0.94 - 2 \times 0.023 \times 5.5) + 0.9 - 0.02 \times 5.5 + 5.5 \times (0.10952 - 0.02)] = 961.05 \text{ N}$$

$$Fp2b = 0.25 K \cdot \gamma \cdot g \cdot L \cdot [(2 h_e - Ge' \cdot L)] [2 h_e + 4 C_2 \cdot We - 2 \cdot Ge \cdot L + Ge' \cdot L - 4 C_2 \cdot Gp \cdot L] \cdot \sin\beta \text{ N}$$

$$= 0.25 \times 0.2827 \times 1000 \times 9.81 \times 5.5 [(2 \times 0.9 - 0.10952 \times 5.5)] \times [2 \times 0.9 + 4 \times 4 \times 0.94 - 2 \times 0.02 \times 5.5 + 0.10952 \times 5.5 - 4 \times 4 \times 0.023 \times 5.5] \times \sin 1.131757 = 1596 \text{ N}$$

$$Ms' = \gamma \cdot [6 \cdot h_e \cdot We \cdot L - 3 (Ge' \cdot We + 2 \cdot Gp \cdot h_e) \cdot L^2 + 4 \cdot Ge' \cdot Gp \cdot L^3] \div 6$$

$$= 1000 \times [6 \times 0.9 \times 0.94 \times 5.5 - 3 \times (0.10952 \times 0.94 + 2 \times 0.023 \times 0.9) \times 5^2 + 4 \times 0.10952 \times 0.023 \times 5^3] \div 6 = 2749 \text{ kg}$$

$$Fp3 = \mu_b \cdot F' \cdot [\cos(\delta + \theta')] \cdot [\cos\theta' + \mu_m \cdot \sin\theta'] + \mu_b \cdot Ms' \cdot g \cdot \cos\delta \text{ N}$$

$$= 0.5914 \times 154030 \times [\cos 8.25] \times [\cos 6.25 + 0.5914 \times \sin 6.25] + 0.5914 \times 2749.14 \times 9.81 \times \cos 2 = 111361 \text{ N}$$

$$Fr1 = \mu_m \cdot F' \cdot [\cos(\delta + \theta')] \cdot \cos\theta' \text{ N}$$

$$= \mu_m \cdot F' \cdot [\cos(\delta + \theta')] \cdot \cos\theta' = 0.5914 \times 154030 \times \cos 8.25 \times \cos 6.25 = 89617 \text{ N}$$

$$Fr2 = 0.25 \mu_s \cdot K \cdot \gamma \cdot g \cdot L \cdot [(2 h_e - Ge' \cdot L)] [2 h_e + 4 C_2 \cdot We - 2 \cdot Ge \cdot L + Ge' \cdot L - 4 C_2 \cdot Gp \cdot L] \text{ N}$$

$$= 0.25 \times 0.45 \times 0.2827 \times 1000 \times 9.81 \times 5.5 [(2 \times 0.9 - 0.10952 \times 5.5)] [2 \times 0.9 + 4 \times 4 \times 0.94 - 2 \times 0.02 \times 5.5 + 0.10952 \times 5.5 - 4 \times 4 \times 0.023 \times 5.5] = 31236 \text{ N}$$

$$Fr3 = Qd \cdot G \cdot hf \div (3.6 V) \text{ N}$$

$$hf = (0.5 \cdot L) \cdot \sin\delta = 0.5 \times 5.5 \times \sin 2 = 0.09597 \text{ m}$$

$$Fr3 = 500 \times 9.81 \times 0.09597 \div (3.6 \times 0.22) = 594 \text{ N}$$

$$Fp = Fp1 + Fp2a + Fp2b + Fp3 = 16595 + 961 + 1596 + 111361 = 130514 \text{ N}$$

$$Fr = Fr1 + Fr2 + Fr3 = 89617 + 31236 + 594 = 121447 \text{ N (1.07 Fr = 129948 N)}$$

Thus,  $F_p \geq 1.07 F_r$ . So, general shear can be considered at this angle. Thus shear is not interface at angle  $\theta=1.45763^\circ$  but at  $6.25^\circ$  and intersects back plate. Hence, it is not necessary to investigate in case-2.

# Chapter 11: BELT TRACTIVE PULL, POWER AND BELT TENSIONS

This chapter has 51 **pages**. Following 11 pages write-up is typical.

## **BELT TRACTIVE PULL, POWER AND BELT TENSIONS**

The earlier chapter-1 to chapter-10 have explained various phenomena occurring in belt feeder, and have also provided the design procedure to decide fundamental features of belt feeder. The information so generated is now adequate for designer to proceed with the design of remaining main parameters viz. belt tractive pull, power and belt tensions. This chapter discusses and defines the procedure to calculate these remaining main parameters, as appearing in title of this chapter.

The chapter firstly decides / sums-up various resistances and inherent propelling forces, to arrive at required tractive pull for operation of belt feeder. The tractive pull so calculated is utilised to calculate power and appropriate tensions in belt. In fact calculation of belt tensions is one of main aims in designing the belt feeder. Once the belt tensions are known, they enable to quickly design / decide pulley diameter, shaft diameter, pulley bearing size, take-up specifications and even sizing of belt feeder frame. Thus calculation of belt tensions is a culmination of design activity; because the same enable to decide specifications for apparently visible most of the items in belt feeder.

## **RESISTANCES**

### **Resistances grouping for calculation ease**

The belt motional / operational resistances have been calculated in following two groups. Although such grouping is not necessary for calculation of tractive pull and power, but same are needed for calculating belt tensions.

- Belt feeder carrying run resistance. This resistance can be further subdivided as resistances from feed zone and other resistances. The feed zone resistance constitutes the major portion of carrying run resistance. The carrying run resistances are described under clauses-11.1.3, 11.1.4, 11.1.5, 11.1.6, 11.1.7, 11.1.8, 11.1.9, 11.1.10, 11.1.11, 11.1.12 and 11.1.13 (summary).
- Belt feeder return run resistance. The magnitude of this resistance is small. The return run resistances are described under clauses.-11.2.1, 11.2.2, 11.2.3, 11.2.4, 11.2.5, 11.2.6 and 11.2.7 (summary)

The head pulley and tail pulley are at junction of carrying run and return run. Therefore, resistances at location of head pulley and tail pulley can be put either in carrying run or in return run. It is convenient to count these resistances as part of return run resistances. Therefore, the book considers the resistances at head pulley as well as tail pulley, as part of return run resistance. There is no advantage in dividing them as 50% for carrying and 50% for return, etc. Certain resistances which are very complicated in nature, have been already discussed along with their calculation procedure, in chapter-9. This chapter utilises the earlier formulae wherever applicable.

Unlike conveyor, the belt feeder also has some in-built propelling force, as discussed in chapter-9. These propelling forces are relatively of less magnitude. So their effect in pull / power is limited, but as mentioned in chapter-9, they tilt the forces balance toward favourable side, for proper movement of material in feed zone. These propelling forces with negative sign, are counted among resistances.

The other crucial point is the implication of actual shear plane on resistances within feed zone. The designer has two options, viz.

1. Just consider shear at interface and calculate resistances accordingly.
2. Decide theoretical shear plane as per chapter - 9 and make calculations for resistances based on this shear plane.

In case of first option, i.e. calculation made by assuming shear at interface, would have relative merit / demerit in comparison to actual conditions, as below.

Situation-1: The material is actually shearing at interface, and we are also calculating resistances considering material shear at interface. So no compromise in calculations.

Situation-2: The material shear is on plane, which is intersecting on back plate, as shown in figure-9c, page-285, chapter-9. In this situation, the overall net resistance (sum of shear resistance, skirt plates resistances, skirt plate reaction pushing force and pushing force on upper face) will be somewhat less than net resistance attributed to same items based on shear at interface. So, calculations will be on safer side, by reasonable magnitude most of the time. For this situation-2, the designer can safely opt for calculation based on shear at interface (i.e. situation-1).

Situation-3: The material shear is on plane which is intersecting belt, within feed zone, as shown in figure-9d, page-288, chapter-9. In this situation, net resistance (due to shear resistance, skirt plates resistances, skirt plates reaction pushing force and pushing force on upper face) will be less (by sufficient margin say up to 10%) than net resistance attributed to same items based on shear at interface. However, the shear along actual plane introduces one new / additional resistance directly to belt i.e. material rubbing on belt or material shear immediately above belt level, in portion rear of triangle tail. This would jack up the comparative value of resistance associated with actual shear plane. It appears that even in this situation-3, there would be tolerable difference between two results (i.e. calculation basis shear at interface versus calculation basis shear on actual plane). However, it is difficult to predict in a very specific way. So, calculation procedure (formulae) have been given for both the options. The situation-3 is mostly relevant to uniform cross section skirt board and long feed zone, where resistance based on actual shear plane, can need attention.

All resistances under this cl.-11.1.0 and its sub-clauses are for steady state operation (dynamic condition). This also means  $C_2$  value corresponds to material pressure at hopper outlet during flow condition.

The resistance during start-up phase is discussed under cl.-11.4.1 (11.4.0). This affects only few values / parameters of steady state resistance.

### **Carrying run resistance $R_c$ summary**

- Rsh : Material shear resistance
- Rsk1 : Skirt plates resistance, feed zone
- Rsk2 : Skirt plates resistance, beyond feed zone
- Rsk3 : Skirt rubber to belt resistance
- Rcc : Conveying resistance
- Rslc : Slope resistance
- Rpi : Force from interface
- Rpb : Force from skirt board back plate
- Rps : Force from skirt plates

The algebraic sum of above resistances, is the resistance Rc from carrying run, during operating, steady state.

### Return run resistance summary, Rr

- Rcr : Conveying resistance, return run  
 Rslr : Slope resistance, return run  
 Rce : External belt cleaner resistance  
 Rci : Internal belt cleaner resistance  
 Rw : Belt wrap resistance around pulleys  
 Rt : Pulley turning resistance

The algebraic sum of above resistance, is the resistance from return run during operation, steady state.

### Example -1

Calculate belt feeder tractive pull (during steady state), power (this is always for steady state), motor kW, belt tractive pull during starting and starting phase total time ts, Motor starting is DOL, without fluid coupling. The 1400 mm belt feeder particulars are as below (this is same as example-6, chapter-9, page-282).

$$\begin{aligned} &he = 0.82 \text{ m}, \quad hi = 0.27 \text{ m}, \quad He = 0.938 \times 3 = 2.81 \text{ m}, \quad Hi = 0.4 \times 3 = 1.2 \text{ m}, \quad We = 0.938 \text{ m} \\ &Wi = 0.4 \text{ m}, \quad \theta = 5.710593^\circ, \quad Ge = 0.1, \quad \beta = 2.8^\circ, \quad Gp = 0.0489, \quad L = 5.5 \text{ m}, \\ &\delta = 2^\circ, \quad C_2 = 3, \quad \phi = 36^\circ, \quad \mu_s = 0.423, \quad Qd = 480 \text{ mtph}, \quad \mu_b = \mu_m = 0.6346, \quad \gamma = 1000 \text{ kg/m}^3 \\ &\text{Belt velocity } V = 0.23 \text{ mps}, \quad L_1 = 10 \text{ m}, \quad L_2 = 6.25 \text{ m}, \quad L_{sk} = 3.5 \text{ m}, \quad h = 0.62 \text{ m} \\ &M_b = 30 \text{ kg/m}, \quad M_c = 150 \text{ kg/m}, \quad f = 0.04, \quad M_r = 15 \text{ kg/m} \end{aligned}$$

The  $C_2$  value during static status is 2.3, a case similar to rotary wagon tippler with steep hopper. The belt feeder is handling granular material. Select the drive as if with induction motor.

This belt feeder has been already checked for its shear plane (page-283 to 284). Accordingly, the material shear is at interface. Therefore, following calculations for tractive pull and power are on the basis of material shear at interface (situation-1).

### Solution :

#### Material shear resistance Rsh

$$\begin{aligned} Me &= \gamma \cdot C_2 \cdot \cos(\delta + \theta) \cdot \frac{L}{\cos \theta} \cdot \left[ We^2 - 2 \cdot Gp \cdot We \cdot L + \frac{4}{3} \cdot Gp^2 \cdot L^2 \right] \text{ kg} \\ &= 1000 \times 3 \times \cos(7.710593) \times \frac{5.5}{\cos 5.710593} \times \left[ 0.938^2 - 2 \times 0.0489 \times 0.938 \times 5.5 + \frac{4}{3} \times 0.0489^2 \times 5.5^2 \right] \end{aligned}$$

$$Me = 7752 \text{ kg}$$

$$\text{Gravity force } F = Me \cdot g = 7752 \times 9.81 = 76047 \text{ N}$$

$$R_{sh} = \mu_m \cdot F \cdot [\cos(\delta + \theta)] \cdot \cos \theta = 0.6346 \times 76047 \times [\cos 7.710593] \times \cos 5.710593 = 47586 \text{ N}$$

#### Skirt plate resistance Rsk1, feed zone

$$R_{sk1} = 0.25 \mu_s \cdot K \cdot \gamma \cdot g \cdot L \cdot (2 \cdot he - Ge \cdot L) \cdot (2 \cdot he + 4 \cdot C_2 \cdot We - Ge \cdot L - 4 \cdot C_2 \cdot Gp \cdot L) \text{ N}$$

$$K = (1 - \sin 36) \div (1 + \sin 36) = 0.2596$$

$$R_{sk1} = 0.25 \times 0.423 \times 0.2596 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.82 - 0.1 \times 5.5) \times (2 \times 0.82 + 4 \times 3 \times 0.938 - 0.1 \times 5.5 - 4 \times 3 \times 0.0489 \times 5.5) = 14722 \text{ N}$$

#### Skirt plates resistance Rsk2, beyond feed zone

$$R_{sk2} = \mu_s \cdot K \cdot \gamma \cdot g \cdot h^2 \cdot L_{sk} \text{ N}$$

$$R_{sk2} = 0.423 \times 0.2596 \times 1000 \times 9.81 \times 0.62^2 \times 3.5 = 1449 \text{ N}$$

### Skirt rubber to belt resistance, Rsk3

$$Rsk3 = 90 \times 9 = 810 \text{ N}$$

### Conveying resistance carrying run, Rcc

$$Ms = \gamma \cdot [6 \text{ he} \cdot \text{We} \cdot L - 3 (\text{Ge} \cdot \text{We} + 2 \text{Gp} \cdot \text{he}) \cdot L^2 + 4 \text{Ge} \cdot \text{Gp} \cdot L^3] \div 6 \text{ kg}$$
$$= 1000 \times [6 \times 0.82 \times 0.938 \times 5.5 - 3 \times (0.1 \times 0.938 + 2 \times 0.0489 \times 0.82) \times 5.5^2 + 4 \times 0.1 \times 0.0489 \times 5.5^3] \div 6$$

$$Ms = 2141 \text{ Kg}$$

$$Me = 7752 \text{ kg (as calculated for material shear resistance Rsh, in the beginning of the solution)}$$

$$Mm = Qd \div (3.6 V) = 480 \div (3.6 \times 0.23) = 579.7 \text{ kg/m}$$

$$Rcc = [Ms + Me + Mb \cdot L_1 + Mc \cdot L_1 + Mm (L_1 - L - 0.5)] \cdot f \cdot g \text{ N}$$
$$= [2141 + 7752 + 30 \times 10 + 150 \times 10 + 579.7 \times (10 - 5.5 - 0.5)] \times 0.04 \times 9.81$$

$$Rcc = 5498 \text{ N}$$

### Slope resistance carrying run, Rslc

$$Rslc = Mb \cdot L_1 \cdot g \cdot \sin\delta + Mm \cdot L_2 \cdot g \cdot \sin\delta \text{ N}$$
$$= 30 \times 10 \times 9.81 \times \sin 2 + 579.7 \times 6.25 \times 9.81 \times \sin 2 = 1343 \text{ N}$$

### The force from interface, Rpi

$$F = Me \cdot g$$

$$Me = 7752 \text{ kg (as calculated for material shear resistance Rsh, in the beginning of the solution)}$$

$$F = 7752 \times 9.81 = 76047 \text{ N}$$

$$Rpi = - F \cdot [\cos(\delta + \theta)] \cdot \sin\theta \text{ N}$$
$$= - 76047 \times [\cos(7.710593)] \times \sin 5.710593 = -7498 \text{ N}$$

### Force from back plate, Rpb

$$Rpb = - 0.25 \cdot K \cdot \gamma \cdot g \cdot hi \cdot Wi \cdot (hi + 2 \cdot C_2 \cdot Wi) \text{ N}$$
$$= - 0.25 \times 0.2596 \times 1000 \times 9.81 \times 0.27 \times 0.4 \times (0.27 + 2 \times 3 \times 0.4) = -183 \text{ N}$$

### Force from skirt plates, Rps

$$Rps = - 0.25 K \cdot \gamma \cdot g \cdot L \cdot (2 \text{ he} - \text{Ge} \cdot L) \cdot (2 \cdot \text{he} + 4 C_2 \cdot \text{We} - \text{Ge} \cdot L - 4 \cdot C_2 \cdot \text{Gp} \cdot L) \cdot \sin\beta \text{ N}$$
$$= - 0.25 \times 0.2596 \times 1000 \times 9.81 \times 5.5 \times (2 \times 0.82 - 0.1 \times 5.5) \times (2 \times 0.82 + 4 \times 3 \times 0.938 - 0.1 \times 5.5 - 4 \times 3 \times 0.0489 \times 5.5) \times \sin 2.8$$
$$= - 1700 \text{ N}$$

### Carrying run resistance Rc summary

$$Rsh = 47586 \text{ N}$$

$$Rsk1 = 14722 \text{ N}$$

$$Rsk2 = 1449 \text{ N}$$

$$Rsk3 = 810 \text{ N}$$

$$Rcc = 5498 \text{ N}$$

$$Rslc = 1343 \text{ N}$$

$$Rpi = -7498 \text{ N}$$

$$Rpb = -183 \text{ N}$$

$$Rps = -1700 \text{ N}$$

$$\text{Total} = 62027 \text{ N} \quad \text{This is total resistance of carrying run.}$$

### Conveying resistance, return run, Rcr

$$Rcr = f \cdot g \cdot L_1 \cdot (Mb + Mr) = 0.04 \times 9.81 \times 10 \times (30 + 15) = 177 \text{ N}$$

### Slope resistance, return run, Rslr

$$R_{slr} = - M_b \cdot L_1 \cdot g \cdot \sin \delta = - 30 \times 10 \times 9.81 \times \sin 2 = -103 \text{ N}$$

External belt cleaner resistance, Rce

The input data are,  $\mu_e = 0.6$ ,  $A_e = 0.0448 \text{ m}^2$ ,  $P_e = 50000 \text{ N/m}^2$

$$R_{ce} = \mu_e \cdot A_e \cdot P_e = 0.6 \times 0.0448 \times 50000 = 1344 \text{ N}$$

Internal belt cleaner resistance

The input data are,  $\mu_i = 0.6$ ,  $A_i = 0.0336 \text{ m}^2$ ,  $P_i = 50000 \text{ N/m}^2$

$$R_{ci} = \mu_i \cdot A_i \cdot P_i = 0.6 \times 0.0336 \times 50000 = 1008 \text{ N}$$

Belt wrap resistance around pulleys, R<sub>w</sub>

The calculation of wrap resistance and pulley turning resistance requires belt tensions, pulley diameter, shaft diameter at bearings, which are not known at this stage. Actually this exercise is to find these values. So, presently, sum up all resistances without R<sub>w</sub> and R<sub>t</sub>.

$$\text{All resistances (without R}_w \text{ and R}_t) = 62027 + 177 - 103 + 1344 + 1008 = 64453 \text{ N}$$

Make approximate (or actual) design using this value of resistance and decide tension, pulley diameter and shaft diameter at bearings.

Here approximate method is followed as an additional information to reader. Consider drive factor 0.5,  $T_1 = 1.5 \times 64453 = 96679 \text{ N}$ ,  $T_2 = 0.5 \times 64453 = 32226 \text{ N}$ .

At this stage consider both the values approximately 10% more. The values of R<sub>w</sub> and R<sub>t</sub> are small, and such consideration does not make much difference in total resistance. Accordingly,

$$F_{b1} = 0.5 (T_1 + T_2) = 0.5 (1.1 \times 96679 + 1.1 \times 32226) = 70898 \text{ N}$$

$$F_{b2} = 1.1 \times 32226 = 35449 \text{ N}$$

Also, tentative belt could be 1400 mm EP 800 / 4, covers 10 & 5 mm, grade M24. This belt total thickness is approximately 20 mm. Pulley diameters are (650 + 2x12 RL) mm, (500 + 2x10 RL) mm and (400 + 2x10 RL) mm. The shaft diameters at bearings are likely to be 150 mm and 120 mm tentative. After making final design these resistances are recalculated, along with their implication on total resistance (which would be of small magnitude). That is to say first stage design output will become input to final design.

The input data for this calculation are :

$$t = 20 \text{ mm}, \quad F_{b1} = 70898 \text{ N}, \quad F_{b2} = 35449 \text{ N}, \quad N_2 = 2, \quad \text{Textile fabric belt.}$$

$$R_w = 0.009 B \cdot t \cdot \left[ 140 + \frac{10 F_{b1}}{B} \right] \div D_1 + 0.009 B \cdot t \cdot \left[ 140 + \frac{10 F_{b2}}{B} \right] \cdot N_2 \div D_2$$

$$= 0.009 \times 1400 \times 20 \times \left[ 140 + \frac{10 \times 70898}{1400} \right] \div 674 + 0.009 \times 1400 \times 20 \times \left[ 140 + \frac{10 \times 35449}{1400} \right] \times 2 \div 520$$

$$R_w = 623 \text{ N}$$

Pulley turning resistance, R<sub>t</sub>

$$R_t = 0.005 \times (2 \cdot F_{b2}) \times d_2 \times N_2 \div D_2 = 0.005 \times (2 \times 35449) \times 120 \times 2 \div 520 = 163 \text{ N}$$

Return run resistance summary, R<sub>r</sub>

$$R_r = R_{cr} + R_{slr} + R_{ce} + R_{ci} + R_w + R_t = 177 - 103 + 1344 + 1008 + 623 + 163 = 3212 \text{ N}$$

$$R_f = R_c + R_r = 62027 + 3212 = 65239 \text{ N}$$

$$\text{Power at drive pulley periphery, } p_{k1} = P \cdot V \div 1000 = 65239 \times 0.23 \div 1000 = 15 \text{ kW}$$

$$\text{Power required at motor shaft, } p_{k2} = p_{k1} \div \eta = 15 \div 0.9 = 16.67 \text{ kW (considering drive efficiency 90\%)}$$

$$\text{Belt feeder torque at drive pulley rim, steady settled speed} = P \cdot D_1 \div (1000 \times 2) = 65239 \times 674 \div (1000 \times 2) = 21985 \text{ Nm}$$

Belt feeder torque  $T_{Qm}$  at motor shaft, steady settled speed =  $21985 \div (\eta \cdot i)$  Nm =  $21985 \div (0.9 \times 112)$  = 218.1 Nm, drive efficiency and gear box ratio as mentioned below.

#### Drive selection.

The drive pulley diameter is  $650 + 2 \times 12 = 674$  mm, as mentioned above. The drive system total speed reduction would be  $i = 112$  based on 720 rpm motor and 674 mm diameter drive pulley, to get belt speed of nearly 0.23 mps. The totally enclosed gear box along with flexible coupling at input shaft and flexible coupling at output shaft, have been considered for total speed reduction ratio of 112. One can also use geared motor, if same is available with electrical motor of required specifications. This would eliminate input coupling.

Starting state :

Here  $C_2$  static is less than  $C_2$  dynamic. Hence  $R_{fsw} \geq 1.6 R_f$ .

$R_{fsw} = 1.6 \times 65239 = 104382$  N

Therefore required starting torque at feeder shaft =  $104382 \times (0.5 \times 0.674) = 35176$  Nm.

Required starting torque at motor shaft =  $35176 \div (112 \times 0.9) = 348.9$  Nm

Choose the drive motor which has stalled (zero speed) torque and pull-up torque at least 30% more than the above value 348.9 Nm

Chosen motor say 22.4 kW

This motor's rated torque =  $22.4 \times 9555 \div 720 = 297.26$  Nm

This is greater than the required steady speed torque

This motor pull-up torque and stalled (zero speed) torque should be  $\geq 297.26 \times 1.3 = 387$  Nm. It seems the regularly available motor will have stalled torque and pull-up torque suitable for this. Nema-C type motor can have it as high as 75%, although it is not necessary to have such a torque.

#### **TAKE-UP**

Belt feeder includes take-up device to maintain proper tension in belt. The 'proper' tension implies 'minimum' tension to fulfill all the functional needs such as:-

- Adequate tension to transmit mechanical power from drive pulley to belt in all operating conditions, by well known relation  $T_1 / T_2 \leq e^{\mu\theta}$
- Adequate tension to limit sag of belt between idlers, within allowable limit so that material leakage between belt and skirt board is of acceptable level such that it does not spill from belt, but gets conveyed for discharge at head pulley.

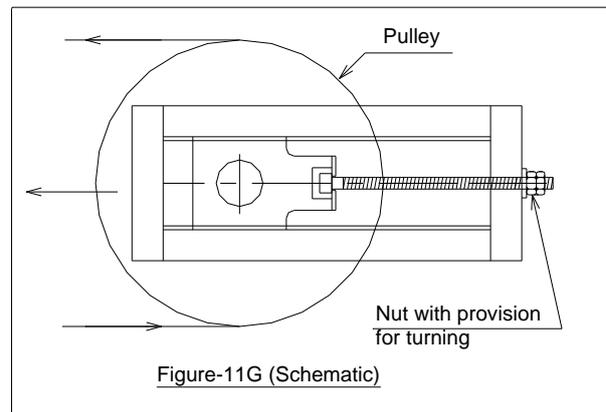
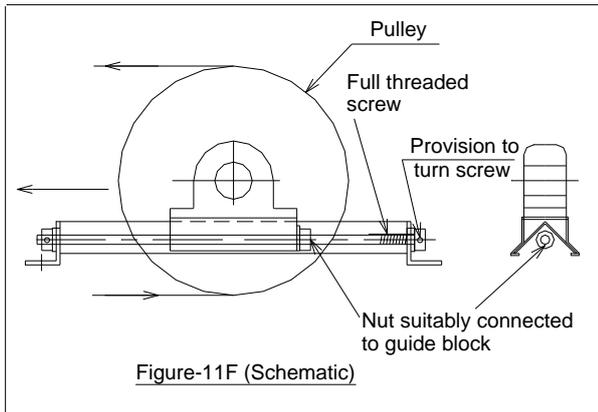
If the tension is more than the necessary, it will result in costlier belt, pulleys and terminal structures. So, the designer always decides minimum tension to suit above requirements. Constructionally 3 types of take-ups viz. screw take-up (plain), screw take-up with hydraulic tensioner and horizontal gravity take-up at tail end can be used. Functionally, these take-up devices can be grouped in two types viz. 'fixed take-up pulley type' and 'floating take-up pulley type'. The reader may wonder with the mention of gravity take-up at tail end, but this has been discussed for possibility of its use in context of modern day high capacity and heavy-duty belt feeders.

#### **Take-up types**

Following is the information about the different types take-up, applicable to belt feeders:

### Screw take-up (simple)

Simple screw take-up suits very well to light-duty belt feeders. This is the most economical type of take-up device because it is simple mechanism and is extensively used. The take-up device is shown in figure-11F and figure-11G, and is generally installed with tail pulley, which also acts as take-up pulley.



The device includes 2 numbers of take-up screw with nut in suitable form. In one arrangement screw remains at same location, and turning of the screw shifts nut. The take-up pulley plummer block is mounted on guide which is attached to the nut. The nut movement carries pulley with it for tightening the belt. Such screw-nut are mounted under angle-frame for protection against spilled material; and therefore are known as protected screw take-up device. The advantage of such take-up device is the use of standard plummer block for pulley support, and protection of screw-nut from spilled material, and suitability for installation on regular tail terminal.

The other arrangement includes shifting screw. The turning of nut shifts the screw. The screw end is connected with special shaped plummer block moving in guides. Such arrangement has screws and pulley centre-line in same plane for transfer of belt force to screw without tilting-movement. Thus the arrangement is more robust from design consideration. However it requires special type of plummer block which increases the inventory.

In the aforesaid arrangements, both side screws are operated alternatively in short step movement. The belt tightening is by judgement according to skill of the maintenance personnel. Such screw take-ups with manual tightening are commonly used for average duty feeders, in consideration to economy and simplicity. The author does not recommend use of such take-up for heavy or important class belt feeder where specific tension is must for proper functioning of belt feeder. The specific tension can not be achieved by manual judgement.

### Screw take-up with hydraulic tensioner

The screw take-up device with hydraulic tensioner is recommended for medium to heavy class feeders. In this arrangement, portable cylinder piston assembly is attached between pulley-guide-block and conveyer structure, at each side. The nuts (or holding devices) are loosened to permit free movement of guide-blocks. Hydraulic hand-pump (simultaneous action to both cylinders) is used to generate necessary oil pressure for desired take-up force. The pulley shifts to new position by hydraulic thrust, where it is locked by nuts on screws. Subsequently, the hydraulic attachments are removed. Such hydraulic tensioner device is in effect a maintenance device / tool. This type of take-up feature can mostly fit to arrangement similar to figure-11G or its appropriate modification.

The other alternative option is to have load cells appropriately placed at tail end, and use their reading while tightening the take-up screw (of earlier title).

All the screw take-up devices are functionally 'constant belt length take-up' i.e. take-up pulley does not shift during feeder operation. This means belt length remains constant whether the feeder is running at steady speed, starting or stoppage.

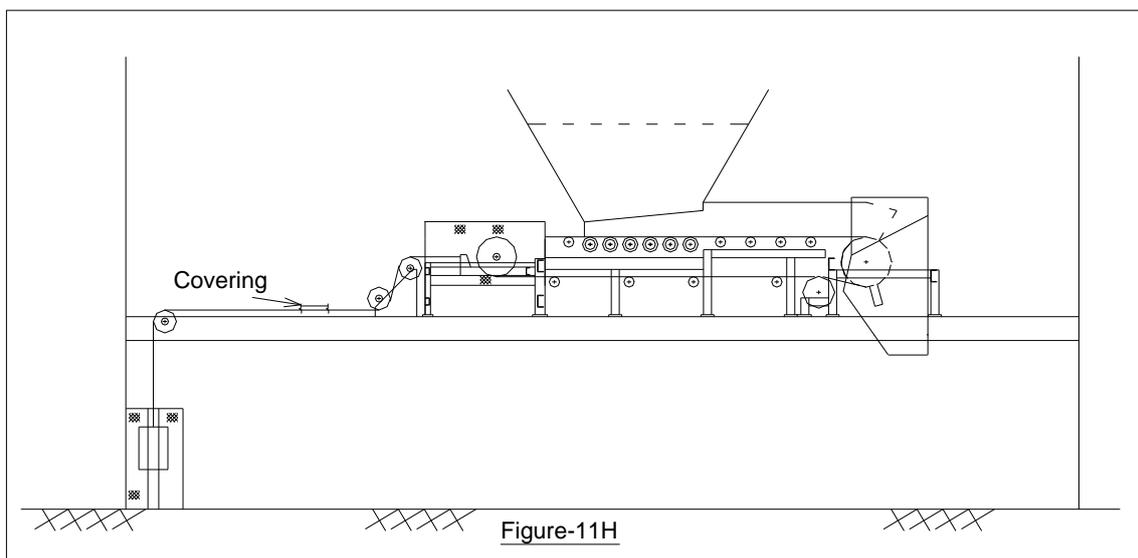
Screw take-up creates tension in belt by stretching the belt. The belt elongates after certain use, which results into reduced tension. This would require stretching (i.e. re-tightening) to restore the tension. The belt needs periodic re-tightening to maintain same value of tension. The new belt needs tightening after short time use, but subsequently such necessity arises after prolonged time interval. The belt has two types of stretches viz. permanent elongation and elastic elongation. The periodic resetting arises due to permanent elongation which is more initially but it diminishes with time.

### Horizontal gravity take-up

As of now this arrangement has been rarely used for belt feeder. Because in general the importance / necessity for presence of appropriate tension in belt feeder, has not received adequate attention (as an average situation). The usual difficulty associated with belt feeder such as material leakage, etc. are consequence of improper tension instead of just focussing on peripheral issues. The advantages of the gravity take-up are: (1) It provides assured value of take-up force at all the times. (2) The take-up device is maintenance free to apply needed force. (3) Take-up force is not effected by belt stretch (within the operating stroke). Also, thermal expansion / contraction of belt does not effect tension. This is due to floating nature of take-up pulley.

The disadvantages of such take-up are: (1) If the belt snaps, the sliding unit and counter weight will hit the barrier. (2) The slackening of belt is difficult compared to non-gravity take-up. (3) It needs more space and special precaution to make it hazard-free for the belt feeder installation, which is often in a constrained space unlike conveyor.

The designer to choose the type of take-up appropriate to the application. Simple screw take-up to be used where it can suit, and general tendency for same to be restricted. The screw take-up with hydraulic tensioner or load cell, will have satisfactory performance, but needs periodic checking and resetting for restoration of belt tension. As against this, gravity take-up will attend itself for the tension, but required space for its installation and to make it hazard-free is to be examined by designer.

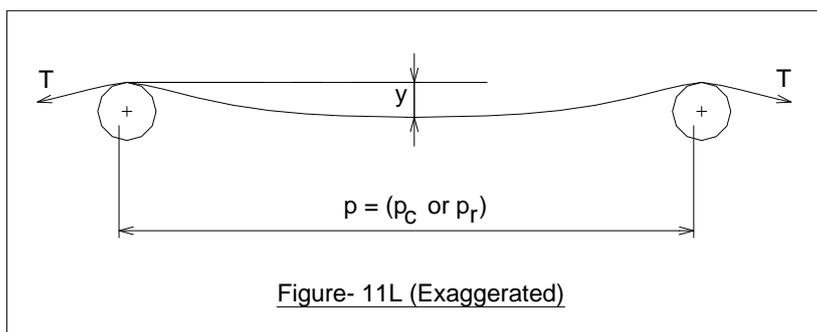


The belt feeder take-up stroke is very small compared to conveyor. Therefore such take-up do not need wheel-fitted travelling carriage for mounting tail (take-up) pulley. The take-up pulley mounted on a frame directly sliding in steel fabricated guides, is adequate. Also, its vertical counterweight will be moving within small tower located at suitable place. The wire rope connection between sliding frame and counterweight should pass in concealed fashion on floor, etc. The counterweight assembly should be just above the ground or barrier so that if belt snaps, the counterweight frame should first hit the barrier instead of sliding frame hitting its barrier. This can be achieved by keeping vertical sliding stroke somewhat less than the stroke provided for horizontal slide frame. Also, while making the wire rope connection, keep the pulley frame location to the extreme inward (head pulley side) position. This would avoid possibility of tail end breakage and injury to attending personnel, in the event of belt snapping.

**The aforesaid features are must to make it hazard-free.** The probable arrangement is shown schematically in figure-11H. The author has discussed this type of arrangement to draw the attention for probability of use and the designer can examine for its suitability in context of the situation.

### Minimum tension in belt to limit sag

In case of belt conveyor, the sagging of belt between idlers affects the conveying friction coefficient and thereby belt tension and complete design of conveyer. Therefore, conveyer is designed keeping belt sag within specific limit (Here the belt sag to be understood as sag of belt along with material, wherever it is applicable). The



sagging of belt is equally objectionable in belt feeder; but main reason is material leakage and more wear of belt and sealing rubber, due to abrasive material acting like emery powder between rubbing surfaces. The belt feeder sag issue is very important for belt feeder, but at the same time it is quite complex for decision. Figure-11L shows the sag of belt between two idlers (exaggerated).

This sag will be zero if belt tension is infinite or if the weight (of belt + material) is zero. None of these conditions are feasible, and hence, belt sag can not be avoided (even if it is not visible). This sag occurs due to earth gravity and spaced location of idlers. Common observations indicate that the sag will increase with increase in idler pitch and belt weight, but it will decrease with the increase in tension.

### Sag formula

The mathematical standard formula for the sag, indicating the relationship between these parameters, is as mentioned hereunder.

$y$  = Belt sag numerical value, m

$p$  = Idler pitch (this could be carrying idler pitch  $p_c$  or return idler pitch  $p_r$ , at point of analysis), m

$g$  = Gravity acceleration value,  $m/sec^2$

$M$  = Belt + material mass,  $kg/m$  (the calculation for  $M$  is mentioned subsequent to formula).

$T$  = Belt tension at this location, N       $Sag\% = 100 y \div p$        $\gamma$  = Material bulk density,  $kg / m^3$

$C_2$  : (Material column equivalent height above interface)  $\div$  (skirt board width at point of analysis).

Qd = Design capacity, mtpm

V = Belt speed, mps (also small v)

Mb = Belt mass, kg/ m

Ge = Skirt board elevation gradient,  $Ge = \tan \theta$

Gp = Skirt board gradient in plan,  $Gp = \tan \beta$

$T = 12.5 M \cdot g \cdot p \div (\text{sag} \%)$       N

Alternatively,  $(\text{sag}\%) = 12.5 M \cdot g \cdot p \div T$

The first formula can be used to decide required tension from selected value of sag%.

The alternative formula can be used to decide sag % that would occur for known value of tension.

The value of M to be used in this equation is as below:

For portion beyond feed zone

Generally the belt tension will be comparatively more, and the value of M will be less in this zone, compared to feed zone. Hence, this calculation will show idler pitch more than feed zone, but it is beneficial to keep it less, say within 325 mm..

$Mm = Qd \div (3.6 v)$       kg/ m, this is material mass per metre.

$M = Mm + Mb$       kg/m

For feed zone portion

Suppose belt sag condition is to be analysed at a distance  $x$  from exit end.

Skirt board width,  $W_1$  at that point =  $We - 2 Gp \cdot x$

Skirt board height,  $h_1$  at that point =  $he - Ge \cdot x$

Material column equivalent height at  $H_1 = C_2 \cdot W_1$

$M = \gamma \cdot W_1 \cdot (h_1 + H_1) \cdot x + Mb = \gamma \cdot W_1 \cdot (h_1 + H_1) + Mb = \gamma \cdot W_1 \cdot h_1 + \gamma \cdot C_2 \cdot W_1^2 + Mb$       kg/ m

For return run

For return run this is simply belt mass kg/m. Hence  $M = Mb$  kg/m.

### **Magnitude of Sag**

The sag value is simply 1 % for return run. The carrying run has to hold material from feed zone to discharge pulley, but material at feed zone is under more pressure. Therefore, sag value (numerical value in mm) selected for feed zone is also used for portion beyond feed zone. The sag value for feed zone is discussed here, and it relates to following issues.

- The locations (or points), which are to be chosen for sag analysis.
- The allowable sag at these locations (or points).

For the belt feeder of expanding cross section, the M value increases as we advance from rear side to exit side of feed zone. But belt tension also increases as we advance towards exit side of feed zone. If the skirt board expansion gradients  $Ge$  and  $Gp$  are sufficiently large, the feed zone exit end condition would be mostly governing. However, if these gradients are not adequate, then the situation at rear end could be governing. For the skirt board of uniform cross section, the sag condition at the rear end of feed zone would be governing (worst). The designer is to see the acceptability of leakage gap at both the ends, possibly for a compromise decision. After all, aggregate leakage from entire feed zone matters, and not the leakage at critical or worst point.

The allowable sag depends upon fineness of material, feed zone length, material pressure and also to some extent abrasiveness of the material as below:

- The leakage is more for finer material, i.e. allowable sag will be comparatively less for finer material.

- The leakage material is to be accommodated by belt, prior to its spillage. This material increases with feed zone length. Thus comparatively less sag is to be considered for longer length of feed zone.
- The material under high pressure would tend to force its way through gap. So comparatively less sag is preferred, when dealing with deep hopper imposing high pressure of material
- Comparatively less sag would be better for more abrasive material.
- Comparatively less sag for narrow belt, which has less margin at belt edge to hold material.

The sag value to be chosen is subjective. The designer can use his experience in dealing with different types of materials. The sag % value is directly linked to idler pitch. For the belt feeder, it is the **numerical value of sag (mm) that matters and not the sag %**.

Again the sag value is to be correlated with the actual gap (maximum at centre of pitch distance). The belt sag profile vary up-down continuously during operation, in tune with variation in vertical force (i.e. variation in level of material in hopper). This prevents creation of zero gap between skirt rubber and belt, even though skirt rubber tends to acquire it by its wear. The actual gap between skirt rubber and belt can be considered about 75% of sag value used in calculation. Thus for example, if idler pitch is 250 mm and sag is 1%, then the gap is likely to be  $2.5 \times 0.75 = 1.875$  mm. The designer is to see the acceptability of the gap so calculated. The foregoing information / explanation helps to understand the applicable technical issues. The author suggests to adopt following approach for technical calculation and decision:

- For usual belt feeder, avoid using pitch more than 250 mm under feed zone, even if sag (gap) condition allows it to be more. The improved performance from this would be more than additional cost of few idlers.
- If need be, use the idler pitch closest to roller diameter, just keeping about 20 to 25 mm gap between rollers. The calculation for belt feeder under high pressure can often lead to such requirement. If the rollers are mounted on idler frame; the frame base to be formed by angle piece welded at transom end, instead of base plate under transom. This would avoid base length greater than roller diameter.
- In general, belt feeder does not deal with very large lumps, continuously falling from great height. So, roller diameter less than 200 mm and closer pitch could be possible, when needed. If the closer pitch is not possible and material pressure is high; then higher tension in belt would be required. This means costlier belt, pulleys, bearings and drive.
- In a heavy class belt feeder, vertical force on belt can be tonne / metre rather than kgf / m, under feed zone. The rolling support provides wear free surface to the belt.

It seems that the actual gap of 5 mm between skirt rubber and belt can be used depending upon the material, belt width, feed zone length and belt feeder length. If the idler pitch is 200 mm, then the above implies 2.5% sag. If the idler pitch is 250 mm, then above implies sag value of 2%. This is just a typical method for calculation. Some time it could be very expensive to restrict actual gap of 5 mm. In such circumstances, the designer can use higher value, say up to 6 to 10 mm, judging the need/ suitability for application. This implies 3% and 4% sag with respect to 200 mm pitch idler. The lesser magnitude of sag is better because it implies less leakage between skirt rubber and belt.

## Chapter 13: TRANSITION DISTANCE

This chapter has 5 pages. Following 5 pages write-up is typical.

### TRANSITION DISTANCE

The belt feeder carrying run will be of troughed type, if the belt feeder is equipped with picking type idler or 3-roll

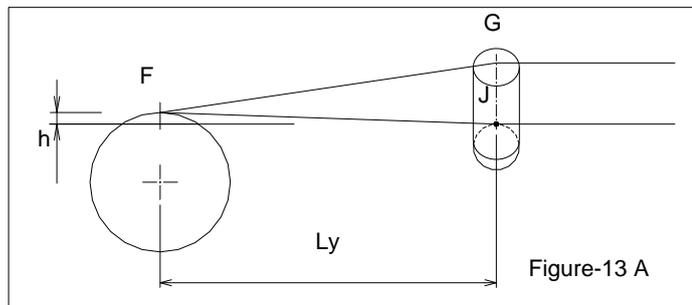
troughing idlers. In such belt feeder; the belt is flat when on pulley, but it acquires trough shape when being on idler. The change of profile from flat to trough OR trough to flat results into additional strain / stress in belt. The change of this profile is done gradually so that additional stress strain remains within tolerable / allowable limit, to prevent damage to belt and also to have workable belt feeder. In effect, this requires certain minimum distance along feeder, for transformation of belt from flat to trough (or trough to flat), safely without damage to belt carcass. This chapter describes the design procedure to calculate this minimum distance which is called 'minimum transition distance'. Figure-13A shows the belt profile in transition zone. The transition distance being used should be greater than or equal to this 'minimum transition distance'.

Generally, the transition distance used is near to minimum, because excess distance can have disadvantages such as (1) Increase in centre to centre length of belt feeder. (2) Difficulty to accommodate within available space. (3) Longer length of special shape skirt-edges (for 3-equal roll trough idlers) matching to transition distance, at discharge end.

The designer can always use transition distance more than minimum if layout and available space permit the same. The transition distance issue is more severe in case of belt conveyors, due to deep troughing angles. The belt feeders troughing angles are comparatively less, and thereby would pose less difficulty in providing the required transition distance. This chapter is not applicable to flat belt feeder.

### BELT STRESS - STRAIN AND BEHAVIOUR IN TRANSITION ZONE

Figure-13A shows the transition zone. The figure shows pulley top point location raised up by distance  $h$ , compared to the line touching the top of central rollers in this zone (reference level of belt). The belt rise  $h$  is shown in figure, because it is part of standard (comprehensive) formula applicable to conveyors as well as belt feeders. However, the belt rise does **not** suit belt feeder (if there is feeding in transition zone) and it should be taken zero or almost zero. As can be seen in this figure, the geometric dimension  $FG$  is larger than  $Ly$  (or  $FJ$ ). The belt same segment when not on transition zone, will have  $FG = Ly$ . This implies the belt outward portion (towards edges) is getting stretched accompanied by reduction in safety factor in this part of the belt. This is shown in figure-13B.

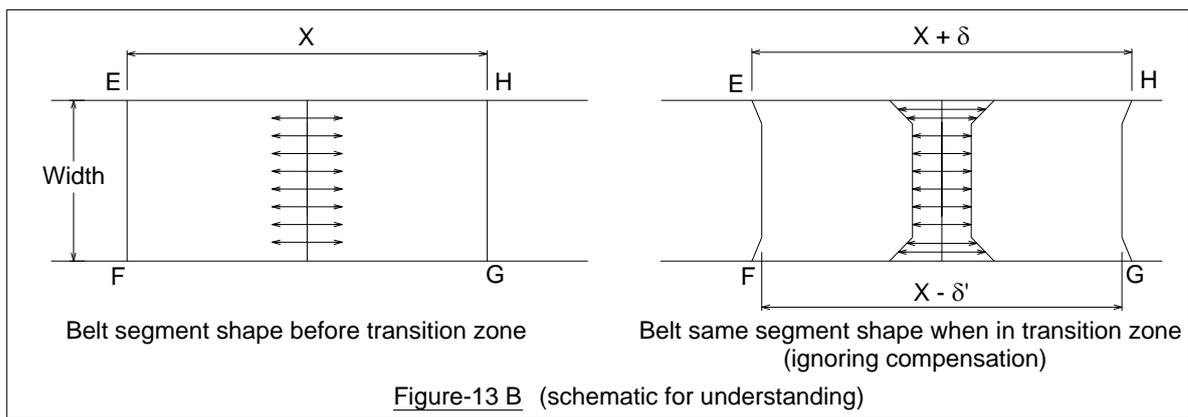


In reality, the belt segment has to create dimensional difference between edges and central portion, when it is forced to pass through transition zone. The edge stretch also creates compressive load (stress) in middle portion, along X and Y directions due to force reaction in the carcass. The belt was under uniform longitudinal tensile stress before transition zone. However when it is passing through transition zone, the side portions are subjected to elongation strain at edges, which adds in to earlier tensile stress. The belt middle portion was also under identical tensile stress, but now it gets superimposed by compressive stress. So, the middle portion will have effective tensile stress less than the original, as far as longitudinal direction is concerned. In addition, belt is also subjected to compressive stress along transverse direction due to belt tendency to slide down on side rollers due to bow - string effect. The situation will result into belt buckling in middle portion of segment i.e. belt fold-up (or fold-up tendency) will appear in this zone, if transition distance is not adequate in relation to prevailing

tensions in the belt. Thus, transition distance depends upon carcass particulars and prevailing tensions in the belt. The transition distance should be sufficiently large so that :

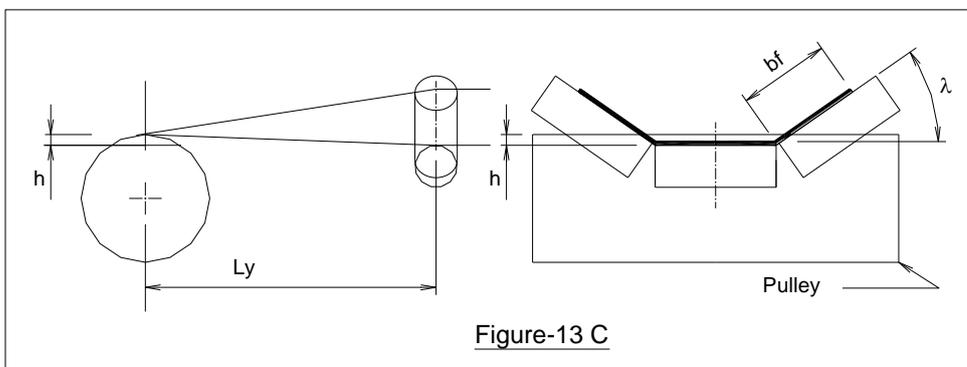
- Belt edges stretching should not cross the allowable limit (lower than yield condition, by adequate margin during life of belt).
- Belt central portion should not buckle or fold-up (lower than fold-up limiting value by adequate margin during life of belt).

The calculations for required transition distance cannot be done purely on theoretical basis. This requires extensive testing for three-dimensional behaviour of 'hollow' belt, which can best be done by belt manufacturer who will have very large number of samples as needed for such tests. The design procedure has been reproduced here from Author's book "Engineering Science and Application Design for Belt Conveyors", which is on the basis of published data of M/s ContiTech Germany, with their kind permission for the said book. One can also refer to the article by D Beckmann and Rainer Alles on this subject.



**NOMENCLATURE**

- B: Belt width, mm
- b<sub>f</sub>: Belt portion length on side roller, mm (refer figure-13C)



- $\lambda$ : Troughing angle, **degree** (refer figure-13C).
- T<sub>x</sub>: Belt tension in N, at point of analysis, steady state
- T<sub>xm</sub>: Belt tension in N, at point of analysis, momentary state
- T<sub>uj</sub>: Belt joint unit strength, N/mm (This is equal to nominal unit strength x joint efficiency. For example EP800 with joint efficiency 0.75, T<sub>uj</sub> = 800 x 0.75 = 600 N/mm)

$S_x$  : Steady state existing safety factor at point of analysis,  $S_x = \frac{T_{uj}}{\frac{T_x}{B}}$

$S_{xm}$  : Momentary state existing safety factor at point of analysis,  $S_{xm} = \frac{T_{uj}}{\frac{T_{xm}}{B}}$

$S_p$ : Permitted bare minimum safety factor, steady state (continuous operation)

$S_{pm}$ : Permitted bare minimum safety factor, momentary state.

The values of  $S_p$  and  $S_{pm}$  are as below:

	$S_p$	$S_{pm}$
Fabric belt	3.6	3.0
Steel cord belt, 1 or 2 lap splice	3.0	2.5
Steel cord belt, 3 or more lap slice	3.3	2.8

$K_G$ : Belt characteristic parameter. The values are as per table-27 refer book.

$h$ : Pulley rise relative to central roller, mm. Generally one should opt for  $h = 0$ , for belt feeder.

$L_y$ : Transition length, mm

$L_{yc}$ : Transition length including compensation effect, mm

### TRANSITION LENGTH (MINIMUM)

The transition length from flat to trough or trough to flat can be calculated as below. The required transition length is to be calculated for steady state and alternatively for momentary state; and use one which is more. Additional nomenclatures are as below.

$$K_1 = \left(\frac{b_f}{B}\right)^2 - \left(\frac{b_f}{B}\right)^3 \quad \text{and} \quad K_2 = \left(\frac{b_f}{B}\right)^3$$

The formulae can use mm or m. The answer will be in the unit so selected.

The value of  $h$  (if used) should not exceed following limiting condition for proper functioning. This is just mentioned as a part of standard formula for conveyors as well as feeders.

$h = (1 - \cos\lambda) \cdot b_f \div \sin\lambda$ . Preferably,  $h$  should be limited up to 15% of  $b_f \cdot \sin\lambda$ , and concave curvature zone of belt from pulley should not exceed last idler in transition zone to avoid interference with skirt board (if same is immediately after transition zone).

#### Steady state requirement

Firstly, find out value of  $f_{convex}$  for steady state.

$$f_{convex} = \frac{S_p}{\frac{b_f}{B}}$$

If  $S_x < f_{convex}$ , then only edge elongation is governing.

$$L_y \geq B \cdot \left( \frac{\lambda}{57.3} - \frac{h}{b_f} \right) \cdot \sqrt{\left( \frac{S_x \cdot S_p}{S_x - S_p} \right) \cdot K_G \cdot K_1} \quad \text{mm}$$

If  $S_x \geq f_{convex}$ , then only buckling is governing.

$$L_y \geq B \cdot \left( \frac{\lambda}{57.3} - \frac{h}{b_f} \right) \cdot \sqrt{S_x \cdot K_G \cdot K_2} \quad \text{mm}$$

The above calculation will give one value of transition distance  $L_y$ , as only one formula is applicable in particular situation.

### Momentary state requirement

Firstly, find out value of  $f_{convex}$  for momentary state.

$$f_{convex} = \frac{S_{pm}}{\frac{b_f}{B}}$$

If  $S_{xm} < f_{convex}$ , then only edge elongation is governing.

$$L_y \geq B \cdot \left( \frac{\lambda}{57.3} - \frac{h}{b_f} \right) \cdot \sqrt{\left( \frac{S_{xm} \cdot S_{pm}}{S_{xm} - S_{pm}} \right) \cdot K_G \cdot K_1} \quad \text{mm}$$

If  $S_{xm} \geq f_{convex}$ , then only edge buckling is governing.

$$L_y \geq B \cdot \left( \frac{\lambda}{57.3} - \frac{h}{b_f} \right) \cdot \sqrt{S_{xm} \cdot K_G \cdot K_2} \quad \text{mm}$$

The above calculation will give one value of transition distance  $L_y$ , as only one formula is applicable in particular situation.

Use the transition length  $L_y$ , as per steady state or momentary state, whichever is more. It is not necessary to have contingency margin for transition length, as compensation effect of belt portion beyond transition zone helps to reduce the strain in belt.

### **TRANSITION LENGTH MINIMUM, INCLUDING COMPENSATION EFFECT**

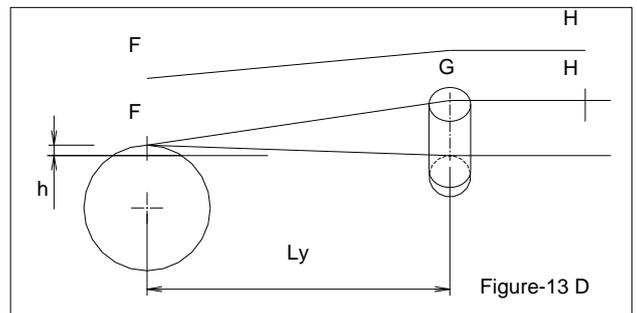
In case of extreme necessity, the transition length can be reduced by application of compensation factor (Comp).

In this case transition distance  $L_{yc}$  is as below.

$$L_{yc} = \frac{L_y^2}{\sqrt{L_y^2 + \text{Comp} \cdot \left( \frac{\lambda}{57.3} \right)^2 \cdot b_f^2}}$$

The value of Comp = 15 for fabric belts. The value of Comp = 100 for steel cord belts. The above formula is valid for  $L_y$  and  $b_f$  values in mm as well as m, common unit in one particular calculation.

Figure-13D shows length FG, which is considered to derive elongation and strain in belt. This elongation actually causes strain in FH instead of FG due to continuity of members. Actual strain is elongation ÷ FH,



which is less than elongation  $\div$  FG, and thereby the compensatory effect. This explains the compensatory effect. The transition length will have transition idlers of gradually increasing  $\lambda$ . The transition length as above should be calculated for each  $\lambda$ , to decide the location of each transition idler, measured from terminal pulley centerline. The transition length for intermediate transition idler can be selected as per the operating status as applicable to last idler of largest  $\lambda$ .

### Example-1

The belt feeder has following parameters.  $B = 1400$  mm,  $\lambda = 15^\circ$ ,  $b_f = 220$  mm (this is Bimax from table-4 of chapter - 6),  $h = 0$ , EP fabric belt 800/4, Joint efficiency  $Je = 0.75$ ,  $T_{uj} = 800 \times 0.75 = 600$  N/mm. Belt tension  $T_1 = 93683$  N,  $T_{1S} = 159557$  N. The data are partly from example - 2 of chapter - 11. Decide the transition distance at head end of belt feeder.

### Solution

The calculations for transition length at head end are as below

$$S_p = 3.6 \text{ and } S_{pm} = 3.0$$

$$K_1 = (b_f \div B)^2 - (b_f \div B)^3 = (220 \div 1400)^2 - (220 \div 1400)^3 = 0.02081$$

Steady state:

$$S_x = T_{uj} \div (T_x \div 1400) = 600 \div (93683 \div 1400) = 8.97$$

$$f_{convex} = S_p \div (b_f \div B) = 3.6 \div (220 \div 1400) = 22.91$$

Therefore,  $S_x < f_{convex}$

$$L_y = B \cdot \frac{\lambda}{57.3} \cdot \sqrt{\left( \frac{S_x \cdot S_p}{S_x - S_p} \right) \cdot K_G \cdot K_1} \text{ mm}$$

$$L_y = 1400 \times \frac{15}{57.3} \times \sqrt{\left( \frac{8.97 \times 3.6}{8.97 - 3.6} \right) \times 13 \times 0.02081} = 467.4 \text{ mm}$$

Momentary state:

$$S_{xm} = T_{uj} \div (T_{xm} \div 1400) = 600 \div (159557 \div 1400) = 5.26$$

$$f_{convex} = S_{pm} \div (b_f \div B) = 3.0 \div (220 \div 1400) = 19.09$$

Therefore,  $S_{xm} < f_{convex}$

$$L_y = B \cdot \frac{\lambda}{57.3} \cdot \sqrt{\left( \frac{S_{xm} \cdot S_{pm}}{S_{xm} - S_{pm}} \right) \cdot K_G \cdot K_1} = 1400 \times \frac{15}{57.3} \times \sqrt{\left( \frac{5.26 \times 3.0}{5.26 - 3.0} \right) \times 13 \times 0.02081} = 504 \text{ mm}$$

Hence required transition length is 504 mm, larger of above two values.

Similarly, the required minimum transition distance should also be calculated at tail end using tension  $T_3$  and  $T_{3S}$ . The value of required transition distance will be different for head end and tail end. The designer can use common value, based on higher of the two if he prefers. The reader to note that the calculation provides minimum transition distance and he is free to use larger value, but such enhancement proportion should be reasonably maintained for distance between two consecutive transition idlers (this need not be in a very precise manner).

### Book information applicability to apron feeder, addendum etc.

The flow balancing calculation procedures of chapter-7, hopper outlet pressure values of chapter-8; and feed zone forces analysis of chapter-9 are fairly applicable to apron feeders also (with appropriate considerations, as necessary). The chapter-11 tractive pull and power calculation procedure can be also extended to apron feeder (resistances  $R_{sk3}$ ,  $R_{cc}$ ,  $R_{cr}$ ,  $R_{ce}$ ,  $R_{ci}$ ,  $R_w$  and  $R_t$  as belt conveyor to be replaced by resistance as chain conveyor), and appropriate considerations as applicable. These are general hints only, for using book information for apron feeders.

### Belt feeder additional information

The expanding type skirt board with adequate expanding rates for flow balance 45 - 50% is essential for good performance together-with certain economy, particularly for belt feeder having-long feed zone. However, longer feed zone and dense material might still result- into exceptionally heavy construction. Such-situation can be averted by blocking.(closing) certain zones at interface in a alternative spaced manner; as shown in following figure arrangement - 1 and 2. This reduces the material load acting on belt, thereby reduction in tractive pull/ tensions/ power; without adverse effect on material transfer, from hopper to belt feeder. Also this feature practically allows the feeder to function as if it is receiving feed along the entire feed zone.

The material column mass acting on belt, should exclude closed zones or consider reduced column height on full interface, as-an equivalent effect. The equivalent reduced column height, in conjunction with full interface area will allow use of usual formulae. The usual column value  $C_2$  to be multiplied by multiplier to get reduced equivalent value of  $C_2$ . The multiplier value is 'material column mass on open area' divided by 'material column mass on total area of interface'. Tentatively this can be also taken as net area divided by total area.

The closing / blocking to be kept of equal length on both the sides of feed zone centre line. This would reasonably uphold the flow balancing condition. The designer can also do finer analysis if need be.

The other alternative method is to provide cross beam at appropriate level and pitch, sufficient to allow flow without arching, as shown in arrangement- 3. Tentatively its location can be at a height around 75% -to 100% of skirt board exit end width. The spacing and level to be decided considering lump size and flow-ability / sluggishness of material. This will also result into equivalent reduced column load, in conjunction with full area of interface.

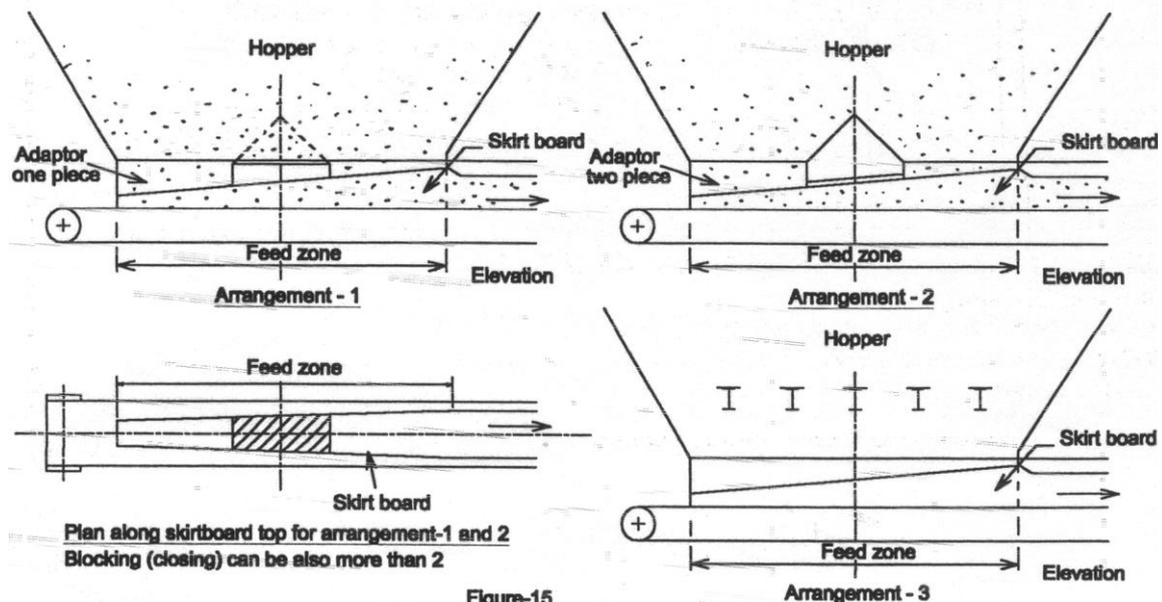


Figure-15